

# Mathematica 11.3 Integration Test Results

Test results for the 263 problems in "3.2.2 (f+g x)^m (h+i x)^q (A+B log(e ((a+b x) over (c+d x))^n))^p.m"

Problem 6: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 142 leaves, 5 steps):

$$\frac{B i (c + d x)}{b g^2 (a + b x)} - \frac{i (c + d x) \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{b g^2 (a + b x)} - \frac{d i \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right) \operatorname{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^2 g^2} + \frac{B d i \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^2 g^2}$$

Result (type 4, 317 leaves):

$$\frac{1}{2 b^2 g^2} i \left( \frac{2 A (-b c + a d)}{a + b x} + 2 A d \operatorname{Log} [a + b x] + 2 b B c \left( \frac{d \operatorname{Log} \left[ \frac{c}{d} + x \right]}{b c - a d} + \frac{d \operatorname{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right]}{-b c + a d} - \frac{1 + \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right]}{a + b x} \right) \right) + B d \left( \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 + \frac{2 a \left( 1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right)}{a + b x} + 2 \left( \frac{a}{a + b x} + \operatorname{Log} [a + b x] \right) \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right) + \frac{2 a \left( (-b c + a d) \operatorname{Log} \left[ \frac{c}{d} + x \right] + d (a + b x) (\operatorname{Log} [a + b x] - \operatorname{Log} [c + d x]) \right)}{(b c - a d) (a + b x)} - 2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \right)$$

Problem 14: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{a g + b g x} dx$$

Optimal (type 4, 276 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{B d (b c - a d) i^2 x}{2 b^2 g} - \frac{B (b c - a d)^2 i^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{2 b^3 g} + \frac{d (b c - a d) i^2 (a+b x) \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{b^3 g} + \\
 & \frac{i^2 (c+d x)^2 \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{2 b g} - \frac{3 B (b c - a d)^2 i^2 \text{Log}[c+d x]}{2 b^3 g} - \\
 & \frac{(b c - a d)^2 i^2 \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \text{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g} + \frac{B (b c - a d)^2 i^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g}
 \end{aligned}$$

Result (type 4, 615 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^3 g} i^2 \left( 4 b^2 B c^2 - 6 a b B c d + 2 a^2 B d^2 + 4 A b^2 c d x - b^2 B c d x - 2 a A b d^2 x + a b B d^2 x + \right. \\
 & A b^2 d^2 x^2 + B (b c - a d)^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 4 b^2 B c^2 \text{Log}\left[\frac{c}{d} + x\right] + 2 a b B c d \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 2 A b^2 c^2 \text{Log}[a+b x] - 4 a A b c d \text{Log}[a+b x] + 2 a^2 A d^2 \text{Log}[a+b x] - a^2 B d^2 \text{Log}[a+b x] + \\
 & 2 b^2 B c^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a+b x] - 4 a b B c d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a+b x] + \\
 & 2 a^2 B d^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a+b x] - 2 B \text{Log}\left[\frac{a}{b} + x\right] \left( a d (-2 b c + a d) + (b c - a d)^2 \text{Log}[a+b x] \right) - \\
 & 2 b^2 B c^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 4 a b B c d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] - \\
 & 2 a^2 B d^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 4 b^2 B c d x \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 2 a b B d^2 x \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] + b^2 B d^2 x^2 \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 2 b^2 B c^2 \text{Log}[a+b x] \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 4 a b B c d \text{Log}[a+b x] \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 2 a^2 B d^2 \text{Log}[a+b x] \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & \left. b^2 B c^2 \text{Log}[c+d x] - 2 B (b c - a d)^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right)
 \end{aligned}$$

### Problem 15: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 247 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) i^2 (c+d x)}{b^2 g^2 (a+b x)} + \frac{d^2 i^2 (a+b x) \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{b^3 g^2} - \\
 & \frac{(b c - a d) i^2 (c+d x) \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{b^2 g^2 (a+b x)} - \frac{B d (b c - a d) i^2 \text{Log}[c+d x]}{b^3 g^2} - \\
 & \frac{2 d (b c - a d) i^2 \left(A+B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \text{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g^2} + \frac{2 B d (b c - a d) i^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g^2}
 \end{aligned}$$

Result (type 4, 595 leaves):

$$\begin{aligned} & \frac{1}{b^3 g^2} i^2 \left( A b d^2 x - \frac{A (b c - a d)^2}{a + b x} + 2 A d (b c - a d) \text{Log}[a + b x] - \right. \\ & \left( b^2 B c^2 \left( -d (a + b x) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \right. \\ & \left. \left. (b c - a d) \left( 1 + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \right) \right) / \left( (b c - a d) (a + b x) \right) + \\ & b B c d \left( \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2 a \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right)}{a + b x} + 2 \left( \frac{a}{a + b x} + \text{Log}[a + b x] \right) \right. \\ & \left. \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) + \right. \\ & \left. \left( 2 a \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) \right) / \\ & \left. \left( (b c - a d) (a + b x) \right) - 2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) - \\ & B d^2 \left( - (a + b x) \left( -1 + \text{Log}\left[\frac{a}{b} + x\right] \right) + a \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{a^2 \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right)}{a + b x} + \right. \\ & b \left( \frac{c}{d} + x \right) \left( -1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - \\ & \left( b x - \frac{a^2}{a + b x} - 2 a \text{Log}[a + b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) + \\ & \left. \left( a^2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) \right) / \\ & \left. \left( (b c - a d) (a + b x) \right) - 2 a \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) \end{aligned}$$

**Problem 16: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^2 \left( A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 4, 230 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{B d i^2 (c+d x)}{b^2 g^3 (a+b x)} - \frac{B i^2 (c+d x)^2}{4 b g^3 (a+b x)^2} - \\
 & \frac{d i^2 (c+d x) \left( A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{b^2 g^3 (a+b x)} - \frac{i^2 (c+d x)^2 \left( A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 b g^3 (a+b x)^2} - \\
 & \frac{d^2 i^2 \left( A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \operatorname{Log}\left[1-\frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g^3} + \frac{B d^2 i^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^3 g^3}
 \end{aligned}$$

Result (type 4, 788 leaves):

$$\begin{aligned}
 & \frac{1}{4 b^3 g^3} i^2 \left( -\frac{2 A (b c-a d)^2}{(a+b x)^2} + \frac{8 A d (-b c+a d)}{a+b x} + \right. \\
 & 4 A d^2 \operatorname{Log}[a+b x] - \left( b^2 B c^2 \left( b^2 c^2-4 a b c d+a^2 d^2-2 b^2 c d x-2 a b d^2 x-2 b^2 d^2 x^2 + \right. \right. \\
 & \left. \left. 2 d^2 (a+b x)^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-2 d^2 (a+b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 b^2 c^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \right. \right. \\
 & \left. \left. 4 a b c d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+2 a^2 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \right) / \left( (b c-a d)^2 (a+b x)^2 \right) - \\
 & \frac{1}{(b c-a d)^2 (a+b x)^2} 2 b B c d \left( 3 a b^2 c^2-4 a^2 b c d+a^3 d^2+4 b^3 c^2 x-6 a b^2 c d x+2 a^2 b d^2 x - \right. \\
 & \left. 2 d (-2 b c+a d) (a+b x)^2 \operatorname{Log}[a+b x]+2 (b c-a d)^2 (a+2 b x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \right. \\
 & \left. 4 a^2 b c d \operatorname{Log}[c+d x]+2 a^3 d^2 \operatorname{Log}[c+d x]-8 a b^2 c d x \operatorname{Log}[c+d x]+ \right. \\
 & \left. 4 a^2 b d^2 x \operatorname{Log}[c+d x]-4 b^3 c d x^2 \operatorname{Log}[c+d x]+2 a b^2 d^2 x^2 \operatorname{Log}[c+d x] \right) + \\
 & B d^2 \left( 2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \frac{8 a \left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{a+b x} - \frac{a^2 \left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{(a+b x)^2} + \right. \\
 & \left. 2 \left( \frac{a(3 a+4 b x)}{(a+b x)^2} + 2 \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) + \right. \\
 & \left( 8 a \left( (-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d(a+b x) \left( \operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right) \right) \right) / \\
 & \left( (b c-a d) (a+b x) \right) + \frac{1}{(a+b x)^2} 2 a^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{1}{(b c-a d)^2} \right. \\
 & \left. d(a+b x) (b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x]) \right) - \\
 & \left. 4 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right)
 \end{aligned}$$

### Problem 17: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{(a g + b g x)^4} dx$$

Optimal (type 3, 89 leaves, 2 steps):

$$-\frac{B i^2 (c+d x)^3}{9 (b c - a d) g^4 (a+b x)^3} - \frac{i^2 (c+d x)^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{3 (b c - a d) g^4 (a+b x)^3}$$

Result (type 3, 186 leaves):

$$\frac{1}{9 b^3 g^4} i^2 \left( -\frac{(3 A + B) (b c - a d)^2}{(a+b x)^3} + \frac{3 (3 A + B) d (-b c + a d)}{(a+b x)^2} - \frac{3 (3 A + B) d^2}{a+b x} + \frac{3 B d^3 \operatorname{Log}[a+b x]}{-b c + a d} - \frac{3 B (a^2 d^2 + a b d (c + 3 d x) + b^2 (c^2 + 3 c d x + 3 d^2 x^2)) \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] + \frac{3 B d^3 \operatorname{Log}[c+d x]}{b c - a d}}{(a+b x)^3} \right)$$

### Problem 24: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{a g + b g x} dx$$

Optimal (type 4, 356 leaves, 14 steps):

$$\begin{aligned} & -\frac{5 B d (b c - a d)^2 i^3 x}{6 b^3 g} - \frac{B (b c - a d) i^3 (c+d x)^2}{6 b^2 g} - \frac{5 B (b c - a d)^3 i^3 \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right]}{6 b^4 g} + \\ & \frac{d (b c - a d)^2 i^3 (a+b x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{b^4 g} + \frac{(b c - a d) i^3 (c+d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{2 b^2 g} + \\ & \frac{i^3 (c+d x)^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{3 b g} - \frac{11 B (b c - a d)^3 i^3 \operatorname{Log}[c+d x]}{6 b^4 g} - \\ & \frac{(b c - a d)^3 i^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{Log} \left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g} + \frac{B (b c - a d)^3 i^3 \operatorname{PolyLog} \left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g} \end{aligned}$$

Result (type 4, 1004 leaves):

$$\frac{1}{6 b^4 g} i^3 \left( 18 b^3 B c^3 - 36 a b^2 B c^2 d + 24 a^2 b B c d^2 - 6 a^3 B d^3 + 18 A b^3 c^2 d x - 7 b^3 B c^2 d x - 18 a A b^2 c d^2 x + \right. \\
12 a b^2 B c d^2 x + 6 a^2 A b d^3 x - 5 a^2 b B d^3 x + 9 A b^3 c d^2 x^2 - b^3 B c d^2 x^2 - 3 a A b^2 d^3 x^2 + a b^2 B d^3 x^2 + \\
2 A b^3 d^3 x^3 + 3 B (b c - a d)^3 \text{Log}\left[\frac{a}{b} + x\right]^2 - 18 b^3 B c^3 \text{Log}\left[\frac{c}{d} + x\right] + 18 a b^2 B c^2 d \text{Log}\left[\frac{c}{d} + x\right] - \\
6 a^2 b B c d^2 \text{Log}\left[\frac{c}{d} + x\right] + 6 A b^3 c^3 \text{Log}[a + b x] - 18 a A b^2 c^2 d \text{Log}[a + b x] + \\
18 a^2 A b c d^2 \text{Log}[a + b x] - 9 a^2 b B c d^2 \text{Log}[a + b x] - 6 a^3 A d^3 \text{Log}[a + b x] + \\
5 a^3 B d^3 \text{Log}[a + b x] + 6 b^3 B c^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 18 a b^2 B c^2 d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + \\
18 a^2 b B c d^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 6 a^3 B d^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + \\
6 B \text{Log}\left[\frac{a}{b} + x\right] \left( a d (3 b^2 c^2 - 3 a b c d + a^2 d^2) - (b c - a d)^3 \text{Log}[a + b x] \right) - \\
6 b^3 B c^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 18 a b^2 B c^2 d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
18 a^2 b B c d^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 6 a^3 B d^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
18 b^3 B c^2 d x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 a b^2 B c d^2 x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 a^2 b B d^3 x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
9 b^3 B c d^2 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 3 a b^2 B d^3 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 b^3 B d^3 x^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
6 b^3 B c^3 \text{Log}[a + b x] \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 a b^2 B c^2 d \text{Log}[a + b x] \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
18 a^2 b B c d^2 \text{Log}[a + b x] \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 6 a^3 B d^3 \text{Log}[a + b x] \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
7 b^3 B c^3 \text{Log}[c + d x] - 3 a b^2 B c^2 d \text{Log}[c + d x] - 6 B (b c - a d)^3 \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \left. \right)$$

**Problem 25: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^3 \left( A + B \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 373 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{B d^2 (b c - a d) i^3 x}{2 b^3 g^2} - \frac{B (b c - a d)^2 i^3 (c + d x)}{b^3 g^2 (a + b x)} - \frac{B d (b c - a d)^2 i^3 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{2 b^4 g^2} + \\
 & \frac{2 d^2 (b c - a d) i^3 (a + b x) \left(A + B \text{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{b^4 g^2} - \frac{(b c - a d)^2 i^3 (c + d x) \left(A + B \text{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{b^3 g^2 (a + b x)} + \\
 & \frac{d i^3 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right)}{2 b^2 g^2} - \frac{5 B d (b c - a d)^2 i^3 \text{Log}[c + d x]}{2 b^4 g^2} - \\
 & \frac{3 d (b c - a d)^2 i^3 \left(A + B \text{Log}\left[\frac{e (a+b x)}{c+d x}\right]\right) \text{Log}\left[1 - \frac{b (c+d x)}{d (a+b x)}\right]}{b^4 g^2} + \frac{3 B d (b c - a d)^2 i^3 \text{PolyLog}\left[2, \frac{b (c+d x)}{d (a+b x)}\right]}{b^4 g^2}
 \end{aligned}$$

Result (type 4, 967 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^4 g^2} i^3 \left( 2 A b d^2 (3 b c - 2 a d) x + A b^2 d^3 x^2 - \frac{2 A (b c - a d)^3}{a + b x} + 6 A d (b c - a d)^2 \text{Log}[a + b x] - \right. \\
 & \left( 2 b^3 B c^3 \left( -d (a + b x) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \right. \\
 & \left. \left. (b c - a d) \left( 1 + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \right) \right) / ((b c - a d) (a + b x)) + \\
 & B d^3 \left( 4 a^2 - \frac{4 a b c}{d} + a b x - \frac{b^2 c x}{d} + \frac{2 a^3}{a + b x} + 3 a^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{4 a b c \text{Log}\left[\frac{c}{d} + x\right]}{d} - \right. \\
 & a^2 \text{Log}[a + b x] + \frac{2 a^3 d \text{Log}[a + b x]}{b c - a d} + 6 a^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 2 a^2 \text{Log}\left[\frac{a}{b} + x\right] \\
 & (2 + 3 \text{Log}[a + b x]) - 6 a^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] - 4 a b x \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \\
 & b^2 x^2 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \frac{2 a^3 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right]}{a + b x} + 6 a^2 \text{Log}[a + b x] \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \\
 & \left. \frac{b^2 c^2 \text{Log}[c + d x]}{d^2} + \frac{2 a^3 d \text{Log}[c + d x]}{-b c + a d} - 6 a^2 \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) + \\
 & 3 b^2 B c^2 d \left( \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2 a (1 + \text{Log}\left[\frac{a}{b} + x\right])}{a + b x} + 2 \left( \frac{a}{a + b x} + \text{Log}[a + b x] \right) \right. \\
 & \left. \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) + \right. \\
 & \left. \left( 2 a \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) \right) / \\
 & \left. \left( (b c - a d) (a + b x) - 2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) - \\
 & 6 b B c d^2 \left( - (a + b x) \left( -1 + \text{Log}\left[\frac{a}{b} + x\right] \right) + a \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{a^2 (1 + \text{Log}\left[\frac{a}{b} + x\right])}{a + b x} + \right. \\
 & b \left( \frac{c}{d} + x \right) \left( -1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - \\
 & \left( b x - \frac{a^2}{a + b x} - 2 a \text{Log}[a + b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) + \\
 & \left. \left( a^2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) \right) / \\
 & \left. \left( (b c - a d) (a + b x) - 2 a \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) \right)
 \end{aligned}$$



### Problem 26: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 4, 345 leaves, 9 steps):

$$\begin{aligned} & -\frac{2 B d (b c - a d) i^3 (c + d x)}{b^3 g^3 (a + b x)} - \frac{B (b c - a d) i^3 (c + d x)^2}{4 b^2 g^3 (a + b x)^2} + \\ & \frac{d^3 i^3 (a + b x) \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{b^4 g^3} - \frac{2 d (b c - a d) i^3 (c + d x) \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{b^3 g^3 (a + b x)} - \\ & \frac{(b c - a d) i^3 (c + d x)^2 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 b^2 g^3 (a + b x)^2} - \frac{B d^2 (b c - a d) i^3 \operatorname{Log}[c + d x]}{b^4 g^3} - \\ & \frac{3 d^2 (b c - a d) i^3 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g^3} + \frac{3 B d^2 (b c - a d) i^3 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g^3} \end{aligned}$$

Result (type 4, 1170 leaves):

$$\begin{aligned} & \frac{1}{4 b^4 g^3} i^3 \left( 4 A b d^3 x - \frac{2 A (b c - a d)^3}{(a + b x)^2} - \frac{12 A d (b c - a d)^2}{a + b x} + 12 A d^2 (b c - a d) \operatorname{Log}[a + b x] - \right. \\ & \left( b^3 B c^3 \left( b^2 c^2 - 4 a b c d + a^2 d^2 - 2 b^2 c d x - 2 a b d^2 x - 2 b^2 d^2 x^2 + \right. \right. \\ & \left. \left. 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 b^2 c^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \right. \right. \\ & \left. \left. 4 a b c d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 2 a^2 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \right) / \left( (b c - a d)^2 (a + b x)^2 \right) - \\ & \frac{1}{(b c - a d)^2 (a + b x)^2} 3 b^2 B c^2 d \left( 3 a b^2 c^2 - 4 a^2 b c d + a^3 d^2 + 4 b^3 c^2 x - 6 a b^2 c d x + 2 a^2 b d^2 x - \right. \\ & \left. 2 d (-2 b c + a d) (a + b x)^2 \operatorname{Log}[a + b x] + 2 (b c - a d)^2 (a + 2 b x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \right. \\ & \left. 4 a^2 b c d \operatorname{Log}[c + d x] + 2 a^3 d^2 \operatorname{Log}[c + d x] - 8 a b^2 c d x \operatorname{Log}[c + d x] + \right. \\ & \left. 4 a^2 b d^2 x \operatorname{Log}[c + d x] - 4 b^3 c d x^2 \operatorname{Log}[c + d x] + 2 a b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) + \\ & 3 b B c d^2 \left( 2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \frac{8 a \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{a + b x} - \frac{a^2 \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{(a + b x)^2} + \right. \\ & \left. 2 \left( \frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \operatorname{Log}[a + b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) + \right. \\ & \left. \left( 8 a \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) \right) / \end{aligned}$$

$$\begin{aligned} & \left( (b c - a d) (a + b x) + \frac{1}{(a + b x)^2} 2 a^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] + \frac{1}{(b c - a d)^2} \right. \right. \\ & \quad \left. \left. d (a + b x) (b c - a d + d (a + b x) \text{Log}[a + b x] - d (a + b x) \text{Log}[c + d x]) \right) \right) - \\ & 4 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) - \\ B d^3 & \left( -4 (a + b x) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right) + 6 a \text{Log} \left[ \frac{a}{b} + x \right]^2 + \frac{12 a^2 \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{a + b x} - \right. \\ & \frac{a^3 \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] \right)}{(a + b x)^2} + 4 b \left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right) + 2 \\ & \left. \left( -2 b x + \frac{a^2 (5 a + 6 b x)}{(a + b x)^2} + 6 a \text{Log}[a + b x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right) + \right. \\ & \left. \left( 12 a^2 \left( (-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) \right) / \\ & \left( (b c - a d) (a + b x) + \frac{1}{(a + b x)^2} 2 a^3 \left( \text{Log} \left[ \frac{c}{d} + x \right] + \frac{1}{(b c - a d)^2} \right. \right. \\ & \quad \left. \left. d (a + b x) (b c - a d + d (a + b x) \text{Log}[a + b x] - d (a + b x) \text{Log}[c + d x]) \right) \right) - \\ & 12 a \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \end{aligned}$$

**Problem 27: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^3 (A + B \text{Log}[\frac{e(a+bx)}{c+dx}])}{(a g + b g x)^4} dx$$

Optimal (type 4, 310 leaves, 9 steps):

$$\begin{aligned} & - \frac{B d^2 i^3 (c + d x)}{b^3 g^4 (a + b x)} - \frac{B d i^3 (c + d x)^2}{4 b^2 g^4 (a + b x)^2} - \frac{B i^3 (c + d x)^3}{9 b g^4 (a + b x)^3} - \frac{d^2 i^3 (c + d x) (A + B \text{Log}[\frac{e(a+bx)}{c+dx}])}{b^3 g^4 (a + b x)} - \\ & \frac{d i^3 (c + d x)^2 (A + B \text{Log}[\frac{e(a+bx)}{c+dx}])}{2 b^2 g^4 (a + b x)^2} - \frac{i^3 (c + d x)^3 (A + B \text{Log}[\frac{e(a+bx)}{c+dx}])}{3 b g^4 (a + b x)^3} - \\ & \frac{d^3 i^3 (A + B \text{Log}[\frac{e(a+bx)}{c+dx}]) \text{Log}[1 - \frac{b(c+dx)}{d(a+bx)}]}{b^4 g^4} + \frac{B d^3 i^3 \text{PolyLog}[2, \frac{b(c+dx)}{d(a+bx)}]}{b^4 g^4} \end{aligned}$$

Result (type 4, 1407 leaves):

$$\frac{1}{36 b^4 g^4}$$

$$\begin{aligned}
 & i^3 \left( -\frac{12 A (b c - a d)^3}{(a + b x)^3} - \frac{54 A d (b c - a d)^2}{(a + b x)^2} + \frac{108 A d^2 (-b c + a d)}{a + b x} + 36 A d^3 \text{Log}[a + b x] - \left( 2 b^3 B c^3 \right. \right. \\
 & \left. \left( 2 b^3 c^3 - 9 a b^2 c^2 d + 18 a^2 b c d^2 - 2 a^3 d^3 - 3 b^3 c^2 d x + 18 a b^2 c d^2 x + 12 a^2 b d^3 x + 6 b^3 c d^2 x^2 + \right. \right. \\
 & \left. \left. 21 a b^2 d^3 x^2 + 9 b^3 d^3 x^3 - 6 d^3 (a + b x)^3 \text{Log}\left[\frac{c}{d} + x\right] + 6 d^3 (a + b x)^3 \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \right. \right. \\
 & \left. \left. 6 b^3 c^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 a b^2 c^2 d \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \right. \right. \\
 & \left. \left. 18 a^2 b c d^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 6 a^3 d^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \right) / \left( (b c - a d)^3 (a + b x)^3 \right) + \\
 & 3 b^2 B c^2 d \left( -\frac{9 \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right)}{(a + b x)^2} + \frac{4 a \left( 1 + 3 \text{Log}\left[\frac{a}{b} + x\right] \right)}{(a + b x)^3} + \right. \\
 & \left. \frac{6 (a + 3 b x) \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right)}{(a + b x)^3} + 6 a \left( -\frac{2 \text{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{1}{(b c - a d)^3} \right. \right. \\
 & \left. \left. d \left( \frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \text{Log}[a + b x] - 2 d^2 \text{Log}[c + d x] \right) \right) \right) + \\
 & \left. \frac{18 \left( \text{Log}\left[\frac{c}{d} + x\right] + \frac{d(a + b x) (b c - a d + d(a + b x) \text{Log}[a + b x] - d(a + b x) \text{Log}[c + d x])}{(b c - a d)^2} \right)}{(a + b x)^2} \right) - \\
 & 6 b B c d^2 \left( \frac{18 \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right)}{a + b x} - \frac{9 a \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right)}{(a + b x)^2} + \frac{2 a^2 \left( 1 + 3 \text{Log}\left[\frac{a}{b} + x\right] \right)}{(a + b x)^3} - \right. \\
 & \left. \frac{1}{(a + b x)^3} 6 (a^2 + 3 a b x + 3 b^2 x^2) \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) + \right. \\
 & \left. \left( 18 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right) \right) \right) / \right. \\
 & \left. \left( (b c - a d) (a + b x) \right) + 3 a^2 \left( -\frac{2 \text{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{1}{(b c - a d)^3} \right. \right. \\
 & \left. \left. d \left( \frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \text{Log}[a + b x] - 2 d^2 \text{Log}[c + d x] \right) \right) \right) + \\
 & \frac{1}{(a + b x)^2} 18 a \left( \text{Log}\left[\frac{c}{d} + x\right] + \frac{1}{(b c - a d)^2} d (a + b x) \right. \\
 & \left. \left( b c - a d + d (a + b x) \text{Log}[a + b x] - d (a + b x) \text{Log}[c + d x] \right) \right) \right) + \\
 & B d^3 \left( 18 \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{108 a \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right)}{a + b x} - \frac{27 a^2 \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right)}{(a + b x)^2} + \right.
 \end{aligned}$$

$$\begin{aligned} & \frac{4 a^3 \left(1+3 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{(a+b x)^3}+6\left(\frac{a\left(11 a^2+27 a b x+18 b^2 x^2\right)}{(a+b x)^3}+6 \operatorname{Log}[a+b x]\right) \\ & \left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)+ \\ & \left(108 a\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right) / \\ & \left((b c-a d)(a+b x)+6 a^3\left(-\frac{2 \operatorname{Log}\left[\frac{c}{d}+x\right]}{(a+b x)^3}+\frac{1}{(b c-a d)^3}\right.\right. \\ & \left.\left.d\left(\frac{(b c-a d)(-b c+3 a d+2 b d x)}{(a+b x)^2}+2 d^2 \operatorname{Log}[a+b x]-2 d^2 \operatorname{Log}[c+d x]\right)\right)\right)+ \\ & \frac{1}{(a+b x)^2} 54 a^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\frac{1}{(b c-a d)^2} d(a+b x)\right. \\ & \left.(b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x]\right)- \\ & \left.36\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2,\frac{b(c+d x)}{b c-a d}\right]\right)\right) \end{aligned}$$

**Problem 28: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i+d i x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{(a g+b g x)^5} d x$$

Optimal (type 3, 89 leaves, 2 steps):

$$-\frac{B i^3(c+d x)^4}{16(b c-a d) g^5(a+b x)^4}-\frac{i^3(c+d x)^4\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{4(b c-a d) g^5(a+b x)^4}$$

Result (type 3, 248 leaves):

$$\begin{aligned} & \frac{1}{16 b^4(b c-a d) g^5(a+b x)^4} \\ & i^3\left(-\left(4 A+B\right)(b c-a d)^4+4\left(4 A+B\right) d(-b c+a d)^3(a+b x)-6\left(4 A+B\right) d^2(b c-a d)^2(a+b x)^2+\right. \\ & \left.4\left(4 A+B\right) d^3(-b c+a d)(a+b x)^3-4 B d^4(a+b x)^4 \operatorname{Log}[a+b x]-\right. \\ & \left.4 B(b c-a d)\left((b c-a d)^3+4 d(b c-a d)^2(a+b x)+6 d^2(b c-a d)(a+b x)^2+4 d^3(a+b x)^3\right)\right. \\ & \left.\operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+4 B d^4(a+b x)^4 \operatorname{Log}[c+d x]\right) \end{aligned}$$

### Problem 31: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{c i + d i x} dx$$

Optimal (type 4, 252 leaves, 6 steps):

$$\frac{g^3 (a+b x)^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{3 d i} - \frac{(b c - a d) g^3 (a+b x)^2 \left( 3 A + B + 3 B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{6 d^2 i} +$$

$$\frac{(b c - a d)^2 g^3 (a+b x) \left( 6 A + 5 B + 6 B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{6 d^3 i} +$$

$$\frac{(b c - a d)^3 g^3 \operatorname{Log} \left[ \frac{b c - a d}{b(c+d x)} \right] \left( 6 A + 11 B + 6 B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{6 d^4 i} + \frac{B (b c - a d)^3 g^3 \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{d^4 i}$$

Result (type 4, 947 leaves):

$$\frac{1}{6 d^4 i} g^3 \left( 6 b^3 B c^3 - 24 a b^2 B c^2 d + 36 a^2 b B c d^2 - 18 a^3 B d^3 + 6 A b^3 c^2 d x + 5 b^3 B c^2 d x - 18 a A b^2 c d^2 x - \right.$$

$$12 a b^2 B c d^2 x + 18 a^2 A b d^3 x + 7 a^2 b B d^3 x - 3 A b^3 c d^2 x^2 - b^3 B c d^2 x^2 + 9 a A b^2 d^3 x^2 + a b^2 B d^3 x^2 +$$

$$2 A b^3 d^3 x^3 - 6 b^3 B c^3 \operatorname{Log} \left[ \frac{c}{d} + x \right] + 18 a b^2 B c^2 d \operatorname{Log} \left[ \frac{c}{d} + x \right] - 18 a^2 b B c d^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] +$$

$$3 b^3 B c^3 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - 9 a b^2 B c^2 d \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 9 a^2 b B c d^2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - 3 a^3 B d^3 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 +$$

$$3 a^2 b B c d^2 \operatorname{Log} [a+b x] - 7 a^3 B d^3 \operatorname{Log} [a+b x] + 6 b^3 B c^2 d x \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] -$$

$$18 a b^2 B c d^2 x \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] + 18 a^2 b B d^3 x \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] - 3 b^3 B c d^2 x^2 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] +$$

$$9 a b^2 B d^3 x^2 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] + 2 b^3 B d^3 x^3 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] - 6 A b^3 c^3 \operatorname{Log} [c+d x] -$$

$$5 b^3 B c^3 \operatorname{Log} [c+d x] + 18 a A b^2 c^2 d \operatorname{Log} [c+d x] + 9 a b^2 B c^2 d \operatorname{Log} [c+d x] -$$

$$18 a^2 A b c d^2 \operatorname{Log} [c+d x] + 6 a^3 A d^3 \operatorname{Log} [c+d x] - 6 b^3 B c^3 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] +$$

$$18 a b^2 B c^2 d \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] - 18 a^2 b B c d^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] +$$

$$6 a^3 B d^3 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] - 6 b^3 B c^3 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \operatorname{Log} [c+d x] +$$

$$18 a b^2 B c^2 d \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \operatorname{Log} [c+d x] - 18 a^2 b B c d^2 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \operatorname{Log} [c+d x] +$$

$$6 a^3 B d^3 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \operatorname{Log} [c+d x] - 6 B \operatorname{Log} \left[ \frac{a}{b} + x \right]$$

$$\left( -a d (b^2 c^2 - 3 a b c d + 3 a^2 d^2) - (b c - a d)^3 \operatorname{Log} [c+d x] + (b c - a d)^3 \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] \right) -$$

$$6 B (b c - a d)^3 \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \Bigg)$$

**Problem 32: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^2 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{c i + d i x} dx$$

Optimal (type 4, 198 leaves, 5 steps):

$$\frac{g^2 (a + b x)^2 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d i} - \frac{(b c - a d) g^2 (a + b x) \left( 2 A + B + 2 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d^2 i} - \frac{(b c - a d)^2 g^2 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left( 2 A + 3 B + 2 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d^3 i} - \frac{B (b c - a d)^2 g^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^3 i}$$

Result (type 4, 575 leaves):

$$\frac{1}{2 d^3 i} g^2 \left( -2 b^2 B c^2 + 6 a b B c d - 4 a^2 B d^2 - 2 A b^2 c d x - b^2 B c d x + \right. \\ 4 a A b d^2 x + a b B d^2 x + A b^2 d^2 x^2 + 2 b^2 B c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - 4 a b B c d \operatorname{Log}\left[\frac{c}{d} + x\right] - \\ b^2 B c^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 a b B c d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a^2 B d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a^2 B d^2 \operatorname{Log}[a + b x] - \\ 2 b^2 B c d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 4 a b B d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + b^2 B d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\ 2 A b^2 c^2 \operatorname{Log}[c + d x] + b^2 B c^2 \operatorname{Log}[c + d x] - 4 a A b c d \operatorname{Log}[c + d x] + 2 a^2 A d^2 \operatorname{Log}[c + d x] + \\ 2 b^2 B c^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 4 a b B c d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\ 2 a^2 B d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 b^2 B c^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c + d x] - \\ 4 a b B c d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c + d x] + 2 a^2 B d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c + d x] - \\ \left. 2 B \operatorname{Log}\left[\frac{a}{b} + x\right] \left( a d (b c - 2 a d) + (b c - a d)^2 \operatorname{Log}[c + d x] - (b c - a d)^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + \right. \\ \left. 2 B (b c - a d)^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right)$$

**Problem 33: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x) \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{c i + d i x} dx$$

Optimal (type 4, 125 leaves, 4 steps):

$$\frac{g(a + b x) \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{d i} + \frac{(b c - a d) g \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left( A + B + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{d^2 i} + \frac{B (b c - a d) g \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^2 i}$$

Result (type 4, 291 leaves):

$$\begin{aligned} & \frac{1}{2 d^2 i} g \left( 2 b B c - 2 a B d + 2 A b d x - 2 b B c \operatorname{Log}\left[\frac{c}{d} + x\right] + \right. \\ & b B c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a B d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 b B d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 2 A b c \operatorname{Log}[c+d x] + \\ & 2 a A d \operatorname{Log}[c+d x] - 2 b B c \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] + 2 a B d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] - \\ & 2 b B c \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + 2 a B d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\ & \left. 2 B \operatorname{Log}\left[\frac{a}{b} + x\right] \left( a d + (b c - a d) \operatorname{Log}[c+d x] + (-b c + a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + \right. \\ & \left. (-2 b B c + 2 a B d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \end{aligned}$$

**Problem 39: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 341 leaves, 9 steps):

$$\begin{aligned} & \frac{3 B (b c - a d)^2 g^3 (a + b x)}{d^3 i^2 (c + d x)} - \frac{(6 A + 5 B) (b c - a d)^2 g^3 (a + b x)}{2 d^3 i^2 (c + d x)} - \\ & \frac{3 B (b c - a d)^2 g^3 (a + b x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^3 i^2 (c + d x)} + \frac{g^3 (a + b x)^3 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d i^2 (c + d x)} - \\ & \frac{(b c - a d) g^3 (a + b x)^2 \left( 3 A + B + 3 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d^2 i^2 (c + d x)} - \\ & \frac{b (b c - a d)^2 g^3 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left( 6 A + 5 B + 6 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{2 d^4 i^2} - \\ & \frac{3 b B (b c - a d)^2 g^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^2} \end{aligned}$$

Result (type 4, 956 leaves):

$$\begin{aligned}
 & \frac{1}{2 d^4 i^2} g^3 \left( -2 A b^2 d (2 b c - 3 a d) x + A b^3 d^2 x^2 + \frac{2 A (b c - a d)^3}{c + d x} + \right. \\
 & 6 A b (b c - a d)^2 \text{Log}[c + d x] + \left( 2 a^3 B d^3 \left( b c - a d + b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] + \right. \right. \\
 & \quad \left. \left. (-b c + a d) \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] - b c \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] - b d x \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) \right) / \\
 & \left( (b c - a d) (c + d x) \right) + 3 a^2 b B d^2 \left( -\text{Log}\left[\frac{c}{d} + x\right]^2 + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] + \right. \\
 & 2 \left( -\frac{c}{c + d x} + \frac{b c \text{Log}[a + b x]}{-b c + a d} + \frac{b c \text{Log}[c + d x]}{b c - a d} - \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right. \\
 & \quad \left. \left( \frac{c}{c + d x} + \text{Log}[c + d x] \right) + \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \left. \right) + \\
 & b^3 B \left( -4 c^2 + \frac{4 a c d}{b} - c d x + \frac{a d^2 x}{b} - \frac{2 c^3}{c + d x} + 4 c^2 \text{Log}\left[\frac{c}{d} + x\right] - 3 c^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - \right. \\
 & \quad \frac{a^2 d^2 \text{Log}[a + b x]}{b^2} + \frac{2 b c^3 \text{Log}[a + b x]}{-b c + a d} - 4 c d x \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \\
 & \quad d^2 x^2 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \frac{2 c^3 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right]}{c + d x} + c^2 \text{Log}[c + d x] + \frac{2 b c^3 \text{Log}[c + d x]}{b c - a d} + \\
 & 6 c^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] + 6 c^2 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \text{Log}[c + d x] - \\
 & \quad \frac{2 c \text{Log}\left[\frac{a}{b} + x\right] \left( 2 a d + 3 b c \text{Log}[c + d x] - 3 b c \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right)}{b} + \\
 & \quad \left. 6 c^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
 & 6 a b^2 B d \left( d \left( \frac{a}{b} + x \right) \left( -1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - (c + d x) \left( -1 + \text{Log}\left[\frac{c}{d} + x\right] \right) + c \text{Log}\left[\frac{c}{d} + x\right]^2 + \right. \\
 & \quad \frac{c^2 \left( 1 + \text{Log}\left[\frac{c}{d} + x\right] \right)}{c + d x} + c^2 \left( -\frac{\text{Log}\left[\frac{a}{b} + x\right]}{c + d x} + \frac{b \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right)}{b c - a d} \right) + \\
 & \quad \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \left( d x - \frac{c^2}{c + d x} - 2 c \text{Log}[c + d x] \right) - \\
 & \quad \left. 2 c \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \left. \right)
 \end{aligned}$$



### Problem 40: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 260 leaves, 8 steps):

$$\begin{aligned} & -\frac{2 B (b c - a d) g^2 (a + b x)}{d^2 i^2 (c + d x)} + \frac{(2 A + B) (b c - a d) g^2 (a + b x)}{d^2 i^2 (c + d x)} + \\ & \frac{2 B (b c - a d) g^2 (a + b x) \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right]}{d^2 i^2 (c + d x)} + \frac{g^2 (a + b x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{d i^2 (c + d x)} + \\ & \frac{b (b c - a d) g^2 \operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right] \left( 2 A + B + 2 B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{d^3 i^2} + \frac{2 b B (b c - a d) g^2 \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{b (c+d x)} \right]}{d^3 i^2} \end{aligned}$$

Result (type 4, 588 leaves):

$$\begin{aligned} & \frac{1}{d^3 i^2} g^2 \\ & \left( A b^2 d x - \frac{A (b c - a d)^2}{c + d x} + 2 A b (-b c + a d) \operatorname{Log}[c + d x] + \left( a^2 B d^2 \left( b c - a d + b (c + d x) \operatorname{Log} \left[ \frac{a}{b} + x \right] + \right. \right. \right. \\ & \quad \left. \left. (-b c + a d) \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] - b c \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] - b d x \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] \right) \right) / \\ & \left( (b c - a d) (c + d x) \right) + a b B d \left( -\operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log}[c + d x] + \right. \\ & \quad \left. 2 \left( -\frac{c}{c + d x} + \frac{b c \operatorname{Log}[a + b x]}{-b c + a d} + \frac{b c \operatorname{Log}[c + d x]}{b c - a d} - \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log}[c + d x] + \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \right. \\ & \quad \left. \left( \frac{c}{c + d x} + \operatorname{Log}[c + d x] \right) + \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] + 2 \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right) + \\ & b^2 B \left( d \left( \frac{a}{b} + x \right) \left( -1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right) - (c + d x) \left( -1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right) + c \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + \right. \\ & \quad \left. \frac{c^2 \left( 1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{c + d x} + c^2 \left( -\frac{\operatorname{Log} \left[ \frac{a}{b} + x \right]}{c + d x} + \frac{b \left( \operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right)}{b c - a d} \right) \right) + \\ & \quad \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \left( d x - \frac{c^2}{c + d x} - 2 c \operatorname{Log}[c + d x] \right) - \\ & \quad \left. 2 c \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right) \right) \end{aligned}$$

**Problem 41: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x) \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 160 leaves, 7 steps):

$$\begin{aligned} & -\frac{A g (a+b x)}{d i^2 (c+d x)} + \frac{B g (a+b x)}{d i^2 (c+d x)} - \frac{B g (a+b x) \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right]}{d i^2 (c+d x)} - \\ & \frac{b g \operatorname{Log} \left[ \frac{b c-a d}{b (c+d x)} \right] \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{d^2 i^2} - \frac{b B g \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^2 i^2} \end{aligned}$$

Result (type 4, 333 leaves):

$$\begin{aligned} & \frac{1}{2 d^2 i^2} \\ & g \left( \frac{2 A (b c-a d)}{c+d x} + 2 A b \operatorname{Log} [c+d x] + \left( 2 a B d \left( b c-a d + b (c+d x) \operatorname{Log} \left[ \frac{a}{b} + x \right] + (-b c+a d) \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] - b c \operatorname{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] - b d x \operatorname{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] \right) \right) / \\ & \left( (b c-a d) (c+d x) \right) + b B \left( -\operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] + \right. \\ & \left. 2 \left( -\frac{c}{c+d x} + \frac{b c \operatorname{Log} [a+b x]}{-b c+a d} + \frac{b c \operatorname{Log} [c+d x]}{b c-a d} - \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [c+d x] + \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right) \right) \\ & \left( \frac{c}{c+d x} + \operatorname{Log} [c+d x] \right) + \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] + 2 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right) \end{aligned}$$

**Problem 47: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 4, 361 leaves, 9 steps):

$$\begin{aligned} & -\frac{3 B (b c-a d) g^3 (a+b x)^2}{4 d^2 i^3 (c+d x)^2} - \frac{3 b B (b c-a d) g^3 (a+b x)}{d^3 i^3 (c+d x)} + \\ & \frac{b (3 A+B) (b c-a d) g^3 (a+b x)}{d^3 i^3 (c+d x)} + \frac{3 b B (b c-a d) g^3 (a+b x) \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right]}{d^3 i^3 (c+d x)} + \\ & \frac{g^3 (a+b x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{d i^3 (c+d x)^2} + \frac{(b c-a d) g^3 (a+b x)^2 \left( 3 A+B+3 B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{2 d^2 i^3 (c+d x)^2} + \\ & \frac{b^2 (b c-a d) g^3 \operatorname{Log} \left[ \frac{b c-a d}{b (c+d x)} \right] \left( 3 A+B+3 B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{d^4 i^3} + \frac{3 b^2 B (b c-a d) g^3 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^4 i^3} \end{aligned}$$

Result (type 4, 1161 leaves):

$$\begin{aligned}
 & \frac{1}{4 d^4 i^3} g^3 \left( 4 A b^3 d x + \frac{2 A (b c - a d)^3}{(c + d x)^2} - \frac{12 A b (b c - a d)^2}{c + d x} + 12 A b^2 (-b c + a d) \text{Log}[c + d x] - \right. \\
 & \frac{1}{(b c - a d)^2 (c + d x)^2} 3 a^2 b B d^2 \left( -b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - 2 b^2 c^2 d x + 6 a b c d^2 x - 4 a^2 d^3 x - \right. \\
 & 2 b (b c - 2 a d) (c + d x)^2 \text{Log}[a + b x] + 2 (b c - a d)^2 (c + 2 d x) \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \\
 & 2 b^2 c^3 \text{Log}[c + d x] - 4 a b c^2 d \text{Log}[c + d x] + 4 b^2 c^2 d x \text{Log}[c + d x] - \\
 & \left. 8 a b c d^2 x \text{Log}[c + d x] + 2 b^2 c d^2 x^2 \text{Log}[c + d x] - 4 a b d^3 x^2 \text{Log}[c + d x] \right) - \\
 & \left( a^3 B d^3 \left( -b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - 2 b^2 (c + d x)^2 \text{Log}\left[\frac{a}{b} + x\right] + \right. \right. \\
 & 2 (b c - a d)^2 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 2 b^2 c^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \\
 & \left. \left. 4 b^2 c d x \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b^2 d^2 x^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) \right) / \left( (b c - a d)^2 (c + d x)^2 \right) + \\
 & 3 a b^2 B d \left( -2 \text{Log}\left[\frac{c}{d} + x\right]^2 - \frac{8 c (1 + \text{Log}\left[\frac{c}{d} + x\right])}{c + d x} + \frac{c^2 (1 + 2 \text{Log}\left[\frac{c}{d} + x\right])}{(c + d x)^2} + \right. \\
 & \left. 8 c \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]}{c + d x} + \frac{b (\text{Log}[a + b x] - \text{Log}[c + d x])}{-b c + a d} \right) \right) + \\
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \left( \frac{c (3 c + 4 d x)}{(c + d x)^2} + 2 \text{Log}[c + d x] \right) + \\
 & \frac{1}{(c + d x)^2} 2 c^2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(b c - a d)^2} \right. \\
 & \left. b (c + d x) (b c - a d + b (c + d x) \text{Log}[a + b x] - b (c + d x) \text{Log}[c + d x]) \right) + \\
 & 4 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) - \\
 & b^3 B \left( -4 d \left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right) + 4 (c + d x) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right) - \right. \\
 & 6 c \text{Log}\left[\frac{c}{d} + x\right]^2 - \frac{12 c^2 (1 + \text{Log}\left[\frac{c}{d} + x\right])}{c + d x} + \frac{c^3 (1 + 2 \text{Log}\left[\frac{c}{d} + x\right])}{(c + d x)^2} - \\
 & \left. 12 c^2 \left( -\frac{\text{Log}\left[\frac{a}{b} + x\right]}{c + d x} + \frac{b (\text{Log}[a + b x] - \text{Log}[c + d x])}{b c - a d} \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \\
 & \left( -2dx + \frac{c^2(5c+6dx)}{(c+dx)^2} + 6c \text{Log}[c+dx] \right) + \frac{1}{(c+dx)^2} 2c^3 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(bc-ad)^2} \right. \\
 & \left. b(c+dx)(bc-ad+b(c+dx) \text{Log}[a+bx] - b(c+dx) \text{Log}[c+dx]) \right) + \\
 & 12c \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \Big) \Big)
 \end{aligned}$$

**Problem 48: Result more than twice size of optimal antiderivative.**

$$\int \frac{(ag + bgx)^2 (A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])}{(ci + dix)^3} dx$$

Optimal (type 4, 251 leaves, 8 steps):

$$\begin{aligned}
 & \frac{B g^2 (a+bx)^2}{4 d i^3 (c+dx)^2} - \frac{A b g^2 (a+bx)}{d^2 i^3 (c+dx)} + \frac{b B g^2 (a+bx)}{d^2 i^3 (c+dx)} - \\
 & \frac{b B g^2 (a+bx) \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]}{d^2 i^3 (c+dx)} - \frac{g^2 (a+bx)^2 (A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])}{2 d i^3 (c+dx)^2} - \\
 & \frac{b^2 g^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] (A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])}{d^3 i^3} - \frac{b^2 B g^2 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{d^3 i^3}
 \end{aligned}$$

Result (type 4, 790 leaves):

$$\begin{aligned}
 & \frac{1}{4 d^3 i^3} g^2 \left( -\frac{2 A (b c - a d)^2}{(c + d x)^2} + \frac{8 A b (b c - a d)}{c + d x} + 4 A b^2 \text{Log}[c + d x] - \right. \\
 & \frac{1}{(b c - a d)^2 (c + d x)^2} 2 a b B d \left( -b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - 2 b^2 c^2 d x + 6 a b c d^2 x - 4 a^2 d^3 x - \right. \\
 & 2 b (b c - 2 a d) (c + d x)^2 \text{Log}[a + b x] + 2 (b c - a d)^2 (c + 2 d x) \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + \\
 & 2 b^2 c^3 \text{Log}[c + d x] - 4 a b c^2 d \text{Log}[c + d x] + 4 b^2 c^2 d x \text{Log}[c + d x] - \\
 & \left. \left. 8 a b c d^2 x \text{Log}[c + d x] + 2 b^2 c d^2 x^2 \text{Log}[c + d x] - 4 a b d^3 x^2 \text{Log}[c + d x] \right) - \right. \\
 & \left. \left( a^2 B d^2 \left( -b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - 2 b^2 (c + d x)^2 \text{Log}\left[\frac{a}{b} + x\right] + \right. \right. \right. \\
 & 2 (b c - a d)^2 \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] + 2 b^2 c^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \\
 & \left. \left. 4 b^2 c d x \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b^2 d^2 x^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) \right) / \left( (b c - a d)^2 (c + d x)^2 \right) + \\
 & b^2 B \left( -2 \text{Log}\left[\frac{c}{d} + x\right]^2 - \frac{8 c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{c + d x} + \frac{c^2 \left(1 + 2 \text{Log}\left[\frac{c}{d} + x\right]\right)}{(c + d x)^2} + \right. \\
 & \left. 8 c \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]}{c + d x} + \frac{b (\text{Log}[a + b x] - \text{Log}[c + d x])}{-b c + a d} \right) + \right. \\
 & \left. 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \left( \frac{c (3 c + 4 d x)}{(c + d x)^2} + 2 \text{Log}[c + d x] \right) + \right. \\
 & \frac{1}{(c + d x)^2} 2 c^2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(b c - a d)^2} \right. \\
 & \left. \left. b (c + d x) (b c - a d + b (c + d x) \text{Log}[a + b x] - b (c + d x) \text{Log}[c + d x]) \right) + \right. \\
 & \left. \left. 4 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right)
 \end{aligned}$$

**Problem 55: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^3 (c i + d i x) \left( A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2 dx$$

Optimal (type 4, 539 leaves, 11 steps):

$$\begin{aligned} & \frac{3 B^2 (b c - a d)^4 g^3 i x}{10 b d^3} - \frac{3 B^2 (b c - a d)^3 g^3 i (c + d x)^2}{20 d^4} + \frac{b B^2 (b c - a d)^2 g^3 i (c + d x)^3}{30 d^4} \\ & \frac{B (b c - a d)^2 g^3 i (a + b x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{30 b^2 d} - \frac{B (b c - a d) g^3 i (a + b x)^4 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{10 b^2} + \\ & \frac{(b c - a d) g^3 i (a + b x)^4 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2}{20 b^2} + \frac{g^3 i (a + b x)^4 (c + d x) \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2}{5 b} + \\ & \frac{B (b c - a d)^3 g^3 i (a + b x)^2 \left( 3 A + B + 3 B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{60 b^2 d^2} - \\ & \frac{B (b c - a d)^4 g^3 i (a + b x) \left( 6 A + 5 B + 6 B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{60 b^2 d^3} - \\ & \frac{B (b c - a d)^5 g^3 i \operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right] \left( 6 A + 11 B + 6 B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{60 b^2 d^4} - \\ & \frac{B^2 (b c - a d)^5 g^3 i \operatorname{Log} [c + d x]}{10 b^2 d^4} - \frac{B^2 (b c - a d)^5 g^3 i \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{10 b^2 d^4} \end{aligned}$$

Result (type 4, 3093 leaves):

$$\begin{aligned} & \frac{1}{60 b^2 d^4} \\ & g^3 i \left( -6 b^5 B^2 c^5 + 36 a b^4 B^2 c^4 d - 90 a^2 b^3 B^2 c^3 d^2 + 90 a^3 b^2 B^2 c^2 d^3 - 24 a^4 b B^2 c d^4 - 6 a^5 B^2 d^5 - 6 A b^5 B \right. \\ & \quad c^4 d x + b^5 B^2 c^4 d x + 30 a A b^4 B c^3 d^2 x - 8 a b^4 B^2 c^3 d^2 x - 60 a^2 A b^3 B c^2 d^3 x + 24 a^2 b^3 B^2 c^2 d^3 x + \\ & \quad 60 a^3 A^2 b^2 c d^4 x + 30 a^3 A b^2 B c d^4 x - 28 a^3 b^2 B^2 c d^4 x + 6 a^4 A b B d^5 x + 11 a^4 b B^2 d^5 x + \\ & \quad 3 A b^5 B c^3 d^2 x^2 - 2 b^5 B^2 c^3 d^2 x^2 - 15 a A b^4 B c^2 d^3 x^2 + 12 a b^4 B^2 c^2 d^3 x^2 + 90 a^2 A^2 b^3 c d^4 x^2 - \\ & \quad 15 a^2 A b^3 B c d^4 x^2 - 18 a^2 b^3 B^2 c d^4 x^2 + 30 a^3 A^2 b^2 d^5 x^2 + 27 a^3 A b^2 B d^5 x^2 + 8 a^3 b^2 B^2 d^5 x^2 - \\ & \quad 2 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 60 a A^2 b^4 c d^4 x^3 - 20 a A b^4 B c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + \\ & \quad 60 a^2 A^2 b^3 d^5 x^3 + 22 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 15 A^2 b^5 c d^4 x^4 - 6 A b^5 B c d^4 x^4 + \\ & \quad 45 a A^2 b^4 d^5 x^4 + 6 a A b^4 B d^5 x^4 + 12 A^2 b^5 d^5 x^5 - 6 a b^4 B^2 c^4 d \operatorname{Log} \left[ \frac{a}{b} + x \right] + \\ & \quad 30 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] - 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[ \frac{a}{b} + x \right] + 30 a^4 b B^2 c d^4 \operatorname{Log} \left[ \frac{a}{b} + x \right] + \\ & \quad 6 a^5 B^2 d^5 \operatorname{Log} \left[ \frac{a}{b} + x \right] + 15 a^4 b B^2 c d^4 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 - 3 a^5 B^2 d^5 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 + 6 b^5 B^2 c^5 \operatorname{Log} \left[ \frac{c}{d} + x \right] - \\ & \quad 30 a b^4 B^2 c^4 d \operatorname{Log} \left[ \frac{c}{d} + x \right] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] - 30 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[ \frac{c}{d} + x \right] - \\ & \quad 6 a^4 b B^2 c d^4 \operatorname{Log} \left[ \frac{c}{d} + x \right] - 3 b^5 B^2 c^5 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 15 a b^4 B^2 c^4 d \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - \\ & \quad 30 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 30 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - 3 a^2 b^3 B^2 c^3 d^2 \operatorname{Log} [a + b x] + \\ & \quad 13 a^3 b^2 B^2 c^2 d^3 \operatorname{Log} [a + b x] + 30 a^4 A b B c d^4 \operatorname{Log} [a + b x] + a^4 b B^2 c d^4 \operatorname{Log} [a + b x] - \\ & \quad 6 a^5 A B d^5 \operatorname{Log} [a + b x] - 11 a^5 B^2 d^5 \operatorname{Log} [a + b x] - 30 a^4 b B^2 c d^4 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [a + b x] + \\ & \quad 6 a^5 B^2 d^5 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 30 a^4 b B^2 c d^4 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [a + b x] - \\ & \quad 6 a^5 B^2 d^5 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [a + b x] - 30 a^4 b B^2 c d^4 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + \end{aligned}$$

$$\begin{aligned}
 & 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-6 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 30 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-60 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 120 a^3 A b^2 B c d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+30 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 6 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+3 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 15 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+180 a^2 A b^3 B c d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 15 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+60 a^3 A b^2 B d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 27 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-2 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 120 a A b^4 B c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-20 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 120 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+22 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 30 A b^5 B c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 90 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+30 a^4 b B^2 c d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 6 a^5 B^2 d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+60 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
 & 90 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
 & 60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+60 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
 & 15 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+45 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
 & 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+6 A b^5 B c^5 \operatorname{Log}[c+d x]-b^5 B^2 c^5 \operatorname{Log}[c+d x]- \\
 & 30 a A b^4 B c^4 d \operatorname{Log}[c+d x]+11 a b^4 B^2 c^4 d \operatorname{Log}[c+d x]+60 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c+d x]- \\
 & 37 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+d x]-60 a^3 A b^2 B c^2 d^3 \operatorname{Log}[c+d x]+27 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+d x]- \\
 & 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
 & 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
 & 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
 & 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+
 \end{aligned}$$

$$\begin{aligned}
 & 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\
 & 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\
 & 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 6 b^2 B^2 c^2 \left(b^3 c^3 - 5 a b^2 c^2 d + 10 a^2 b c d^2 - 10 a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 6 a^4 B^2 d^4 (-5 b c+a d) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 56: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^2 (c i + d i x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2 dx$$

Optimal (type 4, 450 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{B^2(b c-a d)^3 g^2 i x}{3 b d^2} + \frac{B^2(b c-a d)^2 g^2 i(c+d x)^2}{12 d^3} - \\
 & \frac{B(b c-a d)^2 g^2 i(a+b x)^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{12 b^2 d} - \frac{B(b c-a d) g^2 i(a+b x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{6 b^2} + \\
 & \frac{(b c-a d) g^2 i(a+b x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{12 b^2} + \frac{g^2 i(a+b x)^3(c+d x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{4 b} + \\
 & \frac{B(b c-a d)^3 g^2 i(a+b x)\left(2 A+B+2 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{12 b^2 d^2} + \\
 & \frac{B(b c-a d)^4 g^2 i \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]\left(2 A+3 B+2 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{12 b^2 d^3} + \\
 & \frac{B^2(b c-a d)^4 g^2 i \operatorname{Log}[c+d x]}{6 b^2 d^3} + \frac{B^2(b c-a d)^4 g^2 i \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{6 b^2 d^3}
 \end{aligned}$$

Result (type 4, 2270 leaves):

$$\begin{aligned}
 & \frac{1}{12 b^2 d^3} \\
 & g^2 i \left(2 b^4 B^2 c^4 - 10 a b^3 B^2 c^3 d + 12 a^2 b^2 B^2 c^2 d^2 - 2 a^3 b B^2 c d^3 - 2 a^4 B^2 d^4 + 2 A b^4 B c^3 d x - b^4 B^2 c^3 d x - \right. \\
 & 8 a A b^3 B c^2 d^2 x + 5 a b^3 B^2 c^2 d^2 x + 12 a^2 A^2 b^2 c d^3 x + 4 a^2 A b^2 B c d^3 x - 7 a^2 b^2 B^2 c d^3 x + \\
 & 2 a^3 A b B d^4 x + 3 a^3 b B^2 d^4 x - A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 + 12 a A^2 b^3 c d^3 x^2 - \\
 & 4 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 + 6 a^2 A^2 b^2 d^4 x^2 + 5 a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + \\
 & \left. 4 A^2 b^4 c d^3 x^3 - 2 A b^4 B c d^3 x^3 + 8 a A^2 b^3 d^4 x^3 + 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 + \right)
 \end{aligned}$$



$$\begin{aligned}
 & 2 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right]-8 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]+4 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]+ \\
 & 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]+4 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]+ \\
 & 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right]-4 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-2 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]+ \\
 & b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-4 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2+6 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+ \\
 & a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a+b x]+8 a^3 A b B c d^3 \operatorname{Log}[a+b x]+2 a^3 b B^2 c d^3 \operatorname{Log}[a+b x]- \\
 & 2 a^4 A B d^4 \operatorname{Log}[a+b x]-3 a^4 B^2 d^4 \operatorname{Log}[a+b x]-8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+ \\
 & 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]-8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 8 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+24 a^2 A b^2 B c d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 4 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+2 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-4 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 12 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+5 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 8 A b^4 B c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 16 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 8 a^3 b B^2 c d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-2 a^4 B^2 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 12 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
 & 6 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+4 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
 & 8 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2- \\
 & 2 A b^4 B c^4 \operatorname{Log}[c+d x]+b^4 B^2 c^4 \operatorname{Log}[c+d x]+8 a A b^3 B c^3 d \operatorname{Log}[c+d x]- \\
 & 6 a b^3 B^2 c^3 d \operatorname{Log}[c+d x]-12 a^2 A b^2 B c^2 d^2 \operatorname{Log}[c+d x]+5 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c+d x]+ \\
 & 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
 & 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
 & 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-
 \end{aligned}$$

$$\begin{aligned}
 & 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - \\
 & 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 2 b^2 B^2 c^2\left(b^2 c^2-4 a b c d+6 a^2 d^2\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 2 a^3 B^2 d^3(-4 b c+a d) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 57: Result more than twice size of optimal antiderivative.**

$$\int (a g+b g x)(c i+d i x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2 d x$$

Optimal (type 4, 343 leaves, 9 steps):

$$\begin{aligned}
 & \frac{B^2(b c-a d)^2 g i x}{3 b d}-\frac{B(b c-a d)^2 g i(a+b x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b^2 d}- \\
 & \frac{B(b c-a d) g i(a+b x)^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b^2}+ \\
 & \frac{(b c-a d) g i(a+b x)^2\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{6 b^2}+\frac{g i(a+b x)^2(c+d x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{3 b}- \\
 & \frac{B(b c-a d)^3 g i \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]\left(A+B+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b^2 d^2}- \\
 & \frac{B^2(b c-a d)^3 g i \operatorname{Log}[c+d x]}{3 b^2 d^2}-\frac{B^2(b c-a d)^3 g i \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{3 b^2 d^2}
 \end{aligned}$$

Result (type 4, 1443 leaves):

$$\frac{1}{6 b^2 d^2}$$

$$\begin{aligned} & \text{g i} \left( -2 b^3 B^2 c^3 + 2 a b^2 B^2 c^2 d + 2 a^2 b B^2 c d^2 - 2 a^3 B^2 d^3 - 2 A b^3 B c^2 d x + 2 b^3 B^2 c^2 d x + 6 a A^2 b^2 c d^2 x - \right. \\ & 4 a b^2 B^2 c d^2 x + 2 a^2 A b B d^3 x + 2 a^2 b B^2 d^3 x + 3 A^2 b^3 c d^2 x^2 - 2 A b^3 B c d^2 x^2 + 3 a A^2 b^2 d^3 x^2 + \\ & 2 a A b^2 B d^3 x^2 + 2 A^2 b^3 d^3 x^3 - 2 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\ & 3 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] - 2 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\ & b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 3 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 6 a^2 A b B c d^2 \operatorname{Log}[a + b x] + \\ & 2 a^2 b B^2 c d^2 \operatorname{Log}[a + b x] - 2 a^3 A B d^3 \operatorname{Log}[a + b x] - 2 a^3 B^2 d^3 \operatorname{Log}[a + b x] - \\ & 6 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\ & 6 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 2 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\ & 6 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\ & 2 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a A b^2 B c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 2 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 A b^3 B c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 2 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 6 a A b^2 B d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 4 A b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 6 a^2 b B^2 c d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 2 a^3 B^2 d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\ & 6 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 3 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + \\ & 3 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 b^3 B^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 A b^3 B c^3 \operatorname{Log}[c + d x] - \\ & 2 b^3 B^2 c^3 \operatorname{Log}[c + d x] - 6 a A b^2 B c^2 d \operatorname{Log}[c + d x] + 2 a b^2 B^2 c^2 d \operatorname{Log}[c + d x] - \\ & 2 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + 6 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\ & 2 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\ & 2 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] - 6 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] \operatorname{Log}[c + d x] + \\ & 2 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 6 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \\ & 2 b^2 B^2 c^2 (b c - 3 a d) \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + 2 a^2 B^2 d^2 (-3 b c + a d) \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \Big) \end{aligned}$$

**Problem 58: Result more than twice size of optimal antiderivative.**

$$\int (c i + d i x) \left( A + B \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 203 leaves, 7 steps):

$$\begin{aligned} & - \frac{B (b c - a d) i (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right)}{b^2} + \\ & \frac{i (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right)^2}{2 d} + \frac{B^2 (b c - a d)^2 i \operatorname{Log} [c + d x]}{b^2 d} + \\ & \frac{B (b c - a d)^2 i \left( A + B \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right) \operatorname{Log} \left[ 1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d} - \frac{B^2 (b c - a d)^2 i \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d} \end{aligned}$$

Result (type 4, 734 leaves):

$$\begin{aligned} & i \left( A^2 c x + \frac{1}{2} A^2 d x^2 - \frac{2 A B c \left( -a d \operatorname{Log} [a + b x] - b d x \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] + b c \operatorname{Log} [c + d x] \right)}{b d} \right) + \\ & A B \left( -c x + \frac{a d x}{b} - \frac{a^2 d \operatorname{Log} [a + b x]}{b^2} + d x^2 \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] + \frac{c^2 \operatorname{Log} [c + d x]}{d} \right) + \\ & \frac{1}{b d} B^2 c \left( a d \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 + b c \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - 2 a d \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [a + b x] + 2 a d \operatorname{Log} \left[ \frac{c}{d} + x \right] \right. \\ & \quad \left. \operatorname{Log} [a + b x] - 2 a d \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + 2 a d \operatorname{Log} [a + b x] \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] + \right. \\ & \quad \left. b d x \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right]^2 + 2 b c \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c + d x] - \right. \\ & \quad \left. 2 b c \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \operatorname{Log} [c + d x] - 2 b c \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] - \right. \\ & \quad \left. 2 b c \operatorname{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] - 2 a d \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) + \frac{1}{2} B^2 d \\ & \left( x^2 \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right]^2 - \frac{1}{b^2 d^2} \left( -2 d (-b c + a d) (a + b x) \left( -1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right) + a^2 d^2 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 - \right. \right. \\ & \quad \left. \left. 2 b (b c - a d) (c + d x) \left( -1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right) + b^2 c^2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - 2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \right. \right. \right. \\ & \quad \left. \left. \left. \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right) \left( a^2 d^2 \operatorname{Log} [a + b x] - b (d (-b c + a d) x + b c^2 \operatorname{Log} [c + d x]) \right) - \right. \right. \\ & \quad \left. \left. 2 b^2 c^2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right) - \right. \right. \\ & \quad \left. \left. 2 a^2 d^2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) \end{aligned}$$

### Problem 59: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 286 leaves, 8 steps):

$$\begin{aligned} & \frac{2 B (b c - a d) i \operatorname{Log} \left[ \frac{b c - a d}{b (c + d x)} \right] \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{b^2 g} + \frac{d i (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{b^2 g} - \\ & \frac{(b c - a d) i \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2 \operatorname{Log} \left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^2 g} + \frac{2 B^2 (b c - a d) i \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{b^2 g} + \\ & \frac{2 B (b c - a d) i \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{PolyLog} \left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^2 g} + \frac{2 B^2 (b c - a d) i \operatorname{PolyLog} \left[ 3, \frac{b(c+d x)}{d(a+b x)} \right]}{b^2 g} \end{aligned}$$

Result (type 4, 1196 leaves):

$$\begin{aligned} & \frac{1}{3 b^2 g} i \left( 3 A^2 b d x + 3 A^2 (b c - a d) \operatorname{Log}[a + b x] - \right. \\ & 3 A B \left( a d \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 - 2 a d \operatorname{Log} \left[ \frac{a}{b} + x \right] (1 + \operatorname{Log}[a + b x]) + \right. \\ & 2 \left( -b c + a d + \operatorname{Log} \left[ \frac{c}{d} + x \right] \left( b c + a d \operatorname{Log}[a + b x] - a d \operatorname{Log} \left[ \frac{d(a+b x)}{-b c + a d} \right] \right) + \right. \\ & \left. \left. (-b d x + a d \operatorname{Log}[a + b x]) \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] - 2 a d \operatorname{PolyLog} \left[ 2, \frac{b(c+d x)}{b c - a d} \right] \right) + \right. \\ & 3 A b B c \left( \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 - 2 \operatorname{Log}[a + b x] \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) - \right. \\ & \left. 2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d(a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{b(c+d x)}{b c - a d} \right] \right) \right) - \\ & B^2 \left( a d \operatorname{Log} \left[ \frac{a}{b} + x \right]^3 - 3 d (a + b x) \left( 2 - 2 \operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 \right) - \right. \\ & 3 b (c + d x) \left( 2 - 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 \right) - \\ & 3 d (b x - a \operatorname{Log}[a + b x]) \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2 + \\ & 6 \left( a d + 2 b d x - b d x \operatorname{Log} \left[ \frac{c}{d} + x \right] - b c \operatorname{Log}[c + d x] + \right. \\ & \operatorname{Log} \left[ \frac{a}{b} + x \right] \left( -d (a + b x) + d (a + b x) \operatorname{Log} \left[ \frac{c}{d} + x \right] + (b c - a d) \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] \right) + \\ & \left. (b c - a d) \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right) - 3 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \end{aligned}$$

$$\begin{aligned}
 & \left( -2 b c + 2 a d - 2 d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\
 & \quad \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \left( b (c + d x) - a d \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) - 2 a d \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) - \\
 & 3 a d \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + \right. \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) + 3 a d \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \\
 & \quad \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right) \Big) + \\
 & b B^2 c \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 3 \operatorname{Log}[a + b x] \right. \\
 & \quad \left. \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2 + \right. \\
 & \quad \left. 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( -\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + \right. \\
 & \quad \left. 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 3 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \right. \\
 & \quad \left. \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) - \\
 & \quad \left. 6 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right) \Big)
 \end{aligned}$$

**Problem 60: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x) \left( A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{(a g + b g x)^2} dx$$

Optimal (type 4, 241 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{2 B^2 i (c + d x)}{b g^2 (a + b x)} - \frac{2 B i (c + d x) \left( A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)}{b g^2 (a + b x)} - \\
 & \frac{i (c + d x) \left( A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{b g^2 (a + b x)} - \frac{d i \left( A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2 \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g^2} + \\
 & \frac{2 B d i \left( A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g^2} + \frac{2 B^2 d i \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{d (a + b x)}\right]}{b^2 g^2}
 \end{aligned}$$

Result (type 4, 1155 leaves):



$$\begin{aligned}
 & 3 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \left( \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2a(1 + \text{Log}\left[\frac{a}{b} + x\right])}{a+bx} + \right. \\
 & \left. \left( 2a \left( (-bc+ad) \text{Log}\left[\frac{c}{d} + x\right] + d(a+bx) (\text{Log}[a+bx] - \text{Log}[c+dx]) \right) \right) / \right. \\
 & \left. \left( (bc-ad)(a+bx) - 2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right) - \\
 & \left. \left. \left. 6 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \right)
 \end{aligned}$$

**Problem 64: Result more than twice size of optimal antiderivative.**

$$\int (ag + bgx)^3 (ci + dix)^2 \left( A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 dx$$

Optimal (type 4, 711 leaves, 17 steps):



$$\begin{aligned}
 & \frac{3 B^2 (b c - a d)^5 g^3 i^2 x}{20 b^2 d^3} + \frac{B^2 (b c - a d)^2 g^3 i^2 (a + b x)^4}{60 b^3} - \frac{3 B^2 (b c - a d)^4 g^3 i^2 (c + d x)^2}{40 b d^4} + \\
 & \frac{B^2 (b c - a d)^3 g^3 i^2 (c + d x)^3}{60 d^4} - \frac{B (b c - a d)^3 g^3 i^2 (a + b x)^3 \left( A + B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)}{90 b^3 d} - \\
 & \frac{B (b c - a d)^2 g^3 i^2 (a + b x)^4 \left( A + B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)}{20 b^3} - \\
 & \frac{B (b c - a d) g^3 i^2 (a + b x)^4 (c + d x) \left( A + B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)}{15 b^2} + \\
 & \frac{(b c - a d)^2 g^3 i^2 (a + b x)^4 \left( A + B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{60 b^3} + \\
 & \frac{(b c - a d) g^3 i^2 (a + b x)^4 (c + d x) \left( A + B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{15 b^2} + \\
 & \frac{g^3 i^2 (a + b x)^4 (c + d x)^2 \left( A + B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{6 b} + \\
 & \frac{B (b c - a d)^4 g^3 i^2 (a + b x)^2 \left( 3 A + B + 3 B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)}{180 b^3 d^2} - \\
 & \frac{B (b c - a d)^5 g^3 i^2 (a + b x) \left( 6 A + 5 B + 6 B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)}{180 b^3 d^3} - \\
 & \frac{B (b c - a d)^6 g^3 i^2 \log\left[\frac{b c - a d}{b (c + d x)}\right] \left( 6 A + 11 B + 6 B \log\left[\frac{e(a+b x)}{c+d x}\right] \right)}{180 b^3 d^4} - \\
 & \frac{B^2 (b c - a d)^6 g^3 i^2 \log[c + d x]}{20 b^3 d^4} - \frac{B^2 (b c - a d)^6 g^3 i^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{30 b^3 d^4}
 \end{aligned}$$

Result (type 4, 4173 leaves):

$$\begin{aligned}
 & \frac{1}{360 b^3 d^4} g^3 i^2 \left( -12 b^6 B^2 c^6 + 84 a b^5 B^2 c^5 d - 252 a^2 b^4 B^2 c^4 d^2 + 240 a^3 b^3 B^2 c^3 d^3 + 12 a^4 b^2 B^2 c^2 d^4 - \right. \\
 & 84 a^5 b B^2 c d^5 + 12 a^6 B^2 d^6 - 12 A b^6 B c^5 d x + 8 b^6 B^2 c^5 d x + 72 a A b^5 B c^4 d^2 x - 54 a b^5 B^2 c^4 d^2 x - \\
 & 180 a^2 A b^4 B c^3 d^3 x + 154 a^2 b^4 B^2 c^3 d^3 x + 360 a^3 A^2 b^3 c^2 d^4 x + 60 a^3 A b^3 B c^2 d^4 x - \\
 & 194 a^3 b^3 B^2 c^2 d^4 x + 72 a^4 A b^2 B c d^5 x + 102 a^4 b^2 B^2 c d^5 x - 12 a^5 A b B d^6 x - 16 a^5 b B^2 d^6 x + \\
 & 6 A b^6 B c^4 d^2 x^2 - 7 b^6 B^2 c^4 d^2 x^2 - 36 a A b^5 B c^3 d^3 x^2 + 46 a b^5 B^2 c^3 d^3 x^2 + 540 a^2 A^2 b^4 c^2 d^4 x^2 - \\
 & 180 a^2 A b^4 B c^2 d^4 x^2 - 60 a^2 b^4 B^2 c^2 d^4 x^2 + 360 a^3 A^2 b^3 c d^5 x^2 + 204 a^3 A b^3 B c d^5 x^2 + \\
 & 10 a^3 b^3 B^2 c d^5 x^2 + 6 a^4 A b^2 B d^6 x^2 + 11 a^4 b^2 B^2 d^6 x^2 - 4 A b^6 B c^3 d^3 x^3 + 6 b^6 B^2 c^3 d^3 x^3 + \\
 & 360 a A^2 b^5 c^2 d^4 x^3 - 156 a A b^5 B c^2 d^4 x^3 + 6 a b^5 B^2 c^2 d^4 x^3 + 720 a^2 A^2 b^4 c d^5 x^3 + \\
 & 84 a^2 A b^4 B c d^5 x^3 - 30 a^2 b^4 B^2 c d^5 x^3 + 120 a^3 A^2 b^3 d^6 x^3 + 76 a^3 A b^3 B d^6 x^3 + \\
 & 18 a^3 b^3 B^2 d^6 x^3 + 90 A^2 b^6 c^2 d^4 x^4 - 42 A b^6 B c^2 d^4 x^4 + 6 b^6 B^2 c^2 d^4 x^4 + 540 a A^2 b^5 c d^5 x^4 - \\
 & 36 a A b^5 B c d^5 x^4 - 12 a b^5 B^2 c d^5 x^4 + 270 a^2 A^2 b^4 d^6 x^4 + 78 a^2 A b^4 B d^6 x^4 + 6 a^2 b^4 B^2 d^6 x^4 + \\
 & 144 A^2 b^6 c d^5 x^5 - 24 A b^6 B c d^5 x^5 + 216 a A^2 b^5 d^6 x^5 + 24 a A b^5 B d^6 x^5 + 60 A^2 b^6 d^6 x^6 - \\
 & 12 a b^5 B^2 c^5 d \log\left[\frac{a}{b} + x\right] + 72 a^2 b^4 B^2 c^4 d^2 \log\left[\frac{a}{b} + x\right] - 180 a^3 b^3 B^2 c^3 d^3 \log\left[\frac{a}{b} + x\right] + \\
 & 60 a^4 b^2 B^2 c^2 d^4 \log\left[\frac{a}{b} + x\right] + 72 a^5 b B^2 c d^5 \log\left[\frac{a}{b} + x\right] - 12 a^6 B^2 d^6 \log\left[\frac{a}{b} + x\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 90 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 36 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 6 a^6 B^2 d^6 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \\
 & 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d}+x\right] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d}+x\right] + 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
 & 60 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] - 72 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] + 12 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
 & 6 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 36 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 90 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + \\
 & 120 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 6 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}[a+b x] + 32 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[a+b x] + \\
 & 180 a^4 A b^2 B c^2 d^4 \operatorname{Log}[a+b x] + 66 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[a+b x] - 72 a^5 A B B c d^5 \operatorname{Log}[a+b x] - \\
 & 108 a^5 b B^2 c d^5 \operatorname{Log}[a+b x] + 12 a^6 A B d^6 \operatorname{Log}[a+b x] + 16 a^6 B^2 d^6 \operatorname{Log}[a+b x] - \\
 & 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] - \\
 & 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
 & 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
 & 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 72 a^5 b B^2 c d^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - \\
 & 12 a^6 B^2 d^6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 12 b^6 B^2 c^5 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 72 a b^5 B^2 c^4 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 180 a^2 b^4 B^2 c^3 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 720 a^3 A b^3 B c^2 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 60 a^3 b^3 B^2 c^2 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 72 a^4 b^2 B^2 c d^5 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 12 a^5 b B^2 d^6 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 6 b^6 B^2 c^4 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 36 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 180 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 720 a^3 A b^3 B c d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 204 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 6 a^4 b^2 B^2 d^6 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 4 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 720 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 156 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 1440 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 84 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 240 a^3 A b^3 B d^6 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 76 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 180 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 42 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 36 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 540 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 78 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 288 A b^6 B c d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 24 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 432 a A b^5 B d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 24 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 120 A b^6 B d^6 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 72 a^5 b B^2 c d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 12 a^6 B^2 d^6 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 360 a^3 b^3 B^2 c^2 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 360 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 360 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 720 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 120 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 90 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 270 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 144 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 216 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 12 A b^6 B c^6 \operatorname{Log}[c+d x] - 8 b^6 B^2 c^6 \operatorname{Log}[c+d x] - 72 a A b^5 B c^5 d \operatorname{Log}[c+d x] + \\
 & 60 a b^5 B^2 c^5 d \operatorname{Log}[c+d x] + 180 a^2 A b^4 B c^4 d^2 \operatorname{Log}[c+d x] - 186 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}[c+d x] - \\
 & 240 a^3 A b^3 B c^3 d^3 \operatorname{Log}[c+d x] + 128 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[c+d x] + 6 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[c+d x] - \\
 & 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\
 & 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\
 & 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 12 b^3 B^2 c^3 (b^3 c^3 - 6 a b^2 c^2 d + 15 a^2 b c d^2 - 20 a^3 d^3) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] -
 \end{aligned}$$

$$12 a^4 B^2 d^4 (15 b^2 c^2 - 6 a b c d + a^2 d^2) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]$$

**Problem 65: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^2 (c i + d i x)^2 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 dx$$

Optimal (type 4, 761 leaves, 15 steps):

$$\begin{aligned} & - \frac{B^2 (b c - a d)^4 g^2 i^2 x}{10 b^2 d^2} - \frac{B^2 (b c - a d)^3 g^2 i^2 (c + d x)^2}{20 b d^3} + \frac{B^2 (b c - a d)^2 g^2 i^2 (c + d x)^3}{30 d^3} + \\ & \frac{B^2 (b c - a d)^5 g^2 i^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{30 b^3 d^3} - \frac{B (b c - a d)^3 g^2 i^2 (a + b x)^2 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{30 b^3 d} - \\ & \frac{B (b c - a d)^2 g^2 i^2 (a + b x)^3 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{15 b^3} - \\ & \frac{B (b c - a d)^3 g^2 i^2 (c + d x)^2 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{5 b d^3} + \\ & \frac{4 B (b c - a d)^2 g^2 i^2 (c + d x)^3 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{15 d^3} - \\ & \frac{b B (b c - a d) g^2 i^2 (c + d x)^4 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{10 d^3} + \\ & \frac{(b c - a d)^2 g^2 i^2 (a + b x)^3 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{30 b^3} + \\ & \frac{(b c - a d) g^2 i^2 (a + b x)^3 (c + d x) \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{10 b^2} + \\ & \frac{g^2 i^2 (a + b x)^3 (c + d x)^2 \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{5 b} + \\ & \frac{B (b c - a d)^4 g^2 i^2 (a + b x) \left( 2 A + B + 2 B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{30 b^3 d^2} + \\ & \frac{B (b c - a d)^5 g^2 i^2 \text{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left( 2 A + 3 B + 2 B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)}{30 b^3 d^3} + \\ & \frac{B^2 (b c - a d)^5 g^2 i^2 \text{Log}[c + d x]}{10 b^3 d^3} + \frac{B^2 (b c - a d)^5 g^2 i^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{15 b^3 d^3} \end{aligned}$$

Result (type 4, 3042 leaves):

$$\frac{1}{60 b^3 d^3} g^2 i^2 \left( 4 b^5 B^2 c^5 - 24 a b^4 B^2 c^4 d + 20 a^2 b^3 B^2 c^3 d^2 + 20 a^3 b^2 B^2 c^2 d^3 - 24 a^4 b B^2 c d^4 + 4 a^5 B^2 d^5 + 4 A b^5 B \right)$$

$$\begin{aligned}
 & c^4 d x - 4 b^5 B^2 c^4 d x - 20 a A b^4 B c^3 d^2 x + 22 a b^4 B^2 c^3 d^2 x + 60 a^2 A^2 b^3 c^2 d^3 x - 36 a^2 b^3 B^2 c^2 d^3 x + \\
 & 20 a^3 A b^2 B c d^4 x + 22 a^3 b^2 B^2 c d^4 x - 4 a^4 A b B d^5 x - 4 a^4 b B^2 d^5 x - 2 A b^5 B c^3 d^2 x^2 + \\
 & 3 b^5 B^2 c^3 d^2 x^2 + 60 a A^2 b^4 c^2 d^3 x^2 - 30 a A b^4 B c^2 d^3 x^2 - 3 a b^4 B^2 c^2 d^3 x^2 + 60 a^2 A^2 b^3 c d^4 x^2 + \\
 & 30 a^2 A b^3 B c d^4 x^2 - 3 a^2 b^3 B^2 c d^4 x^2 + 2 a^3 A b^2 B d^5 x^2 + 3 a^3 b^2 B^2 d^5 x^2 + 20 A^2 b^5 c^2 d^3 x^3 - \\
 & 12 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 80 a A^2 b^4 c d^4 x^3 - 4 a b^4 B^2 c d^4 x^3 + 20 a^2 A^2 b^3 d^5 x^3 + \\
 & 12 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 30 A^2 b^5 c d^4 x^4 - 6 A b^5 B c d^4 x^4 + 30 a A^2 b^4 d^5 x^4 + 6 a A b^4 B d^5 x^4 + \\
 & 12 A^2 b^5 d^5 x^5 + 4 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b} + x\right] - 20 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] - \\
 & 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] + 20 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 10 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
 & 2 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right] + 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
 & 20 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 4 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
 & 10 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 20 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a + b x] + \\
 & 40 a^3 A b^2 B c^2 d^3 \operatorname{Log}[a + b x] + 18 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a + b x] - 20 a^4 A b B c d^4 \operatorname{Log}[a + b x] - \\
 & 24 a^4 b B^2 c d^4 \operatorname{Log}[a + b x] + 4 a^5 A B d^5 \operatorname{Log}[a + b x] + 4 a^5 B^2 d^5 \operatorname{Log}[a + b x] - \\
 & 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \\
 & 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
 & 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
 & 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 20 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
 & 4 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 4 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
 & 20 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 120 a^2 A b^3 B c^2 d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
 & 20 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 4 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
 & 2 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 120 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
 & 30 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 120 a^2 A b^3 B c d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
 & 30 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
 & 40 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 12 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
 & 160 a A b^4 B c d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 40 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \\
 & 12 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 60 A b^5 B c d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \\
 & 6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 60 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] +
 \end{aligned}$$

$$\begin{aligned}
 & 6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 40 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 20 a^4 b B^2 c d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 4 a^5 B^2 d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 60 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 60 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 60 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 20 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 80 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 20 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 30 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 30 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - 4 A b^5 B c^5 \operatorname{Log}[c+d x] + \\
 & 4 b^5 B^2 c^5 \operatorname{Log}[c+d x] + 20 A a b^4 B c^4 d \operatorname{Log}[c+d x] - 24 a b^4 B^2 c^4 d \operatorname{Log}[c+d x] - \\
 & 40 a^2 A b^3 B c^3 d^2 \operatorname{Log}[c+d x] + 18 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+d x] + 2 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+d x] + \\
 & 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - \\
 & 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 4 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 20 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 40 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 4 b^3 B^2 c^3 \left(b^2 c^2 - 5 a b c d + 10 a^2 d^2\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\
 & 4 a^3 B^2 d^3 \left(10 b^2 c^2 - 5 a b c d + a^2 d^2\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 66: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x) (c i + d i x)^2 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 dx$$

Optimal (type 4, 589 leaves, 14 steps):

$$\begin{aligned}
 & \frac{B^2 (b c - a d)^3 g i^2 x}{12 b^2 d} + \frac{B^2 (b c - a d)^2 g i^2 (c + d x)^2}{12 b d^2} - \\
 & \frac{B^2 (b c - a d)^4 g i^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{12 b^3 d^2} - \frac{B (b c - a d)^3 g i^2 (a + b x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{6 b^3 d} - \\
 & \frac{B (b c - a d)^2 g i^2 (a + b x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{6 b^3} + \frac{B (b c - a d)^2 g i^2 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{4 b d^2} - \\
 & \frac{B (b c - a d) g i^2 (c + d x)^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{6 d^2} + \frac{(b c - a d)^2 g i^2 (a + b x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{12 b^3} + \\
 & \frac{(b c - a d) g i^2 (a + b x)^2 (c + d x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{6 b^2} + \\
 & \frac{g i^2 (a + b x)^2 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{4 b} - \\
 & \frac{B (b c - a d)^4 g i^2 \text{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{6 b^3 d^2} - \\
 & \frac{B^2 (b c - a d)^4 g i^2 \text{Log}[c + d x]}{4 b^3 d^2} - \frac{B^2 (b c - a d)^4 g i^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{6 b^3 d^2}
 \end{aligned}$$

Result (type 4, 2268 leaves):

$$\begin{aligned}
 & \frac{1}{12 b^3 d^2} g i^2 \\
 & \left( -2 b^4 B^2 c^4 - 2 a b^3 B^2 c^3 d + 12 a^2 b^2 B^2 c^2 d^2 - 10 a^3 b B^2 c d^3 + 2 a^4 B^2 d^4 - 2 A b^4 B c^3 d x + 3 b^4 B^2 c^3 d x + \right. \\
 & 12 a A^2 b^3 c^2 d^2 x - 4 a A b^3 B c^2 d^2 x - 7 a b^3 B^2 c^2 d^2 x + 8 a^2 A b^2 B c d^3 x + 5 a^2 b^2 B^2 c d^3 x - \\
 & 2 a^3 A b B d^4 x - a^3 b B^2 d^4 x + 6 A^2 b^4 c^2 d^2 x^2 - 5 A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 + 12 a A^2 b^3 c d^3 x^2 + \\
 & 4 a A b^3 B c d^3 x^2 - 2 a b^3 B^2 c d^3 x^2 + a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + 8 A^2 b^4 c d^3 x^3 - \\
 & 2 A b^4 B c d^3 x^3 + 4 a A^2 b^3 d^4 x^3 + 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 - 2 a b^3 B^2 c^3 d \text{Log}\left[\frac{a}{b} + x\right] - \\
 & 4 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{a}{b} + x\right] + 8 a^3 b B^2 c d^3 \text{Log}\left[\frac{a}{b} + x\right] - 2 a^4 B^2 d^4 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 6 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 4 a^3 b B^2 c d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 + a^4 B^2 d^4 \text{Log}\left[\frac{a}{b} + x\right]^2 + \\
 & 2 b^4 B^2 c^4 \text{Log}\left[\frac{c}{d} + x\right] + 4 a b^3 B^2 c^3 d \text{Log}\left[\frac{c}{d} + x\right] - 8 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 2 a^3 b B^2 c d^3 \text{Log}\left[\frac{c}{d} + x\right] - b^4 B^2 c^4 \text{Log}\left[\frac{c}{d} + x\right]^2 + 4 a b^3 B^2 c^3 d \text{Log}\left[\frac{c}{d} + x\right]^2 + \\
 & 12 a^2 A b^2 B c^2 d^2 \text{Log}[a + b x] + 5 a^2 b^2 B^2 c^2 d^2 \text{Log}[a + b x] - 8 a^3 A b B c d^3 \text{Log}[a + b x] - \\
 & 6 a^3 b B^2 c d^3 \text{Log}[a + b x] + 2 a^4 A B d^4 \text{Log}[a + b x] + a^4 B^2 d^4 \text{Log}[a + b x] - \\
 & 12 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 8 a^3 b B^2 c d^3 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] - \\
 & 2 a^4 B^2 d^4 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 12 a^2 b^2 B^2 c^2 d^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 8 a^3 b B^2 c d^3 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + 2 a^4 B^2 d^4 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] -
 \end{aligned}$$

$$\begin{aligned}
& 12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+8 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]- \\
& 2 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-2 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
& 24 a A b^3 B c^2 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-4 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
& 8 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-2 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
& 12 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-5 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
& 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+4 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
& a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+16 A b^4 B c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
& 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+8 a A b^3 B d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
& 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+12 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
& 8 a^3 b B^2 c d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+2 a^4 B^2 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
& 12 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+6 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
& 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+8 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
& 4 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2+ \\
& 2 A b^4 B c^4 \operatorname{Log}[c+d x]-3 b^4 B^2 c^4 \operatorname{Log}[c+d x]-8 a A b^3 B c^3 d \operatorname{Log}[c+d x]+ \\
& 2 a b^3 B^2 c^3 d \operatorname{Log}[c+d x]+a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c+d x]-2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
& 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
& 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]- \\
& 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+2 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
& 8 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+2 b^3 B^2 c^3(b c-4 a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]- \\
& 2 a^2 B^2 d^2\left(6 b^2 c^2-4 a b c d+a^2 d^2\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
\end{aligned}$$

Problem 67: Result more than twice size of optimal antiderivative.



$$\int (c i + d i x)^2 \left( A + B \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 334 leaves, 11 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^2 i^2 x}{3 b^2} + \frac{B^2 (b c - a d)^3 i^2 \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right]}{3 b^3 d} - \\ & \frac{2 B (b c - a d)^2 i^2 (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{3 b^3} - \frac{B (b c - a d) i^2 (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{3 b d} + \\ & \frac{i^2 (c + d x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2}{3 d} + \frac{B^2 (b c - a d)^3 i^2 \operatorname{Log} [c + d x]}{b^3 d} + \\ & \frac{2 B (b c - a d)^3 i^2 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right) \operatorname{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{3 b^3 d} - \frac{2 B^2 (b c - a d)^3 i^2 \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{3 b^3 d} \end{aligned}$$

Result (type 4, 1278 leaves):

$$\begin{aligned}
& \frac{1}{6 b^3 d} i^2 \left( 6 A^2 b^3 c^2 d x + 6 A^2 b^3 c d^2 x^2 + 2 A^2 b^3 d^3 x^3 + \right. \\
& 2 A b B d (b c - a d) x (2 b c + 2 a d - b d x) + 12 b B^2 c d (-b c + a d) (a + b x) \left( -1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - \\
& 4 B^2 d (-b c + a d) (b c + a d) (a + b x) \left( -1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - 6 a^2 b B^2 c d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 2 a^3 B^2 d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 + 12 b^2 B^2 c (b c - a d) (c + d x) \left( -1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - \\
& 4 b B^2 (b c - a d) (b c + a d) (c + d x) \left( -1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - \\
& 4 b^3 B^2 c^3 \text{Log}\left[\frac{c}{d} + x\right]^2 - 12 a^2 A b B c d^2 \text{Log}[a + b x] + 4 a^3 A B d^3 \text{Log}[a + b x] + \\
& B^2 d^2 (-b c + a d) \left( b x (2 a - b x) + 2 b^2 x^2 \text{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \text{Log}[a + b x] \right) + \\
& 4 A b^3 B d^3 x^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 6 b^3 B^2 c d^2 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 b^3 B^2 d^3 x^3 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 - \\
& 4 A b^3 B c^3 \text{Log}[c + d x] + 12 A b^2 B c^2 \left( a d \text{Log}[a + b x] + b d x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] - b c \text{Log}[c + d x] \right) - \\
& b^2 B^2 (b c - a d) \left( d x (-2 c + d x) - 2 d^2 x^2 \text{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \text{Log}[c + d x] \right) + \\
& 12 A b^2 B c \left( d (-b c + a d) x + b d^2 x^2 \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + b c^2 \text{Log}[c + d x] \right) + \\
& 2 B^2 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \\
& (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log}[a + b x] + 2 b^3 c^3 \text{Log}[c + d x]) + \\
& 12 b B^2 c \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \right) \\
& (a^2 d^2 \text{Log}[a + b x] - b (d (-b c + a d) x + b c^2 \text{Log}[c + d x])) + \\
& 8 b^3 B^2 c^3 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) + \\
& 12 a^2 b B^2 c d^2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) - \\
& 4 a^3 B^2 d^3 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) + \\
& 6 b^2 B^2 c^2 \left( a d \text{Log}\left[\frac{a}{b} + x\right]^2 + b c \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 a d \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \right. \\
& 2 a d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 2 a d \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
& 2 a d \text{Log}[a + b x] \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] + b d x \text{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 b c \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] - \\
& 2 b c \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] - 2 b c \text{Log}\left[\frac{e(a + b x)}{c + d x}\right] \text{Log}[c + d x] - 2 b c \text{Log}\left[\frac{a}{b} + x\right] \\
& \left. \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - 2 b c \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] - 2 a d \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \Big)
\end{aligned}$$

### Problem 68: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 535 leaves, 15 steps):

$$\begin{aligned} & - \frac{B d (b c - a d) i^2 (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{b^3 g} + \\ & \frac{2 B (b c - a d)^2 i^2 \operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right] \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{b^3 g} + \\ & \frac{d (b c - a d) i^2 (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{b^3 g} + \frac{i^2 (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{2 b g} + \\ & \frac{B^2 (b c - a d)^2 i^2 \operatorname{Log} [c + d x]}{b^3 g} + \frac{B (b c - a d)^2 i^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} - \\ & \frac{(b c - a d)^2 i^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2 \operatorname{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} + \\ & \frac{2 B^2 (b c - a d)^2 i^2 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^3 g} - \frac{B^2 (b c - a d)^2 i^2 \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} + \\ & \frac{2 B (b c - a d)^2 i^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} + \\ & \frac{2 B^2 (b c - a d)^2 i^2 \operatorname{PolyLog} \left[ 3, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} \end{aligned}$$

Result (type 4, 2547 leaves):

$$\begin{aligned} & \frac{1}{12 b^3 g} i^2 \left( 12 A^2 b d (2 b c - a d) x + 6 A^2 b^2 d^2 x^2 + 12 A^2 (b c - a d)^2 \operatorname{Log} [a + b x] - \right. \\ & 24 A b B c \left( a d \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 - 2 a d \operatorname{Log} \left[ \frac{a}{b} + x \right] (1 + \operatorname{Log} [a + b x]) + \right. \\ & 2 \left( -b c + a d + \operatorname{Log} \left[ \frac{c}{d} + x \right] \left( b c + a d \operatorname{Log} [a + b x] - a d \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] \right) + \right. \\ & \left. \left. (-b d x + a d \operatorname{Log} [a + b x]) \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] - 2 a d \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) + \right. \\ & \left. 12 A b^2 B c^2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 - 2 \operatorname{Log} [a + b x] \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right) - \right. \\ & \left. \left. 2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right) + \end{aligned}$$

$$\begin{aligned}
 & 6 A B \left( -4 a d^2 (a+b x) \left( -1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 a b d (c+d x) \right. \\
 & \quad \left. \left( -1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + d^2 \left( b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a+b x] \right) - \right. \\
 & \quad 2 d^2 \left( b x (-2 a + b x) + 2 a^2 \operatorname{Log}[a+b x] \right) \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) + \\
 & \quad b^2 \left( d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c+d x] \right) - \\
 & \quad \left. 4 a^2 d^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) - \\
 & 8 b B^2 c \left( a d \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 3 d (a+b x) \left( 2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \right. \\
 & \quad 3 b (c+d x) \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - \\
 & \quad \left. 3 d (b x - a \operatorname{Log}[a+b x]) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 + \right. \\
 & \quad 6 \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c+d x] + \right. \\
 & \quad \quad \operatorname{Log}\left[\frac{a}{b} + x\right] \left( -d (a+b x) + d (a+b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + \\
 & \quad \quad (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \left. - 3 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \right. \\
 & \quad \quad \left. \left( -2 b c + 2 a d - 2 d (a+b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \\
 & \quad \quad \left. \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \left( b (c+d x) - a d \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] \right) - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) - \right. \\
 & \quad \left. 3 a d \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + \right. \right. \\
 & \quad \quad 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \left. \right) + 3 a d \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \right. \\
 & \quad \quad \left. \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \right) + \\
 & B^2 \left( 4 a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 12 a d^2 (a+b x) \left( 2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \right. \\
 & \quad 3 d^2 (a+b x) \left( 7 a - b x + (-6 a + 2 b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 (a - b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \\
 & \quad 12 a b d (c+d x) \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - \\
 & \quad 3 b^2 (c+d x) \left( 7 c - d x + (-6 c + 2 d x) \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 (c - d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) + \\
 & \quad \left. 6 d^2 (b x (-2 a + b x) + 2 a^2 \operatorname{Log}[a+b x]) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{e(a+bx)}{c+dx} \right] \right) \\
 & \left( -4 a d^2 (a+bx) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right) + 2 a^2 d^2 \text{Log} \left[ \frac{a}{b} + x \right]^2 + 4 a b d (c+dx) \right. \\
 & \quad \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right) + d^2 (bx(2a-bx) + 2 b^2 x^2 \text{Log} \left[ \frac{a}{b} + x \right] - 2 a^2 \text{Log} [a+bx]) + \\
 & \quad b^2 (dx(-2c+dx) - 2 d^2 x^2 \text{Log} \left[ \frac{c}{d} + x \right] + 2 c^2 \text{Log} [c+dx]) - \\
 & \quad \left. 4 a^2 d^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) + \\
 & 6 \left( 2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - 2 a b d^2 x \text{Log} \left[ \frac{c}{d} + x \right] + b^2 d^2 x^2 \text{Log} \left[ \frac{c}{d} + x \right] - \right. \\
 & \quad a^2 d^2 \text{Log} [a+bx] - b^2 c^2 \text{Log} [c+dx] - 2 a b c d \text{Log} [c+dx] - \\
 & \quad \text{Log} \left[ \frac{a}{b} + x \right] \left( b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \text{Log} \left[ \frac{c}{d} + x \right] + \right. \\
 & \quad \left. (-2 b^2 c^2 + 2 a^2 d^2) \text{Log} \left[ \frac{b(c+dx)}{bc-ad} \right] \right) + 2 (b^2 c^2 - a^2 d^2) \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] + \\
 & \quad 4 a d \left( a d + 2 b d x - b d x \text{Log} \left[ \frac{c}{d} + x \right] - b c \text{Log} [c+dx] + \text{Log} \left[ \frac{a}{b} + x \right] \right. \\
 & \quad \left. \left( -d(a+bx) + d(a+bx) \text{Log} \left[ \frac{c}{d} + x \right] + (bc-ad) \text{Log} \left[ \frac{b(c+dx)}{bc-ad} \right] \right) + (bc-ad) \right. \\
 & \quad \left. \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right) - 2 a^2 d^2 \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{b(c+dx)}{bc-ad} \right] \right) - \right. \\
 & \quad \left. 2 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] + 2 \text{PolyLog} \left[ 3, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
 & \quad 12 a^2 d^2 \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] - \right. \\
 & \quad \left. 2 \text{PolyLog} \left[ 3, \frac{b(c+dx)}{bc-ad} \right] \right) + \\
 & 4 b^2 B^2 c^2 \left( \text{Log} \left[ \frac{a}{b} + x \right]^3 + 3 \text{Log} \left[ \frac{c}{d} + x \right]^2 \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + 3 \text{Log} [a+bx] \right. \\
 & \quad \left. \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{e(a+bx)}{c+dx} \right] \right)^2 + \right. \\
 & \quad 3 \text{Log} \left[ \frac{a}{b} + x \right]^2 \left( -\text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{b(c+dx)}{bc-ad} \right] \right) + 6 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] + \\
 & \quad 6 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] - 3 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{e(a+bx)}{c+dx} \right] \right) \\
 & \quad \left. \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 - 2 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] \right) \right) \right) -
 \end{aligned}$$

$$6 \text{ PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \text{ PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \Bigg)$$

**Problem 69: Result more than twice size of optimal antiderivative.**

$$\int \frac{(cix+dx)^2 (A+B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])^2}{(ag+bgx)^2} dx$$

Optimal (type 4, 442 leaves, 11 steps):

$$\begin{aligned} & -\frac{2B^2(bc-ad)i^2(c+dx)}{b^2g^2(a+bx)} - \frac{2B(bc-ad)i^2(c+dx)(A+B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])}{b^2g^2(a+bx)} + \\ & \frac{2Bd(bc-ad)i^2 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right](A+B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])}{b^3g^2} + \\ & \frac{d^2i^2(a+bx)(A+B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])^2}{b^3g^2} - \frac{(bc-ad)i^2(c+dx)(A+B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])^2}{b^2g^2(a+bx)} - \\ & \frac{2d(bc-ad)i^2(A+B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right])^2 \text{Log}\left[1-\frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2} + \frac{2B^2d(bc-ad)i^2 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{b^3g^2} + \\ & \frac{4Bd(bc-ad)i^2(A+B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]) \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2} + \\ & \frac{4B^2d(bc-ad)i^2 \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b^3g^2} \end{aligned}$$

Result (type 4, 2775 leaves):

$$\begin{aligned} & \frac{A^2d^2i^2x}{b^2g^2} + \frac{-A^2b^2c^2i^2+2aA^2bcdi^2-a^2A^2d^2i^2}{b^3g^2(a+bx)} - \frac{2(-A^2bcdi^2+aA^2d^2i^2)\text{Log}[a+bx]}{b^3g^2} + \\ & \left( B^2c^2i^2 \left( -2bc+2ad-2d(a+bx)\text{Log}[a+bx] + (-2bc+2ad)\text{Log}\left[\frac{e(a+bx)}{c+dx}\right] - \right. \right. \\ & \left. \left. b(c+dx)\text{Log}\left[\frac{e(a+bx)}{c+dx}\right]^2 + 2d(a+bx)\text{Log}[c+dx] \right) \right) / (b(bc-ad)g^2(a+bx)) + \\ & \frac{1}{g^2} 2ABc^2i^2 \left( -\frac{\left(\frac{a}{b}+x\right)\left(\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{a}{b}+x\right]^2\right)}{(a+bx)^2\text{Log}\left[\frac{a}{b}+x\right]} - \frac{\frac{b\left(\frac{c}{d}+x\right)\text{Log}\left[\frac{c}{d}+x\right]}{\left(-a+\frac{bc}{d}\right)^2\left(1-\frac{b\left(\frac{c}{d}+x\right)}{-a+\frac{bc}{d}}\right)}+\frac{\text{Log}\left[1-\frac{b\left(\frac{c}{d}+x\right)}{-a+\frac{bc}{d}}\right]}{-a+\frac{bc}{d}}}{b} - \right. \end{aligned}$$

$$\left. \frac{-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]}{b(a+b x)}\right\}+\frac{1}{g^2} 2 A B d^2 i^2$$

$$\left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2}-\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b^3}-\frac{a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3(a+b x)}-\frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b^2}-\right.$$

$$\left.\left(a^2\left(\left(-b c+a d\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right) / \left(b^3(b c-a d)(a+b x)\right)+\frac{1}{b^3}$$

$$\left(b x-\frac{a^2}{a+b x}-2 a \operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)+$$

$$\left.\frac{2 a\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2,\frac{b(c+d x)}{b c-a d}\right]\right)}{b^3}\right\}+$$

$$\frac{1}{g^2} 4 A B c d i^2\left(\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^2}+\frac{a\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2(a+b x)}+\right.$$

$$\left.\left(a\left(\left(-b c+a d\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right) / \left(b^2(b c-a d)(a+b x)\right)+\frac{1}{b^2}$$

$$\left(\frac{a}{a+b x}+\operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)-$$

$$\left.\frac{\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2,\frac{b(c+d x)}{b c-a d}\right]}{b^2}\right\}+$$

$$\frac{1}{g^2} B^2 d^2 i^2\left(-\frac{2 a \operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^3}+\frac{(a+b x)\left(2-2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3}-\right.$$

$$\frac{a^2\left(2+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3(a+b x)}+\frac{(c+d x)\left(2-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{b^2 d}+\frac{1}{b^3}$$

$$\left(b x-\frac{a^2}{a+b x}-2 a \operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)^2+$$

$$\left(a^2\left(-b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 d(a+b x) \operatorname{PolyLog}\left[2,\frac{b(c+d x)}{b c-a d}\right]\right)\right) / \left(b^3(b c-a d)(a+b x)\right)+$$

$$\begin{aligned}
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) \left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} - \right. \\
 & \quad \frac{a \text{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a+b x)} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} - \\
 & \quad \left. \left( a^2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a+b x) \left(\text{Log}[a+b x] - \text{Log}[c+d x]\right) \right) \right) / \right. \\
 & \quad \left. \left( b^3 (b c - a d) (a+b x) \right) + \frac{2 a \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right)}{b^3} \right) - \\
 & 2 \left( \frac{1}{b^3 d} \left( a d + 2 b d x - b d x \text{Log}\left[\frac{c}{d} + x\right] - b c \text{Log}[c+d x] + \text{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
 & \quad \left. \left( -d (a+b x) + d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + (b c - a d) \right. \\
 & \quad \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \left. \right) + \left( a^2 \left( d (a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \right. \\
 & \quad \left. \left. d (a+b x) \left(\text{Log}[a+b x] - \text{Log}[c+d x]\right) \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \quad \left. \left. d (a+b x) \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - 2 d (a+b x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) / \right. \\
 & \quad \left. \left( 2 b^3 (b c - a d) (a+b x) \right) - \frac{1}{b^3} a \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \left( \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - \right. \right. \\
 & \quad \left. \left. 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) - \\
 & \quad \frac{1}{b^3} 2 a \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - \right. \\
 & \quad \left. \left. 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right) + \\
 & \frac{1}{g^2} 2 B^2 c d i^2 \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^3}{3 b^2} + \frac{a \left( 2 + 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^2 (a+b x)} + \frac{1}{b^2} \right. \\
 & \quad \left. \left( \frac{a}{a+b x} + \text{Log}[a+b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right)^2 - \right. \\
 & \quad \left( a \left( -b (c+d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 d (a+b x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) / \left( b^2 (b c - a d) (a+b x) \right) + \\
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} + \frac{a \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right)}{b^2 (a+b x)} \right) +
 \end{aligned}$$



$$\begin{aligned}
 & \left( a \left( (-b c + a d) \operatorname{Log} \left[ \frac{c}{d} + x \right] + d (a + b x) (\operatorname{Log} [a + b x] - \operatorname{Log} [c + d x]) \right) \right) / \\
 & \left( b^2 (b c - a d) (a + b x) \right) - \frac{\operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right]}{b^2} \Bigg) - \\
 & 2 \left( - \left( \left( a \left( d (a + b x) \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 + 2 \left( (-b c + a d) \operatorname{Log} \left[ \frac{c}{d} + x \right] + d (a + b x) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. (\operatorname{Log} [a + b x] - \operatorname{Log} [c + d x]) \right) \right) - 2 \operatorname{Log} \left[ \frac{a}{b} + x \right] \left( (b c - a d) \operatorname{Log} \left[ \frac{c}{d} + x \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. d (a + b x) \operatorname{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] \right) - 2 d (a + b x) \operatorname{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) / \\
 & \left( 2 b^2 (b c - a d) (a + b x) \right) + \frac{1}{2 b^2} \left( \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] \right) - \right. \\
 & \left. 2 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] + 2 \operatorname{PolyLog} \left[ 3, \frac{d (a + b x)}{-b c + a d} \right] \right) + \\
 & \frac{1}{b^2} \left( \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] - \right. \\
 & \left. 2 \operatorname{PolyLog} \left[ 3, \frac{b (c + d x)}{b c - a d} \right] \right) \Bigg)
 \end{aligned}$$

### Problem 70: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 (A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right])^2}{(a g + b g x)^3} dx$$

Optimal (type 4, 387 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{2 B^2 d i^2 (c + d x)}{b^2 g^3 (a + b x)} - \frac{B^2 i^2 (c + d x)^2}{4 b g^3 (a + b x)^2} - \frac{2 B d i^2 (c + d x) (A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right])}{b^2 g^3 (a + b x)} - \\
 & \frac{B i^2 (c + d x)^2 (A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right])}{2 b g^3 (a + b x)^2} - \frac{d i^2 (c + d x) (A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right])^2}{b^2 g^3 (a + b x)} - \\
 & \frac{i^2 (c + d x)^2 (A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right])^2}{2 b g^3 (a + b x)^2} - \frac{d^2 i^2 (A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right])^2 \operatorname{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g^3} + \\
 & \frac{2 B d^2 i^2 (A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right]) \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g^3} + \frac{2 B^2 d^2 i^2 \operatorname{PolyLog} \left[ 3, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g^3}
 \end{aligned}$$

Result (type 4, 3601 leaves):

$$- \frac{A^2 (b^2 c^2 - 2 a b c d + a^2 d^2) i^2}{2 b^3 g^3 (a + b x)^2} + \frac{2 (-A^2 b c d i^2 + a A^2 d^2 i^2)}{b^3 g^3 (a + b x)} + \frac{A^2 d^2 i^2 \operatorname{Log} [a + b x]}{b^3 g^3} -$$

$$\begin{aligned}
 & \left( B^2 c^2 i^2 \left( b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a + b x)^2 \log[a + b x] + \right. \right. \\
 & \quad \left. \left. 2 (b c - a d) (b c - 3 a d - 2 b d x) \log\left[\frac{e (a + b x)}{c + d x}\right] + 2 b (c + d x) (b c - 2 a d - b d x) \right. \right. \\
 & \quad \left. \left. \log\left[\frac{e (a + b x)}{c + d x}\right]^2 + 6 a^2 d^2 \log[c + d x] + 12 a b d^2 x \log[c + d x] + 6 b^2 d^2 x^2 \log[c + d x] \right) \right) / \\
 & \left( 4 b (b c - a d)^2 g^3 (a + b x)^2 \right) + \frac{1}{g^3} 2 A B c^2 i^2 \left( - \frac{\left(\frac{a}{b} + x\right) \left(2 \log\left[\frac{a}{b} + x\right] + 4 \log\left[\frac{a}{b} + x\right]^2\right)}{8 (a + b x)^3 \log\left[\frac{a}{b} + x\right]} - \frac{1}{2 b} \right. \\
 & \left. \left( \frac{b \left(\frac{c}{d} + x\right)}{\left(-a + \frac{b c}{d}\right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right)} - \left( \frac{b^2 \left(\frac{c}{d} + x\right)^2}{\left(-a + \frac{b c}{d}\right)^4 \left(1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right)^2} + \frac{2 b \left(\frac{c}{d} + x\right)}{\left(-a + \frac{b c}{d}\right)^3 \left(1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right)} \right) \log\left[\frac{c}{d} + x\right] - \right. \\
 & \quad \left. \frac{\log\left[1 - \frac{b \left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right]}{\left(-a + \frac{b c}{d}\right)^2} \right) - \frac{-\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]}{2 b (a + b x)^2} \right) + \\
 & \frac{1}{g^3} 4 A B c d i^2 \left( - \frac{1 + \log\left[\frac{a}{b} + x\right]}{b^2 (a + b x)} + \frac{a \left(1 + 2 \log\left[\frac{a}{b} + x\right]\right)}{4 b^2 (a + b x)^2} - \right. \\
 & \quad \frac{(-b c + a d) \log\left[\frac{c}{d} + x\right] + d (a + b x) (\log[a + b x] - \log[c + d x])}{b^2 (b c - a d) (a + b x)} - \\
 & \quad \frac{a \left(\log\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \log[a + b x] - d (a + b x) \log[c + d x])}{(b c - a d)^2}\right)}{2 b^2 (a + b x)^2} - \\
 & \quad \left. \frac{(a + 2 b x) \left(-\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)}{2 b^2 (a + b x)^2} \right) + \\
 & \frac{1}{g^3} 2 A B d^2 i^2 \left( \frac{\log\left[\frac{a}{b} + x\right]^2}{2 b^3} + \frac{2 a \left(1 + \log\left[\frac{a}{b} + x\right]\right)}{b^3 (a + b x)} - \frac{a^2 \left(1 + 2 \log\left[\frac{a}{b} + x\right]\right)}{4 b^3 (a + b x)^2} + \right. \\
 & \quad \left( 2 a \left( (-b c + a d) \log\left[\frac{c}{d} + x\right] + d (a + b x) (\log[a + b x] - \log[c + d x]) \right) \right) / \\
 & \quad \left( b^3 (b c - a d) (a + b x) \right) + \frac{a^2 \left(\log\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \log[a + b x] - d (a + b x) \log[c + d x])}{(b c - a d)^2}\right)}{2 b^3 (a + b x)^2} + \\
 & \quad \left. \frac{1}{2 b^3} \left( \frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \log[a + b x] \right) \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\log\left[\frac{c}{d} + x\right] \log\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]}{b^3}\right) + \\
 & \frac{1}{g^3} 2 B^2 c d i^2 \left( -\frac{2 + 2 \log\left[\frac{a}{b} + x\right] + \log\left[\frac{a}{b} + x\right]^2}{b^2 (a+bx)} + \frac{a \left(1 + 2 \log\left[\frac{a}{b} + x\right] + 2 \log\left[\frac{a}{b} + x\right]^2\right)}{4 b^2 (a+bx)^2} + \right. \\
 & 2 \left( -\frac{1 + \log\left[\frac{a}{b} + x\right]}{b^2 (a+bx)} + \frac{a \left(1 + 2 \log\left[\frac{a}{b} + x\right]\right)}{4 b^2 (a+bx)^2} - \left( (-bc+ad) \log\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \quad \left. \left. d (a+bx) (\log[a+bx] - \log[c+dx]) \right) \right) / (b^2 (bc-ad) (a+bx)) - \\
 & \left. \frac{a \left( \log\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\log[a+bx]-d(a+bx)\log[c+dx])}{(bc-ad)^2} \right)}{2 b^2 (a+bx)^2} \right) \\
 & \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) - \\
 & \frac{(a+2bx) \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)^2}{2 b^2 (a+bx)^2} - \\
 & 2 \left( \left( d (a+bx) \log\left[\frac{a}{b} + x\right]^2 + 2 \left( (-bc+ad) \log\left[\frac{c}{d} + x\right] + d (a+bx) (\log[a+bx] - \log[c+ \right. \right. \right. \\
 & \quad \left. \left. \left. dx]) \right) \right) - 2 \log\left[\frac{a}{b} + x\right] \left( (bc-ad) \log\left[\frac{c}{d} + x\right] + d (a+bx) \log\left[\frac{b(c+dx)}{bc-ad}\right] \right) \right) - \\
 & \quad 2 d (a+bx) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) / (2 b^2 (bc-ad) (a+bx)) + \\
 & \left( a \left( -d (-bc+ad) (a+bx) + (bc-ad)^2 \left( 1 + 2 \log\left[\frac{a}{b} + x\right] \right) \log\left[\frac{c}{d} + x\right] + d^2 (a+bx)^2 \right. \right. \\
 & \quad \left. \left. \log[a+bx] - d^2 (a+bx)^2 \log[c+dx] + d (a+bx) \left( d (a+bx) \log\left[\frac{a}{b} + x\right]^2 + \right. \right. \right. \\
 & \quad \left. \left. \left. 2 (bc-ad) \left( 1 + \log\left[\frac{a}{b} + x\right] \right) - 2 d (a+bx) \left( \log\left[\frac{a}{b} + x\right] \log\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) \right) / (4 b^2 (bc-ad)^2 (a+bx)^2) \right) + \\
 & \left( -b (c+dx) \log\left[\frac{c}{d} + x\right]^2 + 2 d (a+bx) \log\left[\frac{c}{d} + x\right] \log\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
 & \quad \left. 2 d (a+bx) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) / (b^2 (bc-ad) (a+bx)) + \\
 & \left( a \left( b (c+dx) (-2ad+b(c-dx)) \log\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a+bx)^2 \log\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \right. \\
 & \quad \left. \left. 2 d (a+bx) \log\left[\frac{c}{d} + x\right] \left( b (c+dx) + d (a+bx) \log\left[\frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) +
 \end{aligned}$$



$$\begin{aligned}
 & \left( 1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \right) \operatorname{Log}\left[\frac{c}{d} + x\right] + d^2 (a + b x)^2 \operatorname{Log}[a + b x] - d^2 (a + b x)^2 \operatorname{Log}[c + d x] + \\
 & d (a + b x) \left( d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 (b c - a d) \left( 1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - \right. \\
 & \left. 2 d (a + b x) \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \Bigg) / \\
 & \left( 4 b^3 (b c - a d)^2 (a + b x)^2 \right) + \frac{1}{2 b^3} \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - \right. \\
 & \left. 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) + \\
 & \frac{1}{b^3} \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - \right. \\
 & \left. 2 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right)
 \end{aligned}$$

**Problem 74: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^3 (c i + d i x)^3 \left( A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2 dx$$

Optimal (type 4, 1089 leaves, 22 steps):

$$\begin{aligned}
 & \frac{5 B^2 (b c - a d)^6 g^3 i^3 x}{84 b^3 d^3} + \frac{B^2 (b c - a d)^3 g^3 i^3 (a + b x)^4}{140 b^4} - \frac{29 B^2 (b c - a d)^5 g^3 i^3 (c + d x)^2}{840 b^2 d^4} + \\
 & \frac{47 B^2 (b c - a d)^4 g^3 i^3 (c + d x)^3}{1260 b d^4} - \frac{13 B^2 (b c - a d)^3 g^3 i^3 (c + d x)^4}{420 d^4} + \frac{b B^2 (b c - a d)^2 g^3 i^3 (c + d x)^5}{105 d^4} - \\
 & \frac{B^2 (b c - a d)^7 g^3 i^3 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{210 b^4 d^4} - \frac{B (b c - a d)^4 g^3 i^3 (a + b x)^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{210 b^4 d} - \\
 & \frac{3 B (b c - a d)^3 g^3 i^3 (a + b x)^4 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{140 b^4} - \\
 & \frac{B (b c - a d)^2 g^3 i^3 (a + b x)^4 (c + d x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{35 b^3} + \\
 & \frac{2 B (b c - a d)^4 g^3 i^3 (c + d x)^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{21 b d^4} - \\
 & \frac{3 B (b c - a d)^3 g^3 i^3 (c + d x)^4 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{14 d^4} + \\
 & \frac{6 b B (b c - a d)^2 g^3 i^3 (c + d x)^5 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{35 d^4} - \\
 & \frac{b^2 B (b c - a d) g^3 i^3 (c + d x)^6 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{21 d^4} + \\
 & \frac{(b c - a d)^3 g^3 i^3 (a + b x)^4 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{140 b^4} + \\
 & \frac{(b c - a d)^2 g^3 i^3 (a + b x)^4 (c + d x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{35 b^3} + \\
 & \frac{(b c - a d) g^3 i^3 (a + b x)^4 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{14 b^2} + \\
 & \frac{g^3 i^3 (a + b x)^4 (c + d x)^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{7 b} + \\
 & \frac{B (b c - a d)^5 g^3 i^3 (a + b x)^2 \left(3 A + B + 3 B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{420 b^4 d^2} - \\
 & \frac{B (b c - a d)^6 g^3 i^3 (a + b x) \left(6 A + 5 B + 6 B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{420 b^4 d^3} - \\
 & \frac{B (b c - a d)^7 g^3 i^3 \text{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(6 A + 11 B + 6 B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{420 b^4 d^4} - \\
 & \frac{11 B^2 (b c - a d)^7 g^3 i^3 \text{Log}[c + d x]}{420 b^4 d^4} - \frac{B^2 (b c - a d)^7 g^3 i^3 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{70 b^4 d^4}
 \end{aligned}$$

Result(type 4, 5123 leaves):

1

2520 b<sup>4</sup> d<sup>4</sup>

$$\begin{aligned}
 & g^3 i^3 \left( -36 b^7 B^2 c^7 + 288 a b^6 B^2 c^6 d - 1008 a^2 b^5 B^2 c^5 d^2 + 756 a^3 b^4 B^2 c^4 d^3 + 756 a^4 b^3 B^2 c^3 d^4 - 1008 a^5 \right. \\
 & \quad b^2 B^2 c^2 d^5 + 288 a^6 b B^2 c d^6 - 36 a^7 B^2 d^7 - 36 A b^7 B c^6 d x + 36 b^7 B^2 c^6 d x + 252 a A b^6 B c^5 d^2 x - \\
 & \quad 270 a b^6 B^2 c^5 d^2 x - 756 a^2 A b^5 B c^4 d^3 x + 876 a^2 b^5 B^2 c^4 d^3 x + 2520 a^3 A^2 b^4 c^3 d^4 x - \\
 & \quad 1284 a^3 b^4 B^2 c^3 d^4 x + 756 a^4 A b^3 B c^2 d^5 x + 876 a^4 b^3 B^2 c^2 d^5 x - 252 a^5 A b^2 B c d^6 x - \\
 & \quad 270 a^5 b^2 B^2 c d^6 x + 36 a^6 A b B d^7 x + 36 a^6 b B^2 d^7 x + 18 A b^7 B c^5 d^2 x^2 - 27 b^7 B^2 c^5 d^2 x^2 - \\
 & \quad 126 a A b^6 B c^4 d^3 x^2 + 201 a b^6 B^2 c^4 d^3 x^2 + 3780 a^2 A^2 b^5 c^3 d^4 x^2 - 1512 a^2 A b^5 B c^3 d^4 x^2 - \\
 & \quad 174 a^2 b^5 B^2 c^3 d^4 x^2 + 3780 a^3 A^2 b^4 c^2 d^5 x^2 + 1512 a^3 A b^4 B c^2 d^5 x^2 - 174 a^3 b^4 B^2 c^2 d^5 x^2 + \\
 & \quad 126 a^4 A b^3 B c d^6 x^2 + 201 a^4 b^3 B^2 c d^6 x^2 - 18 a^5 A b^2 B d^7 x^2 - 27 a^5 b^2 B^2 d^7 x^2 - 12 A b^7 B c^4 d^3 x^3 + \\
 & \quad 22 b^7 B^2 c^4 d^3 x^3 + 2520 a A^2 b^6 c^3 d^4 x^3 - 1176 a A b^6 B c^3 d^4 x^3 + 152 a b^6 B^2 c^3 d^4 x^3 + \\
 & \quad 7560 a^2 A^2 b^5 c^2 d^5 x^3 - 348 a^2 b^5 B^2 c^2 d^5 x^3 + 2520 a^3 A^2 b^4 c d^6 x^3 + 1176 a^3 A b^4 B c d^6 x^3 + \\
 & \quad 152 a^3 b^4 B^2 c d^6 x^3 + 12 a^4 A b^3 B d^7 x^3 + 22 a^4 b^3 B^2 d^7 x^3 + 630 A^2 b^7 c^3 d^4 x^4 - 306 A b^7 B c^3 d^4 x^4 + \\
 & \quad 60 b^7 B^2 c^3 d^4 x^4 + 5670 a A^2 b^6 c^2 d^5 x^4 - 882 a A b^6 B c^2 d^5 x^4 - 60 a b^6 B^2 c^2 d^5 x^4 + \\
 & \quad 5670 a^2 A^2 b^5 c d^6 x^4 + 882 a^2 A b^5 B c d^6 x^4 - 60 a^2 b^5 B^2 c d^6 x^4 + 630 a^3 A^2 b^4 d^7 x^4 + 306 a^3 A b^4 B d^7 x^4 + \\
 & \quad 60 a^3 b^4 B^2 d^7 x^4 + 1512 A^2 b^7 c^2 d^5 x^5 - 360 A b^7 B c^2 d^5 x^5 + 24 b^7 B^2 c^2 d^5 x^5 + 4536 a A^2 b^6 c d^6 x^5 - \\
 & \quad 48 a b^6 B^2 c d^6 x^5 + 1512 a^2 A^2 b^5 d^7 x^5 + 360 a^2 A b^5 B d^7 x^5 + 24 a^2 b^5 B^2 d^7 x^5 + 1260 A^2 b^7 c d^6 x^6 - \\
 & \quad 120 A b^7 B c d^6 x^6 + 1260 a A^2 b^6 d^7 x^6 + 120 a A b^6 B d^7 x^6 + 360 A^2 b^7 d^7 x^7 - 36 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
 & \quad 252 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 756 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] - \\
 & \quad 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{a}{b} + x\right] + 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{a}{b} + x\right] + 630 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & \quad 378 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 126 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 18 a^7 B^2 d^7 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
 & \quad 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{c}{d} + x\right] - 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{c}{d} + x\right] + 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
 & \quad 756 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] + 252 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] - 36 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
 & \quad 18 b^7 B^2 c^7 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 126 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 378 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\
 & \quad 630 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 18 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}[a + b x] + 114 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}[a + b x] + \\
 & \quad 1260 a^4 A b^3 B c^3 d^4 \operatorname{Log}[a + b x] + 642 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}[a + b x] - 756 a^5 A b^2 B c^2 d^5 \operatorname{Log}[a + b x] - \\
 & \quad 990 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}[a + b x] + 252 a^6 A b B c d^6 \operatorname{Log}[a + b x] + 288 a^6 b B^2 c d^6 \operatorname{Log}[a + b x] - \\
 & \quad 36 a^7 A B d^7 \operatorname{Log}[a + b x] - 36 a^7 B^2 d^7 \operatorname{Log}[a + b x] - 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
 & \quad 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \\
 & \quad 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
 & \quad 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
 & \quad 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & \quad 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 252 a^6 b B^2 c d^6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & \quad 36 a^7 B^2 d^7 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 36 b^7 B^2 c^6 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] +
 \end{aligned}$$

$$\begin{aligned}
& 252 a b^6 B^2 c^5 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 756 a^2 b^5 B^2 c^4 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 5040 a^3 A b^4 B c^3 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 756 a^4 b^3 B^2 c^2 d^5 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 252 a^5 b^2 B^2 c d^6 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 36 a^6 b B^2 d^7 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 18 b^7 B^2 c^5 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 126 a b^6 B^2 c^4 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 7560 a^2 A b^5 B c^3 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 1512 a^2 b^5 B^2 c^3 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 7560 a^3 A b^4 B c^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 1512 a^3 b^4 B^2 c^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 126 a^4 b^3 B^2 c d^6 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 18 a^5 b^2 B^2 d^7 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 12 b^7 B^2 c^4 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 5040 a A b^6 B c^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 1176 a b^6 B^2 c^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 15120 a^2 A b^5 B c^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 5040 a^3 A b^4 B c d^6 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 1176 a^3 b^4 B^2 c d^6 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 12 a^4 b^3 B^2 d^7 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 1260 A b^7 B c^3 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 306 b^7 B^2 c^3 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 11340 a A b^6 B c^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 882 a b^6 B^2 c^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 11340 a^2 A b^5 B c d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 882 a^2 b^5 B^2 c d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 1260 a^3 A b^4 B d^7 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 306 a^3 b^4 B^2 d^7 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 3024 A b^7 B c^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 360 b^7 B^2 c^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 9072 a A b^6 B c d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 3024 a^2 A b^5 B d^7 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 360 a^2 b^5 B^2 d^7 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 2520 A b^7 B c d^6 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 120 b^7 B^2 c d^6 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 2520 a A b^6 B d^7 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 120 a b^6 B^2 d^7 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 720 A b^7 B d^7 x^7 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 1260 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 756 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 252 a^6 b B^2 c d^6 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] -
\end{aligned}$$



$$\begin{aligned}
 & 36 a^7 B^2 d^7 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 2520 a^3 b^4 B^2 c^3 d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 3780 a^2 b^5 B^2 c^3 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 3780 a^3 b^4 B^2 c^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 2520 a b^6 B^2 c^3 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 7560 a^2 b^5 B^2 c^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 2520 a^3 b^4 B^2 c d^6 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 630 b^7 B^2 c^3 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 5670 a b^6 B^2 c^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 5670 a^2 b^5 B^2 c d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 630 a^3 b^4 B^2 d^7 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 1512 b^7 B^2 c^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 4536 a b^6 B^2 c d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 1512 a^2 b^5 B^2 d^7 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 1260 b^7 B^2 c d^6 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 1260 a b^6 B^2 d^7 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 360 b^7 B^2 d^7 x^7 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 36 A b^7 B c^7 \operatorname{Log}[c+d x] - 36 b^7 B^2 c^7 \operatorname{Log}[c+d x] - \\
 & 252 a A b^6 B c^6 d \operatorname{Log}[c+d x] + 288 a b^6 B^2 c^6 d \operatorname{Log}[c+d x] + 756 a^2 A b^5 B c^5 d^2 \operatorname{Log}[c+d x] - \\
 & 990 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}[c+d x] - 1260 a^3 A b^4 B c^4 d^3 \operatorname{Log}[c+d x] + \\
 & 642 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}[c+d x] + 114 a^4 b^3 B^2 c^3 d^4 \operatorname{Log}[c+d x] - 18 a^5 b^2 B^2 c^2 d^5 \operatorname{Log}[c+d x] - \\
 & 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\
 & 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + \\
 & 36 b^7 B^2 c^7 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 252 a b^6 B^2 c^6 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 756 a^2 b^5 B^2 c^5 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 1260 a^3 b^4 B^2 c^4 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 36 b^4 B^2 c^4 \left(b^3 c^3 - 7 a b^2 c^2 d + 21 a^2 b c d^2 - 35 a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 36 a^4 B^2 d^4 \left(-35 b^3 c^3 + 21 a b^2 c^2 d - 7 a^2 b c d^2 + a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 75: Result more than twice size of optimal antiderivative.

$$\int (a g + b g x)^2 (c i + d i x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a + b x)}{c + d x} \right] \right)^2 dx$$

Optimal (type 4, 908 leaves, 20 steps):

$$\begin{aligned} & - \frac{7 B^2 (b c - a d)^5 g^2 i^3 x}{180 b^3 d^2} - \frac{7 B^2 (b c - a d)^4 g^2 i^3 (c + d x)^2}{360 b^2 d^3} - \\ & \frac{B^2 (b c - a d)^3 g^2 i^3 (c + d x)^3}{60 b d^3} + \frac{B^2 (b c - a d)^2 g^2 i^3 (c + d x)^4}{60 d^3} + \\ & \frac{B^2 (b c - a d)^6 g^2 i^3 \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right]}{36 b^4 d^3} - \frac{B (b c - a d)^4 g^2 i^3 (a + b x)^2 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{60 b^4 d} - \\ & \frac{B (b c - a d)^3 g^2 i^3 (a + b x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{30 b^4} - \\ & \frac{B (b c - a d)^4 g^2 i^3 (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{10 b^2 d^3} + \\ & \frac{B (b c - a d)^3 g^2 i^3 (c + d x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{45 b d^3} + \\ & \frac{7 B (b c - a d)^2 g^2 i^3 (c + d x)^4 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{60 d^3} - \\ & \frac{b B (b c - a d) g^2 i^3 (c + d x)^5 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{15 d^3} + \\ & \frac{(b c - a d)^3 g^2 i^3 (a + b x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2}{60 b^4} + \\ & \frac{(b c - a d)^2 g^2 i^3 (a + b x)^3 (c + d x) \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2}{20 b^3} + \\ & \frac{(b c - a d) g^2 i^3 (a + b x)^3 (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2}{10 b^2} + \\ & \frac{g^2 i^3 (a + b x)^3 (c + d x)^3 \left( A + B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2}{6 b} + \\ & \frac{B (b c - a d)^5 g^2 i^3 (a + b x) \left( 2 A + B + 2 B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{60 b^4 d^2} + \\ & \frac{B (b c - a d)^6 g^2 i^3 \operatorname{Log} \left[ \frac{b c - a d}{b (c + d x)} \right] \left( 2 A + 3 B + 2 B \operatorname{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)}{60 b^4 d^3} + \\ & \frac{11 B^2 (b c - a d)^6 g^2 i^3 \operatorname{Log} [c + d x]}{180 b^4 d^3} + \frac{B^2 (b c - a d)^6 g^2 i^3 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{30 b^4 d^3} \end{aligned}$$

Result (type 4, 4173 leaves):

$$\frac{1}{360 b^4 d^3} g^2 i^3 \left( 12 b^6 B^2 c^6 - 84 a b^5 B^2 c^5 d + 12 a^2 b^4 B^2 c^4 d^2 + 240 a^3 b^3 B^2 c^3 d^3 - 252 a^4 b^2 B^2 c^2 d^4 + \right.$$

$$\begin{aligned}
 & 84 a^5 b B^2 c d^5 - 12 a^6 B^2 d^6 + 12 A b^6 B c^5 d x - 16 b^6 B^2 c^5 d x - 72 a A b^5 B c^4 d^2 x + \\
 & 102 a b^5 B^2 c^4 d^2 x + 360 a^2 A^2 b^4 c^3 d^3 x - 60 a^2 A b^4 B c^3 d^3 x - 194 a^2 b^4 B^2 c^3 d^3 x + \\
 & 180 a^3 A b^3 B c^2 d^4 x + 154 a^3 b^3 B^2 c^2 d^4 x - 72 a^4 A b^2 B c d^5 x - 54 a^4 b^2 B^2 c d^5 x + \\
 & 12 a^5 A b B d^6 x + 8 a^5 b B^2 d^6 x - 6 A b^6 B c^4 d^2 x^2 + 11 b^6 B^2 c^4 d^2 x^2 + 360 a A^2 b^5 c^3 d^3 x^2 - \\
 & 204 a A b^5 B c^3 d^3 x^2 + 10 a b^5 B^2 c^3 d^3 x^2 + 540 a^2 A^2 b^4 c^2 d^4 x^2 + 180 a^2 A b^4 B c^2 d^4 x^2 - \\
 & 60 a^2 b^4 B^2 c^2 d^4 x^2 + 36 a^3 A b^3 B c d^5 x^2 + 46 a^3 b^3 B^2 c d^5 x^2 - 6 a^4 A b^2 B d^6 x^2 - \\
 & 7 a^4 b^2 B^2 d^6 x^2 + 120 A^2 b^6 c^3 d^3 x^3 - 76 A b^6 B c^3 d^3 x^3 + 18 b^6 B^2 c^3 d^3 x^3 + 720 a A^2 b^5 c^2 d^4 x^3 - \\
 & 84 a A b^5 B c^2 d^4 x^3 - 30 a b^5 B^2 c^2 d^4 x^3 + 360 a^2 A^2 b^4 c d^5 x^3 + 156 a^2 A b^4 B c d^5 x^3 + \\
 & 6 a^2 b^4 B^2 c d^5 x^3 + 4 a^3 A b^3 B d^6 x^3 + 6 a^3 b^3 B^2 d^6 x^3 + 270 A^2 b^6 c^2 d^4 x^4 - 78 A b^6 B c^2 d^4 x^4 + \\
 & 6 b^6 B^2 c^2 d^4 x^4 + 540 a A^2 b^5 c d^5 x^4 + 36 a A b^5 B c d^5 x^4 - 12 a b^5 B^2 c d^5 x^4 + 90 a^2 A^2 b^4 d^6 x^4 + \\
 & 42 a^2 A b^4 B d^6 x^4 + 6 a^2 b^4 B^2 d^6 x^4 + 216 A^2 b^6 c d^5 x^5 - 24 A b^6 B c d^5 x^5 + 144 a A^2 b^5 d^6 x^5 + \\
 & 24 a A b^5 B d^6 x^5 + 60 A^2 b^6 d^6 x^6 + 12 a b^5 B^2 c^5 d \text{ Log} \left[ \frac{a}{b} + x \right] - 72 a^2 b^4 B^2 c^4 d^2 \text{ Log} \left[ \frac{a}{b} + x \right] - \\
 & 60 a^3 b^3 B^2 c^3 d^3 \text{ Log} \left[ \frac{a}{b} + x \right] + 180 a^4 b^2 B^2 c^2 d^4 \text{ Log} \left[ \frac{a}{b} + x \right] - 72 a^5 b B^2 c d^5 \text{ Log} \left[ \frac{a}{b} + x \right] + \\
 & 12 a^6 B^2 d^6 \text{ Log} \left[ \frac{a}{b} + x \right] + 120 a^3 b^3 B^2 c^3 d^3 \text{ Log} \left[ \frac{a}{b} + x \right]^2 - 90 a^4 b^2 B^2 c^2 d^4 \text{ Log} \left[ \frac{a}{b} + x \right]^2 + \\
 & 36 a^5 b B^2 c d^5 \text{ Log} \left[ \frac{a}{b} + x \right]^2 - 6 a^6 B^2 d^6 \text{ Log} \left[ \frac{a}{b} + x \right]^2 - 12 b^6 B^2 c^6 \text{ Log} \left[ \frac{c}{d} + x \right] + \\
 & 72 a b^5 B^2 c^5 d \text{ Log} \left[ \frac{c}{d} + x \right] + 60 a^2 b^4 B^2 c^4 d^2 \text{ Log} \left[ \frac{c}{d} + x \right] - 180 a^3 b^3 B^2 c^3 d^3 \text{ Log} \left[ \frac{c}{d} + x \right] + \\
 & 72 a^4 b^2 B^2 c^2 d^4 \text{ Log} \left[ \frac{c}{d} + x \right] - 12 a^5 b B^2 c d^5 \text{ Log} \left[ \frac{c}{d} + x \right] + 6 b^6 B^2 c^6 \text{ Log} \left[ \frac{c}{d} + x \right]^2 - \\
 & 36 a b^5 B^2 c^5 d \text{ Log} \left[ \frac{c}{d} + x \right]^2 + 90 a^2 b^4 B^2 c^4 d^2 \text{ Log} \left[ \frac{c}{d} + x \right]^2 + 6 a^2 b^4 B^2 c^4 d^2 \text{ Log} [a + b x] + \\
 & 240 a^3 A b^3 B c^3 d^3 \text{ Log} [a + b x] + 128 a^3 b^3 B^2 c^3 d^3 \text{ Log} [a + b x] - 180 a^4 A b^2 B c^2 d^4 \text{ Log} [a + b x] - \\
 & 186 a^4 b^2 B^2 c^2 d^4 \text{ Log} [a + b x] + 72 a^5 A b B c d^5 \text{ Log} [a + b x] + 60 a^5 b B^2 c d^5 \text{ Log} [a + b x] - \\
 & 12 a^6 A B d^6 \text{ Log} [a + b x] - 8 a^6 B^2 d^6 \text{ Log} [a + b x] - 240 a^3 b^3 B^2 c^3 d^3 \text{ Log} \left[ \frac{a}{b} + x \right] \text{ Log} [a + b x] + \\
 & 180 a^4 b^2 B^2 c^2 d^4 \text{ Log} \left[ \frac{a}{b} + x \right] \text{ Log} [a + b x] - 72 a^5 b B^2 c d^5 \text{ Log} \left[ \frac{a}{b} + x \right] \text{ Log} [a + b x] + \\
 & 12 a^6 B^2 d^6 \text{ Log} \left[ \frac{a}{b} + x \right] \text{ Log} [a + b x] + 240 a^3 b^3 B^2 c^3 d^3 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} [a + b x] - \\
 & 180 a^4 b^2 B^2 c^2 d^4 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} [a + b x] + 72 a^5 b B^2 c d^5 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} [a + b x] - \\
 & 12 a^6 B^2 d^6 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} [a + b x] - 240 a^3 b^3 B^2 c^3 d^3 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} \left[ \frac{d(a + b x)}{-b c + a d} \right] + \\
 & 180 a^4 b^2 B^2 c^2 d^4 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} \left[ \frac{d(a + b x)}{-b c + a d} \right] - 72 a^5 b B^2 c d^5 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} \left[ \frac{d(a + b x)}{-b c + a d} \right] + \\
 & 12 a^6 B^2 d^6 \text{ Log} \left[ \frac{c}{d} + x \right] \text{ Log} \left[ \frac{d(a + b x)}{-b c + a d} \right] + 12 b^6 B^2 c^5 d x \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] - \\
 & 72 a b^5 B^2 c^4 d^2 x \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] + 720 a^2 A b^4 B c^3 d^3 x \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] - \\
 & 60 a^2 b^4 B^2 c^3 d^3 x \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] + 180 a^3 b^3 B^2 c^2 d^4 x \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] - \\
 & 72 a^4 b^2 B^2 c d^5 x \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] + 12 a^5 b B^2 d^6 x \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] - \\
 & 6 b^6 B^2 c^4 d^2 x^2 \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] + 720 a A b^5 B c^3 d^3 x^2 \text{ Log} \left[ \frac{e(a + b x)}{c + d x} \right] -
 \end{aligned}$$

$$\begin{aligned}
& 204 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 180 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 36 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 6 a^4 b^2 B^2 d^6 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 240 A b^6 B c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 76 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 1440 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 84 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 720 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 156 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 4 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 540 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 78 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 36 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 180 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 42 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 432 A b^6 B c d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 24 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 288 a A b^5 B d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 24 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
& 120 A b^6 B d^6 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 240 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 180 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 72 a^5 b B^2 c d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
& 12 a^6 B^2 d^6 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 360 a^2 b^4 B^2 c^3 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
& 360 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
& 120 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 720 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
& 360 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 270 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
& 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 90 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
& 216 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 144 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
& 60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - 12 A b^6 B c^6 \operatorname{Log}[c+d x] + 16 b^6 B^2 c^6 \operatorname{Log}[c+d x] + \\
& 72 a A b^5 B c^5 d \operatorname{Log}[c+d x] - 108 a b^5 B^2 c^5 d \operatorname{Log}[c+d x] - 180 a^2 A b^4 B c^4 d^2 \operatorname{Log}[c+d x] + \\
& 66 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}[c+d x] + 32 a^3 b^3 B^2 c^3 d^3 \operatorname{Log}[c+d x] - 6 a^4 b^2 B^2 c^2 d^4 \operatorname{Log}[c+d x] + \\
& 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] +
\end{aligned}$$

$$\begin{aligned}
 & 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
 & 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
 & 12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]- \\
 & 180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]-12 b^6 B^2 c^6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \\
 & 72 a b^5 B^2 c^5 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-180 a^2 b^4 B^2 c^4 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
 & 12 b^4 B^2 c^4\left(b^2 c^2-6 a b c d+15 a^2 d^2\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 12 a^3 B^2 d^3\left(-20 b^3 c^3+15 a b^2 c^2 d-6 a^2 b c d^2+a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 76: Result more than twice size of optimal antiderivative.**

$$\int (a g+b g x)(c i+d i x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2 d x$$

Optimal (type 4, 730 leaves, 19 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^4 g i^3 x}{60 b^3 d} + \frac{B^2 (b c - a d)^3 g i^3 (c + d x)^2}{30 b^2 d^2} + \frac{B^2 (b c - a d)^2 g i^3 (c + d x)^3}{30 b d^2} - \\ & \frac{B^2 (b c - a d)^5 g i^3 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{12 b^4 d^2} - \frac{B (b c - a d)^4 g i^3 (a + b x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{10 b^4 d} - \\ & \frac{B (b c - a d)^3 g i^3 (a + b x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{10 b^4} + \\ & \frac{3 B (b c - a d)^3 g i^3 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{20 b^2 d^2} + \\ & \frac{B (b c - a d)^2 g i^3 (c + d x)^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{30 b d^2} - \\ & \frac{B (b c - a d) g i^3 (c + d x)^4 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{10 d^2} + \frac{(b c - a d)^3 g i^3 (a + b x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{20 b^4} + \\ & \frac{(b c - a d)^2 g i^3 (a + b x)^2 (c + d x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{10 b^3} + \\ & \frac{3 (b c - a d) g i^3 (a + b x)^2 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{20 b^2} + \\ & \frac{g i^3 (a + b x)^2 (c + d x)^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{5 b} - \\ & \frac{B (b c - a d)^5 g i^3 \text{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{10 b^4 d^2} - \\ & \frac{11 B^2 (b c - a d)^5 g i^3 \text{Log}[c + d x]}{60 b^4 d^2} - \frac{B^2 (b c - a d)^5 g i^3 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{10 b^4 d^2} \end{aligned}$$

Result (type 4, 3093 leaves):

$$\begin{aligned} & \frac{1}{60 b^4 d^2} \\ & g i^3 \left( -6 b^5 B^2 c^5 - 24 a b^4 B^2 c^4 d + 90 a^2 b^3 B^2 c^3 d^2 - 90 a^3 b^2 B^2 c^2 d^3 + 36 a^4 b B^2 c d^4 - 6 a^5 B^2 d^5 - 6 A b^5 B \right. \\ & \quad c^4 d x + 11 b^5 B^2 c^4 d x + 60 a A^2 b^4 c^3 d^2 x - 30 a A b^4 B c^3 d^2 x - 28 a b^4 B^2 c^3 d^2 x + 60 a^2 A b^3 B c^2 d^3 x + \\ & \quad 24 a^2 b^3 B^2 c^2 d^3 x - 30 a^3 A b^2 B c d^4 x - 8 a^3 b^2 B^2 c d^4 x + 6 a^4 A b B d^5 x + a^4 b B^2 d^5 x + \\ & \quad 30 A^2 b^5 c^3 d^2 x^2 - 27 A b^5 B c^3 d^2 x^2 + 8 b^5 B^2 c^3 d^2 x^2 + 90 a A^2 b^4 c^2 d^3 x^2 + 15 a A b^4 B c^2 d^3 x^2 - \\ & \quad 18 a b^4 B^2 c^2 d^3 x^2 + 15 a^2 A b^3 B c d^4 x^2 + 12 a^2 b^3 B^2 c d^4 x^2 - 3 a^3 A b^2 B d^5 x^2 - 2 a^3 b^2 B^2 d^5 x^2 + \\ & \quad 60 A^2 b^5 c^2 d^3 x^3 - 22 A b^5 B c^2 d^3 x^3 + 2 b^5 B^2 c^2 d^3 x^3 + 60 a A^2 b^4 c d^4 x^3 + 20 a A b^4 B c d^4 x^3 - \\ & \quad 4 a b^4 B^2 c d^4 x^3 + 2 a^2 A b^3 B d^5 x^3 + 2 a^2 b^3 B^2 d^5 x^3 + 45 A^2 b^5 c d^4 x^4 - 6 A b^5 B c d^4 x^4 + \\ & \quad 15 a A^2 b^4 d^5 x^4 + 6 a A b^4 B d^5 x^4 + 12 A^2 b^5 d^5 x^5 - 6 a b^4 B^2 c^4 d \text{Log}\left[\frac{a}{b} + x\right] - \\ & \quad 30 a^2 b^3 B^2 c^3 d^2 \text{Log}\left[\frac{a}{b} + x\right] + 60 a^3 b^2 B^2 c^2 d^3 \text{Log}\left[\frac{a}{b} + x\right] - 30 a^4 b B^2 c d^4 \text{Log}\left[\frac{a}{b} + x\right] + \\ & \quad 6 a^5 B^2 d^5 \text{Log}\left[\frac{a}{b} + x\right] + 30 a^2 b^3 B^2 c^3 d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 30 a^3 b^2 B^2 c^2 d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 + \end{aligned}$$

$$\begin{aligned}
 & 15 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 3 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] + \\
 & 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] - 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 30 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
 & 6 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] - 3 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 15 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + \\
 & 60 a^2 A b^3 B c^3 d^2 \operatorname{Log}[a+b x] + 27 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a+b x] - 60 a^3 A b^2 B c^2 d^3 \operatorname{Log}[a+b x] - \\
 & 37 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a+b x] + 30 a^4 A b B c d^4 \operatorname{Log}[a+b x] + 11 a^4 b B^2 c d^4 \operatorname{Log}[a+b x] - \\
 & 6 a^5 A B d^5 \operatorname{Log}[a+b x] - a^5 B^2 d^5 \operatorname{Log}[a+b x] - 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \\
 & 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] - 30 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \\
 & 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
 & 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + 30 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
 & 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
 & 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 30 a^4 b B^2 c d^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
 & 6 a^5 B^2 d^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 6 b^5 B^2 c^4 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 120 a A b^4 B c^3 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 30 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 60 a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 30 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 6 a^4 b B^2 d^5 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 60 A b^5 B c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 27 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 180 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 15 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 15 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 3 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 120 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 22 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 120 a A b^4 B c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 20 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 2 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 90 A b^5 B c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 6 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 30 a A b^4 B d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 6 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 24 A b^5 B d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 60 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 60 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 30 a^4 b B^2 c d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 6 a^5 B^2 d^5 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 60 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 30 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 90 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 60 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 45 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 6 A b^5 B c^5 \operatorname{Log}[c+d x] - 11 b^5 B^2 c^5 \operatorname{Log}[c+d x] - \\
 & 30 a A b^4 B c^4 d \operatorname{Log}[c+d x] + a b^4 B^2 c^4 d \operatorname{Log}[c+d x] + 13 a^2 b^3 B^2 c^3 d^2 \operatorname{Log}[c+d x] - \\
 & 3 a^3 b^2 B^2 c^2 d^3 \operatorname{Log}[c+d x] - 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - \\
 & 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] + 6 b^5 B^2 c^5 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 30 a b^4 B^2 c^4 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 b^4 B^2 c^4 (b c-5 a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 6 a^2 B^2 d^2 \left(-10 b^3 c^3+10 a b^2 c^2 d-5 a^2 b c d^2+a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 77: Result more than twice size of optimal antiderivative.**

$$\int (c i+d i x)^3 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2 d x$$

Optimal (type 4, 420 leaves, 15 steps):

$$\begin{aligned}
 & \frac{5 B^2 (b c-a d)^3 i^3 x}{12 b^3} + \frac{B^2 (b c-a d)^2 i^3 (c+d x)^2}{12 b^2 d} + \\
 & \frac{5 B^2 (b c-a d)^4 i^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{12 b^4 d} - \frac{B (b c-a d)^3 i^3 (a+b x) \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{2 b^4} - \\
 & \frac{B (b c-a d)^2 i^3 (c+d x)^2 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{4 b^2 d} - \frac{B (b c-a d) i^3 (c+d x)^3 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{6 b d} + \\
 & \frac{i^3 (c+d x)^4 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{4 d} + \frac{11 B^2 (b c-a d)^4 i^3 \operatorname{Log}[c+d x]}{12 b^4 d} + \\
 & \frac{B (b c-a d)^4 i^3 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{Log}\left[1-\frac{b(c+d x)}{d(a+b x)}\right]}{2 b^4 d} - \frac{B^2 (b c-a d)^4 i^3 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{2 b^4 d}
 \end{aligned}$$

Result (type 4, 2110 leaves):



$$\frac{1}{12 b^4 d}$$

$$i^3 \left( -18 b^4 B^2 c^4 + 54 a b^3 B^2 c^3 d - 60 a^2 b^2 B^2 c^2 d^2 + 30 a^3 b B^2 c d^3 - 6 a^4 B^2 d^4 + 12 A^2 b^4 c^3 d x - 18 A b^4 B \right. \\ \left. c^3 d x + 7 b^4 B^2 c^3 d x + 36 a A b^3 B c^2 d^2 x - 19 a b^3 B^2 c^2 d^2 x - 24 a^2 A b^2 B c d^3 x + 17 a^2 b^2 B^2 c d^3 x + \right. \\ \left. 6 a^3 A b B d^4 x - 5 a^3 b B^2 d^4 x + 18 A^2 b^4 c^2 d^2 x^2 - 9 A b^4 B c^2 d^2 x^2 + b^4 B^2 c^2 d^2 x^2 + 12 a A b^3 B c d^3 x^2 - \right. \\ \left. 2 a b^3 B^2 c d^3 x^2 - 3 a^2 A b^2 B d^4 x^2 + a^2 b^2 B^2 d^4 x^2 + 12 A^2 b^4 c d^3 x^3 - 2 A b^4 B c d^3 x^3 + \right. \\ \left. 2 a A b^3 B d^4 x^3 + 3 A^2 b^4 d^4 x^4 - 18 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - \right. \\ \left. 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] + 12 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \right. \\ \left. 18 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 12 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 3 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\ \left. 18 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right] - 36 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] + 24 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \right. \\ \left. 6 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 24 a A b^3 B c^3 d \operatorname{Log}[a + b x] - \right. \\ \left. 36 a^2 A b^2 B c^2 d^2 \operatorname{Log}[a + b x] + 9 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] + 24 a^3 A b B c d^3 \operatorname{Log}[a + b x] - \right. \\ \left. 14 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] - 6 a^4 A B d^4 \operatorname{Log}[a + b x] + 5 a^4 B^2 d^4 \operatorname{Log}[a + b x] - \right. \\ \left. 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \right. \\ \left. 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + \right. \\ \left. 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + \right. \\ \left. 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \right. \\ \left. 24 a b^3 B^2 c^3 d \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \right. \\ \left. 24 a^3 b B^2 c d^3 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 6 a^4 B^2 d^4 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \right. \\ \left. 24 A b^4 B c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 18 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \right. \\ \left. 36 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - 24 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \right. \\ \left. 6 a^3 b B^2 d^4 x \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 36 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \right. \\ \left. 9 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \right. \\ \left. 3 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 A b^4 B c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \right. \\ \left. 2 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 2 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + \right. \\ \left. 6 A b^4 B d^4 x^4 \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a b^3 B^2 c^3 d \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \right. \\ \left. 36 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] + 24 a^3 b B^2 c d^3 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \right.$$

$$\begin{aligned}
 & 6 a^4 B^2 d^4 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 12 b^4 B^2 c^3 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 18 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 12 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - 6 A b^4 B c^4 \operatorname{Log}[c+d x] - 7 b^4 B^2 c^4 \operatorname{Log}[c+d x] + \\
 & 10 a b^3 B^2 c^3 d \operatorname{Log}[c+d x] - 3 a^2 b^2 B^2 c^2 d^2 \operatorname{Log}[c+d x] + 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x] - \\
 & 6 b^4 B^2 c^4 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 6 b^4 B^2 c^4 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 6 a B^2 d\left(-4 b^3 c^3+6 a b^2 c^2 d-4 a^2 b c d^2+a^3 d^3\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 78: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i+d i x)^3\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{a g+b g x} d x$$

Optimal (type 4, 712 leaves, 26 steps):

$$\begin{aligned}
 & \frac{B^2 d (b c - a d)^2 i^3 x}{3 b^3 g} + \frac{B^2 (b c - a d)^3 i^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{3 b^4 g} - \\
 & \frac{5 B d (b c - a d)^2 i^3 (a+b x) \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b^4 g} - \frac{B (b c - a d) i^3 (c+d x)^2 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 b^2 g} + \\
 & \frac{2 B (b c - a d)^3 i^3 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{b^4 g} + \\
 & \frac{d (b c - a d)^2 i^3 (a+b x) \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{b^4 g} + \frac{(b c - a d) i^3 (c+d x)^2 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 b^2 g} + \\
 & \frac{i^3 (c+d x)^3 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{3 b g} + \frac{2 B^2 (b c - a d)^3 i^3 \operatorname{Log}[c+d x]}{b^4 g} + \\
 & \frac{5 B (b c - a d)^3 i^3 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{3 b^4 g} - \\
 & \frac{(b c - a d)^3 i^3 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2 \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g} + \\
 & \frac{2 B^2 (b c - a d)^3 i^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{b^4 g} - \frac{5 B^2 (b c - a d)^3 i^3 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{3 b^4 g} + \\
 & \frac{2 B (b c - a d)^3 i^3 \left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g} + \\
 & \frac{2 B^2 (b c - a d)^3 i^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g}
 \end{aligned}$$

Result (type 4, 5055 leaves):

$$\begin{aligned}
 & \frac{1}{12 b^4 g} \\
 & i^3 \left( 72 a b^3 B c^3 + 9 b^3 B^2 c^3 - 144 a A b^2 B c^2 d - 23 a b^2 B^2 c^2 d + 96 a^2 A b B c d^2 - 51 a^2 b B^2 c d^2 - 24 a^3 A B \right. \\
 & \quad d^3 + 21 a^3 B^2 d^3 + 36 A^2 b^3 c^2 d x - 28 A b^3 B c^2 d x + 4 b^3 B^2 c^2 d x - 36 a A^2 b^2 c d^2 x + 48 a A b^2 B c d^2 x - \\
 & \quad 8 a b^2 B^2 c d^2 x + 12 a^2 A^2 b d^3 x - 20 a^2 A b B d^3 x + 4 a^2 b B^2 d^3 x + 18 A^2 b^3 c d^2 x^2 - 4 A b^3 B c d^2 x^2 - \\
 & \quad 6 a A^2 b^2 d^3 x^2 + 4 a A b^2 B d^3 x^2 + 4 A^2 b^3 d^3 x^3 - 72 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
 & \quad 116 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right] - 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 30 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \\
 & \quad 24 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 6 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right] + 12 A b^3 B c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & \quad 36 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 36 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
 & \quad 18 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 12 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & \quad \left. 8 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b} + x\right]^3 + 24 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 24 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^3 + \right)
 \end{aligned}$$

$$\begin{aligned}
& 8 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^3 - 72 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] + 54 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] + \\
& 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] - 90 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] - 24 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \\
& 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] - 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] + 72 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] + 60 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] - \\
& 20 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] - 50 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 42 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - \\
& 12 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 12 A^2 b^3 c^3 \operatorname{Log}[a+b x] - 36 a A^2 b^2 c^2 d \operatorname{Log}[a+b x] + \\
& 36 a^2 A^2 b c d^2 \operatorname{Log}[a+b x] - 36 a^2 A b B c d^2 \operatorname{Log}[a+b x] - 14 a^2 b B^2 c d^2 \operatorname{Log}[a+b x] - \\
& 12 a^3 A^2 d^3 \operatorname{Log}[a+b x] + 20 a^3 A B d^3 \operatorname{Log}[a+b x] - 6 a^3 B^2 d^3 \operatorname{Log}[a+b x] - \\
& 24 A b^3 B c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] - \\
& 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] - 20 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \\
& 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[a+b x] - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[a+b x] + \\
& 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[a+b x] - 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[a+b x] + \\
& 24 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + \\
& 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + 20 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
& 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \\
& \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[a+b x] - \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[a+b x] + 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[a+b x] - \\
& 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[a+b x] - 24 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
& 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
& 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] -
\end{aligned}$$

$$\begin{aligned}
 & 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+72 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 144 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+96 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+72 A b^3 B c^2 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-28 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 72 a A b^2 B c d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+48 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 24 a^2 A b B d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-20 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 36 A b^3 B c d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-4 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 12 a A b^2 B d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+4 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 8 A b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 72 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 24 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+24 A b^3 B c^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 72 a A b^2 B c^2 d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+72 a^2 A b B c d^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]- \\
 & 36 a^2 b B^2 c d^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-24 a^3 A B d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 20 a^3 B^2 d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \\
 & \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]+ \\
 & 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]-72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]
 \end{aligned}$$

$$\begin{aligned}
& \log [a+b x] \log \left[ \frac{e(a+b x)}{c+d x} \right] + 72 a^2 b B^2 c d^2 \log \left[ \frac{c}{d} + x \right] \log [a+b x] \log \left[ \frac{e(a+b x)}{c+d x} \right] - \\
& 24 a^3 B^2 d^3 \log \left[ \frac{c}{d} + x \right] \log [a+b x] \log \left[ \frac{e(a+b x)}{c+d x} \right] - 24 b^3 B^2 c^3 \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d(a+b x)}{-b c+a d} \right] \\
& \log \left[ \frac{e(a+b x)}{c+d x} \right] + 72 a b^2 B^2 c^2 d \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d(a+b x)}{-b c+a d} \right] \log \left[ \frac{e(a+b x)}{c+d x} \right] - \\
& 72 a^2 b B^2 c d^2 \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d(a+b x)}{-b c+a d} \right] \log \left[ \frac{e(a+b x)}{c+d x} \right] + \\
& 24 a^3 B^2 d^3 \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d(a+b x)}{-b c+a d} \right] \log \left[ \frac{e(a+b x)}{c+d x} \right] + 36 b^3 B^2 c^2 d x \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 - \\
& 36 a b^2 B^2 c d^2 x \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 + 12 a^2 b B^2 d^3 x \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 + \\
& 18 b^3 B^2 c d^2 x^2 \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 - 6 a b^2 B^2 d^3 x^2 \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 + \\
& 4 b^3 B^2 d^3 x^3 \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 + 12 b^3 B^2 c^3 \log [a+b x] \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 - \\
& 36 a b^2 B^2 c^2 d \log [a+b x] \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 + 36 a^2 b B^2 c d^2 \log [a+b x] \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 - \\
& 12 a^3 B^2 d^3 \log [a+b x] \log \left[ \frac{e(a+b x)}{c+d x} \right]^2 + 28 A b^3 B c^3 \log [c+d x] + 42 b^3 B^2 c^3 \log [c+d x] - \\
& 12 a A b^2 B c^2 d \log [c+d x] - 98 a b^2 B^2 c^2 d \log [c+d x] + 44 a^2 b B^2 c d^2 \log [c+d x] - \\
& 28 b^3 B^2 c^3 \log \left[ \frac{a}{b} + x \right] \log [c+d x] + 12 a b^2 B^2 c^2 d \log \left[ \frac{a}{b} + x \right] \log [c+d x] + \\
& 28 b^3 B^2 c^3 \log \left[ \frac{c}{d} + x \right] \log [c+d x] - 12 a b^2 B^2 c^2 d \log \left[ \frac{c}{d} + x \right] \log [c+d x] + \\
& 28 b^3 B^2 c^3 \log \left[ \frac{e(a+b x)}{c+d x} \right] \log [c+d x] - 12 a b^2 B^2 c^2 d \log \left[ \frac{e(a+b x)}{c+d x} \right] \log [c+d x] - \\
& 44 b^3 B^2 c^3 \log \left[ \frac{a}{b} + x \right] \log \left[ \frac{b(c+d x)}{b c-a d} \right] + 132 a b^2 B^2 c^2 d \log \left[ \frac{a}{b} + x \right] \log \left[ \frac{b(c+d x)}{b c-a d} \right] - \\
& 132 a^2 b B^2 c d^2 \log \left[ \frac{a}{b} + x \right] \log \left[ \frac{b(c+d x)}{b c-a d} \right] + 44 a^3 B^2 d^3 \log \left[ \frac{a}{b} + x \right] \log \left[ \frac{b(c+d x)}{b c-a d} \right] + \\
& 12 b^3 B^2 c^3 \log \left[ \frac{a}{b} + x \right]^2 \log \left[ \frac{b(c+d x)}{b c-a d} \right] - 36 a b^2 B^2 c^2 d \log \left[ \frac{a}{b} + x \right]^2 \log \left[ \frac{b(c+d x)}{b c-a d} \right] + \\
& 36 a^2 b B^2 c d^2 \log \left[ \frac{a}{b} + x \right]^2 \log \left[ \frac{b(c+d x)}{b c-a d} \right] - 12 a^3 B^2 d^3 \log \left[ \frac{a}{b} + x \right]^2 \log \left[ \frac{b(c+d x)}{b c-a d} \right] + \\
& 4 B^2 (b c-a d)^3 \left( -11 + 6 \log \left[ \frac{a}{b} + x \right] \right) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] - \\
& 24 B (b c-a d)^3 \left( A - B \log \left[ \frac{a}{b} + x \right] + B \log \left[ \frac{e(a+b x)}{c+d x} \right] \right) \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] - \\
& 24 b^3 B^2 c^3 \text{PolyLog} \left[ 3, \frac{d(a+b x)}{-b c+a d} \right] + 72 a b^2 B^2 c^2 d \text{PolyLog} \left[ 3, \frac{d(a+b x)}{-b c+a d} \right] - \\
& 72 a^2 b B^2 c d^2 \text{PolyLog} \left[ 3, \frac{d(a+b x)}{-b c+a d} \right] + 24 a^3 B^2 d^3 \text{PolyLog} \left[ 3, \frac{d(a+b x)}{-b c+a d} \right] -
\end{aligned}$$

$$24 b^3 B^2 c^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 72 a b^2 B^2 c^2 d \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] -$$

$$72 a^2 b B^2 c d^2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 24 a^3 B^2 d^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right]$$

**Problem 79: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^3 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{(a g + b g x)^2} dx$$

Optimal (type 4, 692 leaves, 17 steps):

$$\frac{2 B^2 (bc-ad)^2 i^3 (c+dx)}{b^3 g^2 (a+bx)} - \frac{B d^2 (bc-ad) i^3 (a+bx) \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^4 g^2}$$

$$\frac{2 B (bc-ad)^2 i^3 (c+dx) \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^3 g^2 (a+bx)} +$$

$$\frac{4 B d (bc-ad)^2 i^3 \text{Log}\left[\frac{bc-ad}{b(c+dx)}\right] \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)}{b^4 g^2} +$$

$$\frac{2 d^2 (bc-ad) i^3 (a+bx) \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{b^4 g^2} - \frac{(bc-ad)^2 i^3 (c+dx) \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{b^3 g^2 (a+bx)} +$$

$$\frac{d i^3 (c+dx)^2 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2}{2 b^2 g^2} + \frac{B^2 d (bc-ad)^2 i^3 \text{Log}[c+dx]}{b^4 g^2} +$$

$$\frac{B d (bc-ad)^2 i^3 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \text{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} -$$

$$\frac{3 d (bc-ad)^2 i^3 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right)^2 \text{Log}\left[1 - \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} +$$

$$\frac{4 B^2 d (bc-ad)^2 i^3 \text{PolyLog}\left[2, \frac{d(a+bx)}{b(c+dx)}\right]}{b^4 g^2} - \frac{B^2 d (bc-ad)^2 i^3 \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} +$$

$$\frac{6 B d (bc-ad)^2 i^3 \left(A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right]\right) \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2} +$$

$$\frac{6 B^2 d (bc-ad)^2 i^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right]}{b^4 g^2}$$

Result (type 4, 4817 leaves):

$$\frac{A^2 d^2 (3bc-2ad) i^3 x}{b^3 g^2} + \frac{A^2 d^3 i^3 x^2}{2 b^2 g^2} + \frac{-A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3}{b^4 g^2 (a+bx)} +$$

$$\frac{3 (A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3) \text{Log}[a+bx]}{b^4 g^2} +$$

$$\left( B^2 c^3 i^3 \left( -2 b c + 2 a d - 2 d (a + b x) \operatorname{Log}[a + b x] + (-2 b c + 2 a d) \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right] - \right. \right. \\ \left. \left. b(c + d x) \operatorname{Log}\left[\frac{e(a + b x)}{c + d x}\right]^2 + 2 d(a + b x) \operatorname{Log}[c + d x] \right) \right) / (b(b c - a d) g^2 (a + b x)) + \\ \frac{1}{g^2} 2 A B c^3 i^3 \left( - \frac{\left(\frac{a}{b} + x\right) \left(\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{(a + b x)^2 \operatorname{Log}\left[\frac{a}{b} + x\right]} - \frac{\frac{b\left(\frac{c}{d} + x\right) \operatorname{Log}\left[\frac{c}{d} + x\right]}{\left(-a + \frac{b c}{d}\right)^2 \left(1 - \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right)} + \frac{\operatorname{Log}\left[1 - \frac{b\left(\frac{c}{d} + x\right)}{-a + \frac{b c}{d}}\right]}{-a + \frac{b c}{d}} \right. \\ \left. - \frac{-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]}{b(a + b x)} \right) + \\ \frac{1}{g^2} 2 A B d^3 i^3 \left( - \frac{2 a\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} + \frac{3 a^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} + \frac{a^3 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} + \right. \\ \left. \frac{2 a\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} + \frac{-\frac{1}{2} b\left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \operatorname{Log}[a + b x]}{b^3}\right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{a + b x}{b}\right]}{b^2} \right) \\ \left( a^3 \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]\right) \right) \right) / \\ \left( b^4 (b c - a d) (a + b x) - \frac{-\frac{1}{2} d\left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \operatorname{Log}[c + d x]}{d^3}\right) + \frac{1}{2} x^2 \operatorname{Log}\left[\frac{c + d x}{d}\right]}{b^2} + \frac{1}{2 b^4} \left(-4 a b x + \right. \right. \\ \left. \left. b^2 x^2 + \frac{2 a^3}{a + b x} + 6 a^2 \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) - \right. \\ \left. \frac{3 a^2 \left(\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right]\right)}{b^4} \right) + \frac{1}{g^2} 6 A B c d^2 i^3 \\ \left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} - \frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 \left(1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a + b x)} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} \right. \\ \left. \left( a^2 \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + b x) \left(\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]\right) \right) \right) / \\ \left( b^3 (b c - a d) (a + b x) + \frac{1}{b^3} \right. \\ \left. \left( b x - \frac{a^2}{a + b x} - 2 a \operatorname{Log}[a + b x] \right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) + \right.$$



$$\begin{aligned}
 & \left. \frac{2 a \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] \right)}{b^3} \right) + \\
 & \frac{1}{g^2} 6 A B c^2 d i^3 \left( \frac{\text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^2} + \frac{a \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^2 (a+b x)} + \right. \\
 & \left. \left( a \left( (-b c+a d) \text{Log} \left[ \frac{c}{d} + x \right] + d(a+b x) \left( \text{Log} [a+b x] - \text{Log} [c+d x] \right) \right) \right) / \right. \\
 & \left. \left( b^2 (b c-a d) (a+b x) \right) + \frac{1}{b^2} \right. \\
 & \left. \left( \frac{a}{a+b x} + \text{Log} [a+b x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right) - \right. \\
 & \left. \frac{\text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right]}{b^2} \right) + \\
 & \frac{1}{g^2} B^2 d^3 i^3 \left( \frac{a^2 \text{Log} \left[ \frac{a}{b} + x \right]^3}{b^4} - \frac{2 a (a+b x) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^4} + \right. \\
 & \frac{a^3 \left( 2 + 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^4 (a+b x)} + \frac{1}{4 b^4} \\
 & (a+b x) \left( -7 a+b x + (6 a-2 b x) \text{Log} \left[ \frac{a}{b} + x \right] - 2 (a-b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 \right) - \\
 & \frac{2 a (c+d x) \left( 2 - 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{b^3 d} + \frac{1}{4 b^2 d^2} \\
 & (c+d x) \left( -7 c+d x + (6 c-2 d x) \text{Log} \left[ \frac{c}{d} + x \right] - 2 (c-d x) \text{Log} \left[ \frac{c}{d} + x \right]^2 \right) + \\
 & \frac{1}{2 b^4} \left( -4 a b x + b^2 x^2 + \frac{2 a^3}{a+b x} + 6 a^2 \text{Log} [a+b x] \right) \\
 & \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right)^2 - \left( a^3 \left( -b (c+d x) \text{Log} \left[ \frac{c}{d} + x \right]^2 + \right. \right. \\
 & \left. \left. 2 d (a+b x) \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + 2 d (a+b x) \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] \right) \right) / \\
 & \left( b^4 (b c-a d) (a+b x) \right) + 2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right) \\
 & \left( -\frac{2 a \left( \frac{a}{b} + x \right) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^3} + \frac{3 a^2 \text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^4} + \frac{a^3 \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^4 (a+b x)} + \right. \\
 & \left. \frac{2 a \left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{b^3} + \frac{-\frac{1}{2} b \left( -\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log} [a+b x]}{b^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{a+b x}{b} \right]}{b^2} \right. \\
 & \left. \left( a^3 \left( (-b c+a d) \text{Log} \left[ \frac{c}{d} + x \right] + d(a+b x) \left( \text{Log} [a+b x] - \text{Log} [c+d x] \right) \right) \right) / \right. \\
 & \left. \left( b^4 (b c-a d) (a+b x) \right) - \frac{-\frac{1}{2} d \left( -\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log} [c+d x]}{d^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{c+d x}{d} \right]}{b^2} - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{3 a^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] \right)}{b^4} \right) - 2 \left( -\frac{1}{b^4 d} \right. \\
 & 2 a \left( a d + 2 b d x - b d x \text{Log} \left[ \frac{c}{d} + x \right] - b c \text{Log} [c+d x] + \text{Log} \left[ \frac{a}{b} + x \right] \left( -d(a+b x) + d(a+b x) \right. \right. \\
 & \quad \left. \left. \text{Log} \left[ \frac{c}{d} + x \right] + (b c - a d) \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] \right) + (b c - a d) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] \right) + \\
 & \frac{1}{4 b^4 d^2} \left( -2 a b c d - 3 b^2 c d x - 3 a b d^2 x + b^2 d^2 x^2 + 2 a b d^2 x \text{Log} \left[ \frac{c}{d} + x \right] - \right. \\
 & \quad b^2 d^2 x^2 \text{Log} \left[ \frac{c}{d} + x \right] + a^2 d^2 \text{Log} [a+b x] + b^2 c^2 \text{Log} [c+d x] + 2 a b c d \text{Log} [c+d x] + \\
 & \quad \text{Log} \left[ \frac{a}{b} + x \right] \left( b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \text{Log} \left[ \frac{c}{d} + x \right] + (-2 b^2 c^2 + 2 a^2 d^2) \right. \\
 & \quad \left. \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] \right) + (-2 b^2 c^2 + 2 a^2 d^2) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] \right) - \\
 & \left( a^3 \left( d(a+b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 + 2 \left( (-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + d(a+b x) \right. \right. \right. \\
 & \quad \left. \left. \left( \text{Log} [a+b x] - \text{Log} [c+d x] \right) \right) - 2 \text{Log} \left[ \frac{a}{b} + x \right] \left( (b c - a d) \text{Log} \left[ \frac{c}{d} + x \right] + \right. \right. \\
 & \quad \left. \left. d(a+b x) \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] \right) - 2 d(a+b x) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] \right) \Big/ \\
 & \left( 2 b^4 (b c - a d) (a+b x) \right) + \frac{1}{2 b^4} 3 a^2 \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] \right) \right) - \\
 & \quad 2 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] + 2 \text{PolyLog} \left[ 3, \frac{d(a+b x)}{-b c+a d} \right] \Big) + \\
 & \frac{1}{b^4} 3 a^2 \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] - \right. \\
 & \quad \left. 2 \text{PolyLog} \left[ 3, \frac{b(c+d x)}{b c-a d} \right] \right) \Big) + \\
 & \frac{1}{g^2} 3 B^2 c d^2 i^3 \left( -\frac{2 a \text{Log} \left[ \frac{a}{b} + x \right]^3}{3 b^3} + \frac{(a+b x) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^3} - \right. \\
 & \quad \frac{a^2 \left( 2 + 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^3 (a+b x)} + \frac{(c+d x) \left( 2 - 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{b^2 d} + \frac{1}{b^3} \\
 & \quad \left( b x - \frac{a^2}{a+b x} - 2 a \text{Log} [a+b x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right)^2 + \\
 & \quad \left( a^2 \left( -b(c+d x) \text{Log} \left[ \frac{c}{d} + x \right]^2 + 2 d(a+b x) \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + \right. \right. \\
 & \quad \left. \left. 2 d(a+b x) \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] \right) \right) \Big/ (b^3 (b c - a d) (a+b x)) +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) \left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} - \right. \\
 & \quad \frac{a \text{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a+b x)} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} - \\
 & \quad \left. \left( a^2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a+b x) \left(\text{Log}[a+b x] - \text{Log}[c+d x]\right) \right) \right) / \right. \\
 & \quad \left. \left( b^3 (b c - a d) (a+b x) \right) + \frac{2 a \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right)}{b^3} \right) - \\
 & 2 \left( \frac{1}{b^3 d} \left( a d + 2 b d x - b d x \text{Log}\left[\frac{c}{d} + x\right] - b c \text{Log}[c+d x] + \text{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
 & \quad \left. \left( -d (a+b x) + d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + (b c - a d) \right. \\
 & \quad \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \left. \right) + \left( a^2 \left( d (a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \right. \\
 & \quad \left. \left. d (a+b x) \left(\text{Log}[a+b x] - \text{Log}[c+d x]\right) \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \quad \left. \left. d (a+b x) \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - 2 d (a+b x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) / \right. \\
 & \quad \left. \left( 2 b^3 (b c - a d) (a+b x) \right) - \frac{1}{b^3} a \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \left( \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - \right. \right. \\
 & \quad \left. \left. 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) - \\
 & \quad \frac{1}{b^3} 2 a \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - \right. \\
 & \quad \left. \left. 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \right) + \\
 & \frac{1}{g^2} 3 B^2 c^2 d i^3 \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^3}{3 b^2} + \frac{a \left( 2 + 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^2 (a+b x)} + \frac{1}{b^2} \right. \\
 & \quad \left. \left( \frac{a}{a+b x} + \text{Log}[a+b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right)^2 - \right. \\
 & \quad \left( a \left( -b (c+d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 d (a+b x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) / \left( b^2 (b c - a d) (a+b x) \right) + \\
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} + \frac{a \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right)}{b^2 (a+b x)} \right) +
 \end{aligned}$$

$$\left( a \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) /$$

$$\left( b^2 (b c - a d) (a + b x) - \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]}{b^2} \right) -$$

$$2 \left( - \left( \left( a \left( d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \right. \right. \right. \right.$$

$$\left. \left. \left. (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + \right. \right. \right.$$

$$\left. \left. \left. d (a + b x) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) /$$

$$\left( 2 b^2 (b c - a d) (a + b x) \right) + \frac{1}{2 b^2} \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - \right.$$

$$\left. 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \right) +$$

$$\frac{1}{b^2} \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - \right.$$

$$\left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right)$$

**Problem 80: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^3 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{(a g + b g x)^3} dx$$

Optimal (type 4, 604 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{4 B^2 d (b c - a d) i^3 (c + d x)}{b^3 g^3 (a + b x)} - \frac{B^2 (b c - a d) i^3 (c + d x)^2}{4 b^2 g^3 (a + b x)^2} - \\
 & \frac{4 B d (b c - a d) i^3 (c + d x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{b^3 g^3 (a + b x)} - \frac{B (b c - a d) i^3 (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{2 b^2 g^3 (a + b x)^2} + \\
 & \frac{2 B d^2 (b c - a d) i^3 \operatorname{Log} \left[ \frac{b c - a d}{b(c+d x)} \right] \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{b^4 g^3} + \frac{d^3 i^3 (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{b^4 g^3} - \\
 & \frac{2 d (b c - a d) i^3 (c + d x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{b^3 g^3 (a + b x)} - \frac{(b c - a d) i^3 (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{2 b^2 g^3 (a + b x)^2} - \\
 & \frac{3 d^2 (b c - a d) i^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2 \operatorname{Log} \left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^3} + \\
 & \frac{2 B^2 d^2 (b c - a d) i^3 \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{b^4 g^3} + \\
 & \frac{6 B d^2 (b c - a d) i^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{PolyLog} \left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^3} + \\
 & \frac{6 B^2 d^2 (b c - a d) i^3 \operatorname{PolyLog} \left[ 3, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^3}
 \end{aligned}$$

Result (type 4, 5661 leaves):

$$\begin{aligned}
 & \frac{A^2 d^3 i^3 x}{b^3 g^3} - \frac{A^2 (b^3 c^3 - 3 a b^2 c^2 d + 3 a^2 b c d^2 - a^3 d^3) i^3}{2 b^4 g^3 (a + b x)^2} - \\
 & \frac{3 (A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3)}{b^4 g^3 (a + b x)} - \frac{3 (-A^2 b c d^2 i^3 + a A^2 d^3 i^3) \operatorname{Log}[a + b x]}{b^4 g^3} - \\
 & \left( B^2 c^3 i^3 \left( b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a + b x)^2 \operatorname{Log}[a + b x] + \right. \right. \\
 & \quad \left. \left. 2 (b c - a d) (b c - 3 a d - 2 b d x) \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] + 2 b (c + d x) (b c - 2 a d - b d x) \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right]^2 + 6 a^2 d^2 \operatorname{Log}[c + d x] + 12 a b d^2 x \operatorname{Log}[c + d x] + 6 b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) \right) / \\
 & \left( 4 b (b c - a d)^2 g^3 (a + b x)^2 \right) + \frac{1}{g^3} 2 A B c^3 i^3 \left( - \frac{\left( \frac{a}{b} + x \right) \left( 2 \operatorname{Log} \left[ \frac{a}{b} + x \right] + 4 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{8 (a + b x)^3 \operatorname{Log} \left[ \frac{a}{b} + x \right]} - \frac{1}{2 b} \right. \\
 & \left. \left( \frac{b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^3 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} - \left( \frac{b^2 \left( \frac{c}{d} + x \right)^2}{\left( -a + \frac{b c}{d} \right)^4 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^2} + \frac{2 b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^3 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} \right) \operatorname{Log} \left[ \frac{c}{d} + x \right] - \right.
 \end{aligned}$$

$$\left. \frac{\log\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right]}{\left(-a + \frac{bc}{d}\right)^2} \right) - \frac{-\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]}{2b(a+bx)^2} \right) +$$

$$\frac{1}{g^3} 6ABc^2 d i^3 \left( -\frac{1 + \log\left[\frac{a}{b} + x\right]}{b^2(a+bx)} + \frac{a(1 + 2\log\left[\frac{a}{b} + x\right])}{4b^2(a+bx)^2} - \right.$$

$$\frac{(-bc + ad)\log\left[\frac{c}{d} + x\right] + d(a+bx)(\log[a+bx] - \log[c+dx])}{b^2(bc - ad)(a+bx)} -$$

$$\frac{a\left(\log\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc - ad + d(a+bx)\log[a+bx] - d(a+bx)\log[c+dx])}{(bc - ad)^2}\right)}{2b^2(a+bx)^2} -$$

$$\left. \frac{(a + 2bx)\left(-\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right)}{2b^2(a+bx)^2} \right) +$$

$$\frac{1}{g^3} 2ABd^3 i^3 \left( \frac{\left(\frac{a}{b} + x\right)\left(-1 + \log\left[\frac{a}{b} + x\right]\right)}{b^3} - \frac{3a\log\left[\frac{a}{b} + x\right]^2}{2b^4} - \frac{3a^2(1 + \log\left[\frac{a}{b} + x\right])}{b^4(a+bx)} + \right.$$

$$\frac{a^3(1 + 2\log\left[\frac{a}{b} + x\right])}{4b^4(a+bx)^2} - \frac{\left(\frac{c}{d} + x\right)\left(-1 + \log\left[\frac{c}{d} + x\right]\right)}{b^3} -$$

$$\left. \frac{\left(3a^2\left((-bc + ad)\log\left[\frac{c}{d} + x\right] + d(a+bx)(\log[a+bx] - \log[c+dx])\right)\right)}{b^4(bc - ad)(a+bx)} - \frac{a^3\left(\log\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc - ad + d(a+bx)\log[a+bx] - d(a+bx)\log[c+dx])}{(bc - ad)^2}\right)}{2b^4(a+bx)^2} - \right.$$

$$\frac{1}{2b^4} \left( -2bx + \frac{a^2(5a + 6bx)}{(a+bx)^2} + 6a\log[a+bx] \right) \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \right.$$

$$\left. \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) + \frac{3a\left(\log\left[\frac{c}{d} + x\right]\log\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right)}{b^4} \right) +$$

$$\frac{1}{g^3} 6ABcd^2 i^3 \left( \frac{\log\left[\frac{a}{b} + x\right]^2}{2b^3} + \frac{2a(1 + \log\left[\frac{a}{b} + x\right])}{b^3(a+bx)} - \frac{a^2(1 + 2\log\left[\frac{a}{b} + x\right])}{4b^3(a+bx)^2} + \right.$$

$$\left. \frac{2a\left((-bc + ad)\log\left[\frac{c}{d} + x\right] + d(a+bx)(\log[a+bx] - \log[c+dx])\right)}{b^3(bc - ad)(a+bx)} + \frac{a^2\left(\log\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc - ad + d(a+bx)\log[a+bx] - d(a+bx)\log[c+dx])}{(bc - ad)^2}\right)}{2b^3(a+bx)^2} + \right.$$

$$\left. \frac{1}{2b^3} \left( \frac{a(3a + 4bx)}{(a+bx)^2} + 2\log[a+bx] \right) \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) -$$

$$\begin{aligned}
 & \left. \frac{\log\left[\frac{c}{d} + x\right] \log\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]\right)}{b^3} + \\
 & \frac{1}{g^3} 3 B^2 c^2 d i^3 \left( -\frac{2 + 2 \log\left[\frac{a}{b} + x\right] + \log\left[\frac{a}{b} + x\right]^2}{b^2 (a+bx)} + \frac{a \left(1 + 2 \log\left[\frac{a}{b} + x\right] + 2 \log\left[\frac{a}{b} + x\right]^2\right)}{4 b^2 (a+bx)^2} + \right. \\
 & 2 \left( -\frac{1 + \log\left[\frac{a}{b} + x\right]}{b^2 (a+bx)} + \frac{a \left(1 + 2 \log\left[\frac{a}{b} + x\right]\right)}{4 b^2 (a+bx)^2} - \left( (-bc+ad) \log\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \quad \left. \left. d (a+bx) (\log[a+bx] - \log[c+dx]) \right) \right) / (b^2 (bc-ad) (a+bx)) - \\
 & \left. \frac{a \left( \log\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\log[a+bx]-d(a+bx)\log[c+dx])}{(bc-ad)^2} \right)}{2 b^2 (a+bx)^2} \right) \\
 & \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) - \\
 & \frac{(a+2bx) \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)^2}{2 b^2 (a+bx)^2} - \\
 & 2 \left( \left( d (a+bx) \log\left[\frac{a}{b} + x\right]^2 + 2 \left( (-bc+ad) \log\left[\frac{c}{d} + x\right] + d (a+bx) (\log[a+bx] - \log[c+ \right. \right. \right. \\
 & \quad \left. \left. \left. dx]) \right) \right) - 2 \log\left[\frac{a}{b} + x\right] \left( (bc-ad) \log\left[\frac{c}{d} + x\right] + d (a+bx) \log\left[\frac{b(c+dx)}{bc-ad}\right] \right) \right) - \\
 & \quad \left. 2 d (a+bx) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) / (2 b^2 (bc-ad) (a+bx)) + \\
 & \left( a \left( -d (-bc+ad) (a+bx) + (bc-ad)^2 \left( 1 + 2 \log\left[\frac{a}{b} + x\right] \right) \log\left[\frac{c}{d} + x\right] + d^2 (a+bx)^2 \right. \right. \\
 & \quad \left. \left. \log[a+bx] - d^2 (a+bx)^2 \log[c+dx] + d (a+bx) \left( d (a+bx) \log\left[\frac{a}{b} + x\right]^2 + \right. \right. \right. \\
 & \quad \left. \left. \left. 2 (bc-ad) \left( 1 + \log\left[\frac{a}{b} + x\right] \right) - 2 d (a+bx) \left( \log\left[\frac{a}{b} + x\right] \log\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) \right) / (4 b^2 (bc-ad)^2 (a+bx)^2) + \\
 & \left( -b (c+dx) \log\left[\frac{c}{d} + x\right]^2 + 2 d (a+bx) \log\left[\frac{c}{d} + x\right] \log\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
 & \quad \left. 2 d (a+bx) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) / (b^2 (bc-ad) (a+bx)) + \\
 & \left( a \left( b (c+dx) (-2ad+b(c-dx)) \log\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a+bx)^2 \log\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \right. \\
 & \quad \left. \left. 2 d (a+bx) \log\left[\frac{c}{d} + x\right] \left( b (c+dx) + d (a+bx) \log\left[\frac{d(a+bx)}{-bc+ad}\right] \right) \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. 2 d^2 (a+b x)^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(2 b^2(b c-a d)^2(a+b x)^2\right) + \\
 & \frac{1}{g^3} B^2 d^3 i^3 \left( -\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^3}{b^4} + \frac{(a+b x)\left(2-2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^4} - \right. \\
 & \frac{3 a^2\left(2+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^4(a+b x)} + \frac{a^3\left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{4 b^4(a+b x)^2} + \\
 & \frac{(c+d x)\left(2-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{b^3 d} - \frac{1}{2 b^4}\left(-2 b x+\frac{a^2(5 a+6 b x)}{(a+b x)^2}+6 a \operatorname{Log}[a+b x]\right) \\
 & \left. \left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)^2 + \right. \\
 & \left. \left(3 a^2\left(-b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+ \right. \right. \\
 & \left. \left. 2 d(a+b x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(b^4(b c-a d)(a+b x)\right) + \right. \\
 & \left. \left(a^3\left(b(c+d x)(-2 a d+b(c-d x)) \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2 d^2(a+b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+ \right. \right. \\
 & \left. \left. 2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right]\left(b(c+d x)+d(a+b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)\right) + \right. \\
 & \left. 2 d^2(a+b x)^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \\
 & \left(2 b^4(b c-a d)^2(a+b x)^2\right)+2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right) \\
 & \left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3}-\frac{3 a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^4}-\frac{3 a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^4(a+b x)}+\right. \\
 & \frac{a^3\left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{4 b^4(a+b x)^2}-\frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b^3}- \\
 & \left. \left(3 a^2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right) / \left(b^4(b c-a d)\right) \right. \\
 & \left. (a+b x)\right)-\frac{a^3\left(\operatorname{Log}\left[\frac{c}{d}+x\right]+\frac{d(a+b x)(b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x])}{(b c-a d)^2}\right)}{2 b^4(a+b x)^2} + \\
 & \left. \frac{3 a\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^4}\right) - \\
 & 2\left(\frac{1}{b^4 d}\left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right]-b c \operatorname{Log}[c+d x]+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)\right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( -d (a+b x) + d (a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] + (b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + (b c-a d) \\
 & \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \left( 3 a^2 \left( d (a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2 \left( (-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. d (a+b x) \left( \operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right) \right) - 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left( (b c-a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. d (a+b x) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - 2 d (a+b x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) / \\
 & \left( 2 b^4 (b c-a d) (a+b x) \right) + \left( a^3 \left( -d (-b c+a d) (a+b x) + (b c-a d)^2 \right. \right. \\
 & \quad \left. \left. \left( 1+2 \operatorname{Log}\left[\frac{a}{b}+x\right] \right) \operatorname{Log}\left[\frac{c}{d}+x\right] + d^2 (a+b x)^2 \operatorname{Log}[a+b x] - d^2 (a+b x)^2 \operatorname{Log}[c+d x] + \right. \right. \\
 & \quad \left. \left. d (a+b x) \left( d (a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2 (b c-a d) \left( 1+\operatorname{Log}\left[\frac{a}{b}+x\right] \right) - \right. \right. \right. \\
 & \quad \left. \left. \left. 2 d (a+b x) \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) \right) / \\
 & \left( 4 b^4 (b c-a d)^2 (a+b x)^2 \right) - \frac{1}{2 b^4} 3 a \left( \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - \right. \\
 & \quad \left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) - \\
 & \frac{1}{b^4} 3 a \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - \right. \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) + \\
 & \frac{1}{g^3} 3 B^2 c d^2 i^3 \left( \frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^3} + \frac{2 a \left( 2+2 \operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \right)}{b^3 (a+b x)} - \right. \\
 & \quad \left. \frac{a^2 \left( 1+2 \operatorname{Log}\left[\frac{a}{b}+x\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \right)}{4 b^3 (a+b x)^2} + \frac{1}{2 b^3} \right. \\
 & \quad \left. \left( \frac{a(3 a+4 b x)}{(a+b x)^2} + 2 \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right)^2 - \right. \\
 & \quad \left( 2 a \left( -b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) / \left( b^3 (b c-a d) (a+b x) \right) - \\
 & \left( a^2 \left( b(c+d x) (-2 a d+b(c-d x)) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 d^2 (a+b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \left( b(c+d x) + d(a+b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. 2 d^2 (a+b x)^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \\
 & \left( 2 b^3 (b c-a d)^2 (a+b x)^2 + 2 \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) \right. \\
 & \left( \frac{\text{Log}\left[\frac{a}{b}+x\right]^2}{2 b^3} + \frac{2 a \left(1 + \text{Log}\left[\frac{a}{b}+x\right]\right)}{b^3 (a+b x)} - \frac{a^2 \left(1 + 2 \text{Log}\left[\frac{a}{b}+x\right]\right)}{4 b^3 (a+b x)^2} + \right. \\
 & \left. \left( 2 a \left( (-b c+a d) \text{Log}\left[\frac{c}{d}+x\right] + d (a+b x) \left(\text{Log}[a+b x] - \text{Log}[c+d x]\right) \right) \right) / \left( b^3 (b c-a d) \right. \\
 & \left. (a+b x) \right) + \frac{a^2 \left( \text{Log}\left[\frac{c}{d}+x\right] + \frac{d(a+b x)(b c-a d+d(a+b x) \text{Log}[a+b x]-d(a+b x) \text{Log}[c+d x])}{(b c-a d)^2} \right)}{2 b^3 (a+b x)^2} - \right. \\
 & \left. \frac{\text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b^3} \right) - \\
 & 2 \left( - \left( \left( a \left( d (a+b x) \text{Log}\left[\frac{a}{b}+x\right]^2 + 2 \left( (-b c+a d) \text{Log}\left[\frac{c}{d}+x\right] + d (a+b x) \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \left( \text{Log}[a+b x] - \text{Log}[c+d x] \right) \right) - 2 \text{Log}\left[\frac{a}{b}+x\right] \left( (b c-a d) \text{Log}\left[\frac{c}{d}+x\right] + \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. \left. d (a+b x) \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - 2 d (a+b x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) / \right. \\
 & \left. \left( b^3 (b c-a d) (a+b x) \right) \right) - \left( a^2 \left( -d (-b c+a d) (a+b x) + (b c-a d)^2 \right. \right. \\
 & \left. \left. \left( 1 + 2 \text{Log}\left[\frac{a}{b}+x\right] \right) \text{Log}\left[\frac{c}{d}+x\right] + d^2 (a+b x)^2 \text{Log}[a+b x] - d^2 (a+b x)^2 \text{Log}[c+d x] + \right. \right. \\
 & \left. \left. d (a+b x) \left( d (a+b x) \text{Log}\left[\frac{a}{b}+x\right]^2 + 2 (b c-a d) \left( 1 + \text{Log}\left[\frac{a}{b}+x\right] \right) - \right. \right. \right. \\
 & \left. \left. \left. 2 d (a+b x) \left( \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) \right) / \\
 & \left( 4 b^3 (b c-a d)^2 (a+b x)^2 + \frac{1}{2 b^3} \left( \text{Log}\left[\frac{a}{b}+x\right]^2 \left( \text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - \right. \right. \\
 & \left. \left. 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) + \\
 & \frac{1}{b^3} \left( \text{Log}\left[\frac{c}{d}+x\right]^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - \right. \\
 & \left. \left. 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right)
 \end{aligned}$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{(a g + b g x)^5} dx$$

Optimal (type 3, 147 leaves, 3 steps):

$$-\frac{B^2 i^3 (c+d x)^4}{32 (b c - a d) g^5 (a+b x)^4} - \frac{B i^3 (c+d x)^4 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{8 (b c - a d) g^5 (a+b x)^4} - \frac{i^3 (c+d x)^4 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{4 (b c - a d) g^5 (a+b x)^4}$$

Result (type 3, 327 leaves):

$$\frac{1}{32 b^4 (b c - a d) g^5 (a+b x)^4} i^3 \left( - (8 A^2 + 4 A B + B^2) (b c - a d)^4 + 4 (8 A^2 + 4 A B + B^2) d (-b c + a d)^3 (a+b x) - \right. \\ \left. 6 (8 A^2 + 4 A B + B^2) d^2 (b c - a d)^2 (a+b x)^2 + 4 (8 A^2 + 4 A B + B^2) d^3 (-b c + a d) (a+b x)^3 - \right. \\ \left. 4 B (4 A + B) d^4 (a+b x)^4 \operatorname{Log}[a+b x] - 4 B (4 A + B) (b c - a d) \right. \\ \left. \left( (b c - a d)^3 + 4 d (b c - a d)^2 (a+b x) + 6 d^2 (b c - a d) (a+b x)^2 + 4 d^3 (a+b x)^3 \right) \right. \\ \left. \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] - 8 b^4 B^2 (c+d x)^4 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right]^2 + 4 B (4 A + B) d^4 (a+b x)^4 \operatorname{Log}[c+d x] \right)$$

**Problem 84: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 718 leaves, 25 steps):

$$\begin{aligned}
 & \frac{b B^2 (b c - a d)^2 g^3 x}{3 d^3 i} + \frac{B^2 (b c - a d)^3 g^3 \text{Log}\left[\frac{a+b x}{c+d x}\right]}{3 d^4 i} + \\
 & \frac{7 B (b c - a d)^2 g^3 (a + b x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 d^3 i} - \frac{b^2 B (b c - a d) g^3 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{3 d^4 i} + \\
 & \frac{6 B (b c - a d)^3 g^3 \text{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{d^4 i} + \\
 & \frac{3 (b c - a d)^2 g^3 (a + b x) \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^3 i} - \\
 & \frac{3 b^2 (b c - a d) g^3 (c + d x)^2 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 d^4 i} + \frac{b^3 g^3 (c + d x)^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{3 d^4 i} + \\
 & \frac{(b c - a d)^3 g^3 \text{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^4 i} - \frac{2 B^2 (b c - a d)^3 g^3 \text{Log}[c + d x]}{d^4 i} - \\
 & \frac{7 B (b c - a d)^3 g^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \text{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{3 d^4 i} + \frac{6 B^2 (b c - a d)^3 g^3 \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i} + \\
 & \frac{2 B (b c - a d)^3 g^3 \left(A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i} + \\
 & \frac{7 B^2 (b c - a d)^3 g^3 \text{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{3 d^4 i} - \frac{2 B^2 (b c - a d)^3 g^3 \text{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i}
 \end{aligned}$$

Result (type 4, 5057 leaves):

$$\begin{aligned}
 & \frac{1}{12 d^4 i} g^3 \left( 24 A b^3 B c^3 + 45 b^3 B^2 c^3 - 96 a A b^2 B c^2 d - 155 a b^2 B^2 c^2 d + 144 a^2 A b B c d^2 + 129 a^2 b B^2 c d^2 - \right. \\
 & 72 a^3 A B d^3 - 63 a^3 B^2 d^3 + 12 A^2 b^3 c^2 d x + 20 A b^3 B c^2 d x + 4 b^3 B^2 c^2 d x - 36 a A^2 b^2 c d^2 x - \\
 & 48 a A b^2 B c d^2 x - 8 a b^2 B^2 c d^2 x + 36 a^2 A^2 b d^3 x + 28 a^2 A b B d^3 x + 4 a^2 b B^2 d^3 x - 6 A^2 b^3 c d^2 x^2 - \\
 & 4 A b^3 B c d^2 x^2 + 18 a A^2 b^2 d^3 x^2 + 4 a A b^2 B d^3 x^2 + 4 A^2 b^3 d^3 x^3 - 24 b^3 B^2 c^3 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 24 a A b^2 B c^2 d \text{Log}\left[\frac{a}{b} + x\right] + 116 a b^2 B^2 c^2 d \text{Log}\left[\frac{a}{b} + x\right] - 72 a^2 A b B c d^2 \text{Log}\left[\frac{a}{b} + x\right] - \\
 & 198 a^2 b B^2 c d^2 \text{Log}\left[\frac{a}{b} + x\right] + 72 a^3 A B d^3 \text{Log}\left[\frac{a}{b} + x\right] + 126 a^3 B^2 d^3 \text{Log}\left[\frac{a}{b} + x\right] - \\
 & 12 a b^2 B^2 c^2 d \text{Log}\left[\frac{a}{b} + x\right]^2 + 42 a^2 b B^2 c d^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 50 a^3 B^2 d^3 \text{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & 24 A b^3 B c^3 \text{Log}\left[\frac{c}{d} + x\right] - 18 b^3 B^2 c^3 \text{Log}\left[\frac{c}{d} + x\right] + 72 a A b^2 B c^2 d \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 30 a b^2 B^2 c^2 d \text{Log}\left[\frac{c}{d} + x\right] - 72 a^2 A b B c d^2 \text{Log}\left[\frac{c}{d} + x\right] + 72 a^2 b B^2 c d^2 \text{Log}\left[\frac{c}{d} + x\right] - \\
 & 72 a^3 B^2 d^3 \text{Log}\left[\frac{c}{d} + x\right] + 24 b^3 B^2 c^3 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] - 72 a b^2 B^2 c^2 d \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 60 a^2 b B^2 c d^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] + 28 a^3 B^2 d^3 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 12 A b^3 B c^3 \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 b^3 B^2 c^3 \text{Log}\left[\frac{c}{d} + x\right]^2 - 36 a A b^2 B c^2 d \text{Log}\left[\frac{c}{d} + x\right]^2 +
 \end{aligned}$$

$$\begin{aligned}
 & 18 a^2 b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 36 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - \\
 & 12 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 8 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^3 - 24 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^3 + \\
 & 24 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^3 - 8 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^3 + 12 a^2 A b B c d^2 \operatorname{Log}[a+b x] + \\
 & 10 a^2 b B^2 c d^2 \operatorname{Log}[a+b x] - 28 a^3 A B d^3 \operatorname{Log}[a+b x] - 30 a^3 B^2 d^3 \operatorname{Log}[a+b x] - \\
 & 12 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + 28 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \\
 & 12 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 28 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
 & 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - \\
 & 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
 & 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 96 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 144 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 72 a^3 B^2 d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 24 A b^3 B c^2 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 20 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 72 a A b^2 B c d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 48 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 72 a^2 A b B d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 28 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - \\
 & 12 A b^3 B c d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 4 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 36 a A b^2 B d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 4 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + 8 A b^3 B d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 24 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 72 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 12 a^2 b B^2 c d^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 28 a^3 B^2 d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \\
 & 12 b^3 B^2 c^2 d x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - 36 a b^2 B^2 c d^2 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 36 a^2 b B^2 d^3 x \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - 6 b^3 B^2 c d^2 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + \\
 & 18 a b^2 B^2 d^3 x^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 4 b^3 B^2 d^3 x^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 - 12 A^2 b^3 c^3 \operatorname{Log}[c+d x] -
 \end{aligned}$$

$$\begin{aligned}
& 20 A b^3 B c^3 \operatorname{Log}[c+d x]+18 b^3 B^2 c^3 \operatorname{Log}[c+d x]+36 a A^2 b^2 c^2 d \operatorname{Log}[c+d x]+ \\
& 36 a A b^2 B c^2 d \operatorname{Log}[c+d x]-74 a b^2 B^2 c^2 d \operatorname{Log}[c+d x]-36 a^2 A^2 b c d^2 \operatorname{Log}[c+d x]+ \\
& 44 a^2 b B^2 c d^2 \operatorname{Log}[c+d x]+12 a^3 A^2 d^3 \operatorname{Log}[c+d x]+24 A b^3 B c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
& 20 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+d x]+ \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+d x]-36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+d x]+ \\
& 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+d x]-24 A b^3 B c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
& 20 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
& 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+d x]+ \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+d x]-36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+d x]+ \\
& 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+d x]-24 A b^3 B c^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]- \\
& 20 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+ \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]-72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+ \\
& 24 a^3 A B d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]- \\
& 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \\
& \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]-24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]- \\
& 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right] \\
& \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]-72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]+ \\
& 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}[c+d x]-12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 \operatorname{Log}[c+d x]+ \\
& 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 \operatorname{Log}[c+d x]-36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 \operatorname{Log}[c+d x]+
\end{aligned}$$

$$\begin{aligned}
 & 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 \operatorname{Log}[c+d x] - 24 A b^3 B c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 44 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 72 a A b^2 B c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 132 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 72 a^2 A b B c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 132 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 24 a^3 A B d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 44 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 12 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 36 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 36 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 12 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 24 b^3 B^2 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \\
 & \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 72 a b^2 B^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 72 a^2 b B^2 c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 24 a^3 B^2 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 4 B(b c-a d)^3\left(6 A+11 B+6 B \operatorname{Log}\left[\frac{c}{d}+x\right]+6 B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \\
 & 24 B^2(b c-a d)^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + \\
 & 24 b^3 B^2 c^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 72 a b^2 B^2 c^2 d \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 72 a^2 b B^2 c d^2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 24 a^3 B^2 d^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 24 b^3 B^2 c^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] - 72 a b^2 B^2 c^2 d \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] + \\
 & 72 a^2 b B^2 c d^2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] - 24 a^3 B^2 d^3 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

Problem 85: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 536 leaves, 15 steps):

$$\begin{aligned} & - \frac{B (b c - a d) g^2 (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{d^2 i} - \\ & \frac{4 B (b c - a d)^2 g^2 \operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right] \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{d^3 i} - \\ & \frac{2 (b c - a d) g^2 (a + b x) \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{d^2 i} + \frac{b^2 g^2 (c + d x)^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{2 d^3 i} - \\ & \frac{(b c - a d)^2 g^2 \operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right] \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{d^3 i} + \frac{B^2 (b c - a d)^2 g^2 \operatorname{Log}[c + d x]}{d^3 i} + \\ & \frac{B (b c - a d)^2 g^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{Log} \left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{d^3 i} - \frac{4 B^2 (b c - a d)^2 g^2 \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{d^3 i} - \\ & \frac{2 B (b c - a d)^2 g^2 \left( A + B \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{d^3 i} - \\ & \frac{B^2 (b c - a d)^2 g^2 \operatorname{PolyLog} \left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{d^3 i} + \frac{2 B^2 (b c - a d)^2 g^2 \operatorname{PolyLog} \left[ 3, \frac{d(a+b x)}{b(c+d x)} \right]}{d^3 i} \end{aligned}$$

Result (type 4, 2562 leaves):

$$\begin{aligned} & \frac{1}{12 d^3 i} g^2 \left( -12 A^2 b d (b c - 2 a d) x + 6 A^2 b^2 d^2 x^2 + 12 A^2 (b c - a d)^2 \operatorname{Log}[c + d x] + \right. \\ & 12 A B \left( -2 b^2 c^2 + 2 a b c d - b^2 c d x + a b d^2 x + 2 b^2 c^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] - b^2 c^2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - \right. \\ & a^2 d^2 \operatorname{Log}[a + b x] - 2 b^2 c d x \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] + b^2 d^2 x^2 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] + b^2 c^2 \operatorname{Log}[c + d x] + \\ & 2 b^2 c^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log}[c + d x] + 2 b^2 c^2 \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \operatorname{Log}[c + d x] - 2 b c \operatorname{Log} \left[ \frac{a}{b} + x \right] \\ & \left. \left( a d + b c \operatorname{Log}[c + d x] - b c \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] \right) + 2 b^2 c^2 \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right) - \\ & 12 a^2 A B d^2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \operatorname{Log}[c + d x] - \right. \\ & \left. 2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right) \right) - \\ & 24 a A B d \left( -2 d (a + b x) \left( -1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right) + 2 b (c + d x) \left( -1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right) - \right. \\ & \left. b c \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 b \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) (d x - c \operatorname{Log}[c + d x]) + \right. \end{aligned}$$



$$\begin{aligned}
 & 2 b c \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) + \\
 & 4 a^2 B^2 d^2 \left( \text{Log} \left[ \frac{c}{d} + x \right]^3 + 3 \text{Log} \left[ \frac{c}{d} + x \right]^2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] \right) + \right. \\
 & 3 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2 \text{Log} [c+d x] + \\
 & 3 \text{Log} \left[ \frac{a}{b} + x \right]^2 \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + 6 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] + \\
 & 3 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right) \\
 & \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 - 2 \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) + 6 \text{Log} \left[ \frac{c}{d} + x \right] \\
 & \text{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] - 6 \text{PolyLog} \left[ 3, \frac{d (a+b x)}{-b c + a d} \right] - 6 \text{PolyLog} \left[ 3, \frac{b (c+d x)}{b c - a d} \right] \Bigg) + \\
 & 8 a B^2 d \left( 3 d (a+b x) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right) - b c \text{Log} \left[ \frac{c}{d} + x \right]^3 + \right. \\
 & 3 b (c+d x) \left( 2 - 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right) + \\
 & 3 b \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right)^2 (d x - c \text{Log} [c+d x]) - \\
 & 6 \left( a d + 2 b d x - b d x \text{Log} \left[ \frac{c}{d} + x \right] - b c \text{Log} [c+d x] + \right. \\
 & \text{Log} \left[ \frac{a}{b} + x \right] \left( -d (a+b x) + d (a+b x) \text{Log} \left[ \frac{c}{d} + x \right] + (b c - a d) \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) + \\
 & (b c - a d) \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] + 3 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{e (a+b x)}{c+d x} \right] \right) \\
 & \left( -2 d (a+b x) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right) + 2 b (c+d x) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right) - b c \text{Log} \left[ \frac{c}{d} + x \right]^2 + \right. \\
 & 2 b c \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \Bigg) - \\
 & 3 b c \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + 2 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] - \right. \\
 & 2 \text{PolyLog} \left[ 3, \frac{d (a+b x)}{-b c + a d} \right] + 3 b c \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] \right) - \right. \\
 & \left. \left. 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] + 2 \text{PolyLog} \left[ 3, \frac{b (c+d x)}{b c - a d} \right] \right) \right) \Bigg) - \\
 & B^2 \left( 12 b c d (a+b x) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right) + 3 d^2 (a+b x) \right. \\
 & \left. \left( 7 a - b x + (-6 a + 2 b x) \text{Log} \left[ \frac{a}{b} + x \right] + 2 (a - b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 4 b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^3+12 b^2 c(c+d x)\left(2-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)+ \\
 & 3 b^2(c+d x)\left(7 c-d x+\left(-6 c+2 d x\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+2(c-d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)- \\
 & 6 b^2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2(d x(-2 c+d x)+2 c^2 \operatorname{Log}[c+d x])+ \\
 & 6\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \\
 & \left(-4 b c d(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)+4 b^2 c(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)-\right. \\
 & \left.2 b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+d^2\left(b x(2 a-b x)+2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 a^2 \operatorname{Log}[a+b x]\right)+\right. \\
 & \left. b^2\left(d x(-2 c+d x)-2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+2 c^2 \operatorname{Log}[c+d x]\right)+\right. \\
 & \left.4 b^2 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right)- \\
 & 12 b^2 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-\right. \\
 & \left.2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right)-6\left(2 a b c d+3 b^2 c d x+3 a b d^2 x-b^2 d^2 x^2-\right. \\
 & \left.2 a b d^2 x \operatorname{Log}\left[\frac{c}{d}+x\right]+b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-a^2 d^2 \operatorname{Log}[a+b x]-b^2 c^2 \operatorname{Log}[c+d x]-2 a b c\right. \\
 & \left. d \operatorname{Log}[c+d x]-\operatorname{Log}\left[\frac{a}{b}+x\right]\left(b d(2 a c+b x(2 c-d x))-2 d^2\left(a^2-b^2 x^2\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+\right. \\
 & \left.\left(-2 b^2 c^2+2 a^2 d^2\right) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)+2\left(b^2 c^2-a^2 d^2\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 4 b c\left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right]-b c \operatorname{Log}[c+d x]+\operatorname{Log}\left[\frac{a}{b}+x\right]\right. \\
 & \left.\left(-d(a+b x)+d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right]+\left(b c-a d\right) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)+\left(b c-a d\right) \right. \\
 & \left.\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)-2 b^2 c^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)-\right. \\
 & \left.2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right)\right)
 \end{aligned}$$

**Problem 86: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g+b g x)\left(A+B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{c i+d i x} d x$$

Optimal (type 4, 283 leaves, 9 steps):

$$\frac{2 B (b c - a d) g \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)}{d^2 i} + \frac{g (a + b x) \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)^2}{d i} +$$

$$\frac{(b c - a d) g \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right)^2}{d^2 i} + \frac{2 B^2 (b c - a d) g \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^2 i} +$$

$$\frac{2 B (b c - a d) g \left(A + B \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right]\right) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^2 i} - \frac{2 B^2 (b c - a d) g \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{d^2 i}$$

Result (type 4, 1209 leaves):

$$\frac{1}{3 d^2 i} g \left( 3 A^2 b d x - 3 A^2 (b c - a d) \operatorname{Log}[c + d x] - \right.$$

$$3 a A B d \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \operatorname{Log}[c + d x] - \right.$$

$$2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \left. \right) -$$

$$3 A B \left( -2 d (a + b x) \left( -1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 b (c + d x) \left( -1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \right.$$

$$2 b \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) (d x - c \operatorname{Log}[c + d x]) +$$

$$2 b c \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \left. \right) +$$

$$a B^2 d \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) + \right.$$

$$3 \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2 \operatorname{Log}[c + d x] +$$

$$3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] +$$

$$3 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)$$

$$\left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) + 6 \operatorname{Log}\left[\frac{c}{d} + x\right]$$

$$\operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \left. \right) +$$

$$B^2 \left( 3 d (a + b x) \left( 2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - b c \operatorname{Log}\left[\frac{c}{d} + x\right]^3 + 3 b (c + d x) \right.$$

$$\left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) + 3 b \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2$$

$$\left. \left( d x - c \operatorname{Log}[c + d x] \right) - 6 \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \right.$$

$$\begin{aligned} & \text{Log}\left[\frac{a}{b} + x\right] \left( -d (a + b x) + d (a + b x) \text{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \\ & (b c - a d) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 3 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \\ & \left( -2 d (a + b x) \left( -1 + \text{Log}\left[\frac{a}{b} + x\right] \right) + 2 b (c + d x) \left( -1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - b c \text{Log}\left[\frac{c}{d} + x\right]^2 + \right. \\ & \left. 2 b c \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) - \\ & 3 b c \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - \right. \\ & \left. 2 \text{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) + 3 b c \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) - \right. \\ & \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right) \end{aligned}$$

**Problem 87: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left( A + B \text{Log}\left[\frac{e (a+bx)}{c+dx}\right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 127 leaves, 4 steps):

$$\frac{\text{Log}\left[\frac{b c - a d}{b (c + d x)}\right] \left( A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right)^2}{d i} - \frac{2 B \left( A + B \text{Log}\left[\frac{e (a + b x)}{c + d x}\right] \right) \text{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d i} + \frac{2 B^2 \text{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{d i}$$

Result (type 4, 458 leaves):

1  
3 d i

$$\begin{aligned}
 & \left( 3 A^2 \operatorname{Log}[c+d x] - 3 A B \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \operatorname{Log}[c+d x] - \right. \right. \\
 & \quad \left. \left. 2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) + \\
 & B^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) + \right. \\
 & \quad \left. 3 \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2 \operatorname{Log}[c+d x] + \right. \\
 & \quad \left. 3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \right. \\
 & \quad \left. 3 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \right. \\
 & \quad \left. \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) + 6 \operatorname{Log}\left[\frac{c}{d}+x\right] \\
 & \quad \left. \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right)
 \end{aligned}$$

**Problem 92: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left( A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 722 leaves, 18 steps):

$$\begin{aligned}
 & \frac{2 A B (b c - a d)^2 g^3 (a + b x)}{d^3 i^2 (c + d x)} - \frac{2 B^2 (b c - a d)^2 g^3 (a + b x)}{d^3 i^2 (c + d x)} + \\
 & \frac{2 B^2 (b c - a d)^2 g^3 (a + b x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^3 i^2 (c + d x)} - \frac{b B (b c - a d) g^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{d^3 i^2} - \\
 & \frac{6 b B (b c - a d)^2 g^3 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{d^4 i^2} - \\
 & \frac{3 b (b c - a d) g^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^3 i^2} - \\
 & \frac{(b c - a d)^2 g^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^3 i^2 (c + d x)} + \frac{b^3 g^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 d^4 i^2} - \\
 & \frac{3 b (b c - a d)^2 g^3 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^4 i^2} + \frac{b B^2 (b c - a d)^2 g^3 \operatorname{Log}[c + d x]}{d^4 i^2} + \\
 & \frac{b B (b c - a d)^2 g^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{Log}\left[1 - \frac{b(c+d x)}{d(a+b x)}\right]}{d^4 i^2} - \frac{6 b B^2 (b c - a d)^2 g^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^2} - \\
 & \frac{6 b B (b c - a d)^2 g^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^2} - \\
 & \frac{b B^2 (b c - a d)^2 g^3 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{d^4 i^2} + \frac{6 b B^2 (b c - a d)^2 g^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^2}
 \end{aligned}$$

Result(type 4, 4743 leaves):

$$\begin{aligned}
 & -\frac{A^2 b^2 (2 b c - 3 a d) g^3 x}{d^3 i^2} + \frac{A^2 b^3 g^3 x^2}{2 d^2 i^2} + \frac{A^2 b^3 c^3 g^3 - 3 a A^2 b^2 c^2 d g^3 + 3 a^2 A^2 b c d^2 g^3 - a^3 A^2 d^3 g^3}{d^4 i^2 (c + d x)} + \\
 & \frac{a^3 B^2 g^3 (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2\right)}{(b c - a d) i^2 (c + d x)} + \\
 & \frac{3 (A^2 b^3 c^2 g^3 - 2 a A^2 b^2 c d g^3 + a^2 A^2 b d^2 g^3) \operatorname{Log}[c + d x]}{d^4 i^2} + \\
 & \frac{1}{i^2} 2 a^3 A B g^3 \left( \frac{\left(\frac{c}{d} + x\right) \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{(c + d x)^2 \operatorname{Log}\left[\frac{c}{d} + x\right]} + \right.
 \end{aligned}$$

$$\left. \frac{\frac{d \left(\frac{a}{b}+x\right) \operatorname{Log}\left[\frac{a}{b}+x\right]}{\left(-c+\frac{a d}{b}\right)^2 \left(1-\frac{d\left(\frac{a}{b}+x\right)}{-c+\frac{a d}{b}}\right)}+ \frac{\operatorname{Log}\left[1-\frac{d\left(\frac{a}{b}+x\right)}{-c+\frac{a d}{b}}\right]}{-c+\frac{a d}{b}}}{d}-\frac{-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]}{d(c+d x)}\right\}+$$

$$\frac{1}{i^2} 2 A b^3 B g^3 \left( -\frac{2 c\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{d^3}+\frac{2 c\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3}-\frac{3 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2 d^4}-\frac{c^3\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^4(c+d x)}+\frac{-\frac{1}{2} b\left(-\frac{a x}{b^2}+\frac{x^2}{2 b}+\frac{a^2 \operatorname{Log}[a+b x]}{b^3}\right)+\frac{1}{2} x^2 \operatorname{Log}\left[\frac{a+b x}{b}\right]}{d^2}-\frac{c^3\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)}-\frac{b \operatorname{Log}[a+b x]}{d(-b c+a d)}+\frac{b \operatorname{Log}[c+d x]}{d(-b c+a d)}\right)}{d^3}-\frac{-\frac{1}{2} d\left(-\frac{c x}{d^2}+\frac{x^2}{2 d}+\frac{c^2 \operatorname{Log}[c+d x]}{d^3}\right)+\frac{1}{2} x^2 \operatorname{Log}\left[\frac{c+d x}{d}\right]}{d^2}+\frac{1}{2 d^4}\left(-4 c d x+d^2 x^2+\frac{2 c^3}{c+d x}+6 c^2 \operatorname{Log}[c+d x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]+\frac{3 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{d^4}\right)\right\}+$$

$$\frac{1}{i^2} 6 a A b^2 B g^3 \left( \frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{d^2}-\frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^2}+\frac{c \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^3}+\frac{c^2\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3(c+d x)}+\frac{c^2\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)}-\frac{b \operatorname{Log}[a+b x]}{d(-b c+a d)}+\frac{b \operatorname{Log}[c+d x]}{d(-b c+a d)}\right)}{d^2}+\frac{1}{d^3}\left(d x-\frac{c^2}{c+d x}-2 c \operatorname{Log}[c+d x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a e}{c+d x}+\frac{b e x}{c+d x}\right]\right)-\frac{2 c\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{d^3}\right\}+\frac{1}{i^2}$$

$$6 a^2 A b B g^3 \left( -\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2 d^2}-\frac{c\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^2(c+d x)}-\frac{c\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)}-\frac{b \operatorname{Log}[a+b x]}{d(-b c+a d)}+\frac{b \operatorname{Log}[c+d x]}{d(-b c+a d)}\right)}{d}+\right.$$

$$\frac{1}{d^2} \left( \frac{c}{c+d x} + \text{Log}[c+d x] \right) \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) +$$

$$\frac{\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^2} \right) +$$

$$\frac{1}{i^2} b^3 B^2 g^3 \left( -\frac{2 c(a+b x)\left(2-2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{a}{b}+x\right]^2\right)}{b d^3} + \frac{1}{4 b^2 d^2} \right.$$

$$(a+b x)\left(-7 a+b x+(6 a-2 b x) \text{Log}\left[\frac{a}{b}+x\right]-2(a-b x) \text{Log}\left[\frac{a}{b}+x\right]^2\right) + \frac{c^2 \text{Log}\left[\frac{c}{d}+x\right]^3}{d^4} -$$

$$\frac{2 c(c+d x)\left(2-2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2\right)}{d^4} + \frac{c^3\left(2+2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2\right)}{d^4(c+d x)} +$$

$$\frac{1}{4 d^4}(c+d x)\left(-7 c+d x+(6 c-2 d x) \text{Log}\left[\frac{c}{d}+x\right]-2(c-d x) \text{Log}\left[\frac{c}{d}+x\right]^2\right) +$$

$$\frac{1}{2 d^4}\left(-4 c d x+d^2 x^2+\frac{2 c^3}{c+d x}+6 c^2 \text{Log}[c+d x]\right)$$

$$\left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]\right)^2 - \left(c^3\left(-d(a+b x) \text{Log}\left[\frac{a}{b}+x\right]^2 +\right.\right.$$

$$\left.\left.2 b(c+d x) \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 b(c+d x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right) /$$

$$\left(d^4(-b c+a d)(c+d x)\right) + 2\left(-\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]\right)$$

$$\left(-\frac{2 c\left(\frac{a}{b}+x\right)\left(-1+\text{Log}\left[\frac{a}{b}+x\right]\right)}{d^3} + \frac{2 c\left(\frac{c}{d}+x\right)\left(-1+\text{Log}\left[\frac{c}{d}+x\right]\right)}{d^3} - \frac{3 c^2 \text{Log}\left[\frac{c}{d}+x\right]^2}{2 d^4} -$$

$$\frac{c^3\left(1+\text{Log}\left[\frac{c}{d}+x\right]\right)}{d^4(c+d x)} + \frac{-\frac{1}{2} b\left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a+b x]}{b^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{a+b x}{b}\right]}{d^2} -$$

$$\frac{c^3\left(-\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)} - \frac{b \text{Log}[a+b x]}{d(-b c+a d)} + \frac{b \text{Log}[c+d x]}{d(-b c+a d)}\right)}{d^3} - \frac{-\frac{1}{2} d\left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c+d x]}{d^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c+d x}{d}\right]}{d^2} +$$

$$\left.\frac{3 c^2\left(\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{d^4} \right) + \frac{1}{d^4}$$

$$3 c^2\left(\text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] -$$



$$\begin{aligned}
 & 2 \operatorname{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 2 \left( -\frac{1}{bd^4} \right. \\
 & 2c \left( ad + 2bdx - bdx \operatorname{Log}\left[\frac{c}{d} + x\right] - bc \operatorname{Log}[c+dx] + \operatorname{Log}\left[\frac{a}{b} + x\right] \left( -d(a+bx) + d(a+bx) \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
 & \frac{1}{4b^2d^4} \left( -2abcd - 3b^2cdx - 3abd^2x + b^2d^2x^2 + 2abd^2x \operatorname{Log}\left[\frac{c}{d} + x\right] - \right. \\
 & \quad \left. b^2d^2x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + a^2d^2 \operatorname{Log}[a+bx] + b^2c^2 \operatorname{Log}[c+dx] + 2abcd \operatorname{Log}[c+dx] + \right. \\
 & \quad \left. \operatorname{Log}\left[\frac{a}{b} + x\right] \left( bd(2ac+bx(2c-dx)) - 2d^2(a^2-b^2x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + (-2b^2c^2+2a^2d^2) \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (-2b^2c^2+2a^2d^2) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) - \\
 & \left( c^3 \left( 2(bc-ad) \operatorname{Log}\left[\frac{a}{b} + x\right] \left( 1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + b(c+dx) \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \right. \right. \right. \\
 & \quad \left. \left. 2 \operatorname{Log}[a+bx] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - \right. \\
 & \quad \left. \left. 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / (2d^4(-bc+ad)(c+dx)) + \\
 & \frac{1}{2d^4} 3c^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right. \\
 & \quad \left. \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \left. \right) + \\
 & \frac{1}{i^2} 3ab^2B^2g^3 \left( \frac{(a+bx) \left( 2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{bd^2} - \frac{2c \operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3d^3} + \right. \\
 & \quad \frac{(c+dx) \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^3} - \frac{c^2 \left( 2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^3(c+dx)} + \frac{1}{d^3} \\
 & \quad \left( dx - \frac{c^2}{c+dx} - 2c \operatorname{Log}[c+dx] \right) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)^2 + \\
 & \quad \left( c^2 \left( -d(a+bx) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \\
 & \quad \left. \left. 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / \\
 & \quad \left( d^3(-bc+ad)(c+dx) \right) + 2 \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right)
 \end{aligned}$$

$$\left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{d^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2} + \frac{c \text{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \right.$$

$$\frac{c^2 \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + d x)} + \frac{c^2 \left(-\frac{\text{Log}\left[\frac{a+x}{b}\right]}{d (c+d x)} - \frac{b \text{Log}[a+b x]}{d (-b c+a d)} + \frac{b \text{Log}[c+d x]}{d (-b c+a d)}\right)}{d^2} -$$

$$\left. \frac{2 c \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right]\right)}{d^3} - \frac{1}{d^3} \right)$$

$$2 c \left(\text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right] - \right.$$

$$2 \text{PolyLog}\left[3, \frac{d (a+b x)}{-b c+a d}\right] - 2 \left(\frac{1}{b d^3} \left(a d + 2 b d x - b d x \text{Log}\left[\frac{c}{d} + x\right] - b c \text{Log}[c+d x] + \right.$$

$$\left. \text{Log}\left[\frac{a}{b} + x\right] \left(-d (a+b x) + d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] + (b c-a d) \text{Log}\left[\frac{b (c+d x)}{b c-a d}\right]\right) + \right.$$

$$\left. (b c-a d) \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right]\right) + \left(c^2 \left(2 (b c-a d) \text{Log}\left[\frac{a}{b} + x\right] \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right) + \right.$$

$$\left. b (c+d x) \left(\text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a+b x)}{-b c+a d}\right] + \right.$$

$$\left. \left. 2 \text{Log}[c+d x]\right) - 2 b (c+d x) \text{PolyLog}\left[2, \frac{b (c+d x)}{b c-a d}\right]\right) \Bigg/$$

$$\left(2 d^3 (-b c+a d) (c+d x) - \frac{1}{d^3} c \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d (a+b x)}{-b c+a d}\right]\right) - \right.$$

$$\left. \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b (c+d x)}{b c-a d}\right] + 2 \text{PolyLog}\left[3, \frac{b (c+d x)}{b c-a d}\right]\right) \Bigg) + \right.$$

$$\frac{1}{i^2} 3 a^2 b B^2 g^3 \left(\frac{\text{Log}\left[\frac{c}{d} + x\right]^3}{3 d^2} + \frac{c \left(2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^2 (c+d x)} + \frac{1}{d^2} \right.$$

$$\left(\frac{c}{c+d x} + \text{Log}[c+d x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]\right)^2 -$$

$$\left(c \left(-d (a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c+d x) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + \right.$$

$$\left. \left. 2 b (c+d x) \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right]\right) \Bigg/ \left(d^2 (-b c+a d) (c+d x) + \right.$$

$$\begin{aligned}
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right) \left( -\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} - \frac{c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2 (c+d x)} - \right. \\
 & \left. \frac{c \left( -\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c+d x)} - \frac{b \text{Log}[a+b x]}{d (-b c+a d)} + \frac{b \text{Log}[c+d x]}{d (-b c+a d)} \right)}{d} + \frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right]}{d^2} \right) + \\
 & \frac{1}{d^2} \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b (c+d x)}{b c-a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c+a d}\right] - \right. \\
 & \left. 2 \text{PolyLog}\left[3, \frac{d (a+b x)}{-b c+a d}\right] \right) - 2 \left( -\left( \left( c \left( 2 (b c-a d) \text{Log}\left[\frac{a}{b} + x\right] \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right) + b (c+d x) \right. \right. \right. \right. \right. \\
 & \left. \left. \left( \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a+b x)}{-b c+a d}\right] + 2 \text{Log}[c+d x] \right) - 2 \right. \right. \\
 & \left. \left. b (c+d x) \text{PolyLog}\left[2, \frac{b (c+d x)}{b c-a d}\right] \right) \right) / \left( 2 d^2 (-b c+a d) (c+d x) \right) + \frac{1}{2 d^2} \\
 & \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d (a+b x)}{-b c+a d}\right] \right) - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b (c+d x)}{b c-a d}\right] + \right. \\
 & \left. \left. 2 \text{PolyLog}\left[3, \frac{b (c+d x)}{b c-a d}\right] \right) \right)
 \end{aligned}$$

**Problem 93: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^2 \left( A + B \text{Log}\left[\frac{e (a+b x)}{c+d x}\right] \right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 469 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{2 A B (b c - a d) g^2 (a + b x)}{d^2 i^2 (c + d x)} + \frac{2 B^2 (b c - a d) g^2 (a + b x)}{d^2 i^2 (c + d x)} - \\
 & \frac{2 B^2 (b c - a d) g^2 (a + b x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^2 i^2 (c + d x)} + \frac{2 b B (b c - a d) g^2 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{d^3 i^2} + \\
 & \frac{b g^2 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^2 i^2} + \frac{(b c - a d) g^2 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^2 i^2 (c + d x)} + \\
 & \frac{2 b (b c - a d) g^2 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^3 i^2} + \frac{2 b B^2 (b c - a d) g^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^3 i^2} + \\
 & \frac{4 b B (b c - a d) g^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^3 i^2} - \\
 & \frac{4 b B^2 (b c - a d) g^2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d^3 i^2}
 \end{aligned}$$

Result (type 4, 2704 leaves):

$$\begin{aligned}
 & \frac{A^2 b^2 g^2 x}{d^2 i^2} + \frac{-A^2 b^2 c^2 g^2 + 2 a A^2 b c d g^2 - a^2 A^2 d^2 g^2}{d^3 i^2 (c + d x)} + \\
 & \frac{a^2 B^2 g^2 (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2\right)}{(b c - a d) i^2 (c + d x)} + \\
 & \frac{2 \left(-A^2 b^2 c g^2 + a A^2 b d g^2\right) \operatorname{Log}[c + d x]}{d^3 i^2} + \frac{1}{i^2} 2 a^2 A B g^2 \left( \frac{\left(\frac{c}{d} + x\right) \left(\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{(c + d x)^2 \operatorname{Log}\left[\frac{c}{d} + x\right]} + \right. \\
 & \left. \frac{\frac{d\left(\frac{a}{b} + x\right) \operatorname{Log}\left[\frac{a}{b} + x\right]}{\left(-c + \frac{a d}{b}\right)^2 \left(1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)} + \frac{\operatorname{Log}\left[1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right]}{-c + \frac{a d}{b}} - \frac{-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]}{d(c + d x)} \right) + \\
 & \frac{1}{i^2} 2 A b^2 B g^2 \left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{d^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^2} + \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{c^2 \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + d x)} + \frac{c^2 \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \operatorname{Log}[a + b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c + d x]}{d (-b c + a d)}\right)}{d^2} + \frac{1}{d^3} \\
 & \left(d x - \frac{c^2}{c + d x} - 2 c \operatorname{Log}[c + d x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) - \\
 & \left.\frac{2 c \left(\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]\right)}{d^3} \right) + \frac{1}{i^2} \\
 & 4 a A b B g^2 \left(-\frac{\operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} - \frac{c \left(1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^2 (c + d x)} - \frac{c \left(-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \operatorname{Log}[a + b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c + d x]}{d (-b c + a d)}\right)}{d} + \right. \\
 & \left.\frac{1}{d^2} \left(\frac{c}{c + d x} + \operatorname{Log}[c + d x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) + \right. \\
 & \left.\frac{\operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{d^2} \right) + \\
 & \frac{1}{i^2} b^2 B^2 g^2 \left(\frac{(a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2\right)}{b d^2} - \frac{2 c \operatorname{Log}\left[\frac{c}{d} + x\right]^3}{3 d^3} + \right. \\
 & \left.\frac{(c + d x) \left(2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^3} - \frac{c^2 \left(2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^3 (c + d x)} + \frac{1}{d^3} \right. \\
 & \left.\left(d x - \frac{c^2}{c + d x} - 2 c \operatorname{Log}[c + d x]\right) \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right)^2 + \right. \\
 & \left.\left(c^2 \left(-d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \right. \right. \\
 & \left. \left. 2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]\right)\right) / \\
 & \left(d^3 (-b c + a d) (c + d x) + 2 \left(-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right]\right) \right. \\
 & \left.\left(\frac{\left(\frac{a}{b} + x\right) (-1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{d^2} - \frac{\left(\frac{c}{d} + x\right) (-1 + \operatorname{Log}\left[\frac{c}{d} + x\right])}{d^2} + \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{c^2 \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^3 (c + d x)} + \frac{c^2 \left( -\frac{\text{Log} \left[ \frac{a}{b} + x \right]}{d (c + d x)} - \frac{b \text{Log} [a + b x]}{d (-b c + a d)} + \frac{b \text{Log} [c + d x]}{d (-b c + a d)} \right)}{d^2} - \\
 & \left. \frac{2 c \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right)}{d^3} \right) - \frac{1}{d^3} \\
 & 2 c \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + 2 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] - \right. \\
 & \left. 2 \text{PolyLog} \left[ 3, \frac{d (a + b x)}{-b c + a d} \right] \right) - 2 \left( \frac{1}{b d^3} \left( a d + 2 b d x - b d x \text{Log} \left[ \frac{c}{d} + x \right] - b c \text{Log} [c + d x] + \right. \right. \\
 & \left. \left. \text{Log} \left[ \frac{a}{b} + x \right] \left( -d (a + b x) + d (a + b x) \text{Log} \left[ \frac{c}{d} + x \right] + (b c - a d) \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] \right) + \right. \\
 & \left. (b c - a d) \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \left( c^2 \left( 2 (b c - a d) \text{Log} \left[ \frac{a}{b} + x \right] \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right) + \right. \right. \\
 & \left. \left. b (c + d x) \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 - 2 \text{Log} [a + b x] - 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \right. \right. \right. \\
 & \left. \left. \left. 2 \text{Log} [c + d x] \right) \right) - 2 b (c + d x) \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \Bigg/ \\
 & \left( 2 d^3 (-b c + a d) (c + d x) \right) - \frac{1}{d^3} c \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] \right) - \right. \\
 & \left. \left. 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] + 2 \text{PolyLog} \left[ 3, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \Bigg) + \\
 & \frac{1}{i^2} 2 a b B^2 g^2 \left( \frac{\text{Log} \left[ \frac{c}{d} + x \right]^3}{3 d^2} + \frac{c \left( 2 + 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{d^2 (c + d x)} + \frac{1}{d^2} \right. \\
 & \left. \left( \frac{c}{c + d x} + \text{Log} [c + d x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c + d x} + \frac{b e x}{c + d x} \right] \right)^2 - \right. \\
 & \left. \left( c \left( -d (a + b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 + 2 b (c + d x) \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \right. \right. \right. \\
 & \left. \left. \left. 2 b (c + d x) \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right) \right) \Bigg/ (d^2 (-b c + a d) (c + d x)) + \right. \\
 & \left. 2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c + d x} + \frac{b e x}{c + d x} \right] \right) \left( -\frac{\text{Log} \left[ \frac{c}{d} + x \right]^2}{2 d^2} - \frac{c \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^2 (c + d x)} - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{c \left( -\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)} - \frac{b \text{Log}[a+b x]}{d(-b c+a d)} + \frac{b \text{Log}[c+d x]}{d(-b c+a d)} \right)}{d} + \frac{\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^2} \right) + \\
 & \frac{1}{d^2} \left( \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \right. \\
 & \quad 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \left. - 2 \left( -\left( \left( c \left( 2(b c-a d) \text{Log}\left[\frac{a}{b}+x\right] \left( 1+\text{Log}\left[\frac{c}{d}+x\right] \right) + b(c+d x) \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \left( \text{Log}\left[\frac{c}{d}+x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \text{Log}[c+d x] \right) - 2 \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left. \left. \left. b(c+d x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right) \right) \right) \right) \left. \right) / \left( 2 d^2 (-b c+a d)(c+d x) \right) + \frac{1}{2 d^2} \\
 & \quad \left( \text{Log}\left[\frac{c}{d}+x\right]^2 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + \right. \\
 & \quad \left. \left. 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \left. \right)
 \end{aligned}$$

**Problem 94: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x) \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 261 leaves, 9 steps):

$$\begin{aligned}
 & \frac{2 A B g(a+b x)}{d i^2(c+d x)} - \frac{2 B^2 g(a+b x)}{d i^2(c+d x)} + \frac{2 B^2 g(a+b x) \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d i^2(c+d x)} - \\
 & \frac{g(a+b x) \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{d i^2(c+d x)} - \frac{b g \text{Log}\left[\frac{b c-a d}{b(c+d x)}\right] \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right)^2}{d^2 i^2} - \\
 & \frac{2 b B g \left( A + B \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] \right) \text{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^2 i^2} + \frac{2 b B^2 g \text{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d^2 i^2}
 \end{aligned}$$

Result (type 4, 1145 leaves):

$$\begin{aligned}
 & \frac{1}{i^2} g \left( \frac{A^2(b c-a d)}{d^2(c+d x)} + \frac{a B^2(a+b x) \left( 2 - 2 \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] + \text{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 \right)}{(b c-a d)(c+d x)} + \right. \\
 & \quad \frac{A^2 b \text{Log}[c+d x]}{d^2} - \left( 2 a A B \left( b c-a d + b(c+d x) \text{Log}\left[\frac{a}{b}+x\right] + \right. \right. \\
 & \quad \left. \left. (-b c+a d) \text{Log}\left[\frac{e(a+b x)}{c+d x}\right] - b c \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - b d x \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) \right) \left. \right) /
 \end{aligned}$$

$$\begin{aligned}
 & (d(-bc+ad)(c+dx)) + \frac{1}{d^2} A B B \left( -\text{Log}\left[\frac{c}{d}+x\right]^2 + 2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}[c+dx] + \right. \\
 & 2 \left( -\frac{c}{c+dx} + \frac{bc \text{Log}[a+bx]}{-bc+ad} + \frac{bc \text{Log}[c+dx]}{bc-ad} - \text{Log}\left[\frac{a}{b}+x\right] \text{Log}[c+dx] + \right. \\
 & \quad \left. \left. \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \left( \frac{c}{c+dx} + \text{Log}[c+dx] \right) + \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + \right. \\
 & \quad \left. 2 \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \frac{1}{3d^2(bc-ad)(c+dx)} \\
 & b B^2 \left( (bc-ad)(c+dx) \text{Log}\left[\frac{c}{d}+x\right]^3 + 3c(bc-ad) \left( 2 + 2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2 \right) + \right. \\
 & \quad 3(bc-ad) \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2 (c+(c+dx) \text{Log}[c+dx]) + \\
 & \quad 3c \text{Log}\left[\frac{a}{b}+x\right] \left( -d(a+bx) \text{Log}\left[\frac{a}{b}+x\right] + 2b(c+dx) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + \\
 & \quad 6bc(c+dx) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] + 3 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right) \\
 & \quad \left( (bc-ad)(c+dx) \text{Log}\left[\frac{c}{d}+x\right]^2 + 2c(bc-ad) \left( 1 + \text{Log}\left[\frac{c}{d}+x\right] \right) + \right. \\
 & \quad 2c \left( (-bc+ad) \text{Log}\left[\frac{a}{b}+x\right] + b(c+dx) (\text{Log}[a+bx] - \text{Log}[c+dx]) \right) - 2(bc-ad) \\
 & \quad (c+dx) \left( \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \left. \right) + 3(bc-ad) \\
 & (c+dx) \left( \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \right. \\
 & \quad 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \left. \right) - 3 \left( c \left( 2(bc-ad) \text{Log}\left[\frac{a}{b}+x\right] \left( 1 + \text{Log}\left[\frac{c}{d}+x\right] \right) + \right. \right. \\
 & \quad b(c+dx) \left( \text{Log}\left[\frac{c}{d}+x\right]^2 - 2 \text{Log}[a+bx] - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
 & \quad \quad \left. \left. 2 \text{Log}[c+dx] \right) - 2b(c+dx) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) + \\
 & \quad (bc-ad)(c+dx) \left( \text{Log}\left[\frac{c}{d}+x\right]^2 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - \right. \\
 & \quad \left. \left. 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

**Problem 100: Result more than twice size of optimal antiderivative.**

$$\int \frac{(ag+bgx)^3 \left( A + B \text{Log}\left[\frac{e(a+bx)}{c+dx}\right] \right)^2}{(ci+dix)^3} dx$$



Optimal (type 4, 635 leaves, 14 steps):

$$\begin{aligned}
 & \frac{B^2 (b c - a d) g^3 (a + b x)^2}{4 d^2 i^3 (c + d x)^2} - \frac{4 A b B (b c - a d) g^3 (a + b x)}{d^3 i^3 (c + d x)} + \frac{4 b B^2 (b c - a d) g^3 (a + b x)}{d^3 i^3 (c + d x)} - \\
 & \frac{4 b B^2 (b c - a d) g^3 (a + b x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]}{d^3 i^3 (c + d x)} - \frac{B (b c - a d) g^3 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{2 d^2 i^3 (c + d x)^2} + \\
 & \frac{2 b^2 B (b c - a d) g^3 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)}{d^4 i^3} + \frac{b^2 g^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^3 i^3} + \\
 & \frac{(b c - a d) g^3 (a + b x)^2 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{2 d^2 i^3 (c + d x)^2} + \frac{2 b (b c - a d) g^3 (a + b x) \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^3 i^3 (c + d x)} + \\
 & \frac{3 b^2 (b c - a d) g^3 \operatorname{Log}\left[\frac{b c - a d}{b(c+d x)}\right] \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right)^2}{d^4 i^3} + \frac{2 b^2 B^2 (b c - a d) g^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^3} + \\
 & \frac{6 b^3 B (b c - a d) g^3 \left(A + B \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]\right) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^3} - \\
 & \frac{6 b^2 B^2 (b c - a d) g^3 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^3}
 \end{aligned}$$

Result (type 4, 5648 leaves):

$$\begin{aligned}
 & \frac{A^2 b^3 g^3 x}{d^3 i^3} - \frac{A^2 (-b^3 c^3 + 3 a b^2 c^2 d - 3 a^2 b c d^2 + a^3 d^3) g^3}{2 d^4 i^3 (c + d x)^2} - \\
 & \frac{3 (A^2 b^3 c^2 g^3 - 2 a A^2 b^2 c d g^3 + a^2 A^2 b d^2 g^3)}{d^4 i^3 (c + d x)} + \frac{3 (-A^2 b^3 c g^3 + a A^2 b^2 d g^3) \operatorname{Log}[c + d x]}{d^4 i^3} + \\
 & \left( a^3 B^2 g^3 \left( -7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c + d x)^2 \operatorname{Log}[a + b x] + \right. \right. \\
 & \quad \left. \left. 2 (b c - a d) (3 b c - a d + 2 b d x) \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right] - 2 d (a + b x) (-2 b c + a d - b d x) \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[\frac{e(a+b x)}{c+d x}\right]^2 + 6 b^2 c^2 \operatorname{Log}[c + d x] + 12 b^2 c d x \operatorname{Log}[c + d x] + 6 b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) \right) / \\
 & \left( 4 d (b c - a d)^2 i^3 (c + d x)^2 + \frac{1}{i^3} 2 a^3 A B g^3 \left( \frac{\left(\frac{c}{d} + x\right) \left(2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 4 \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{8 (c + d x)^3 \operatorname{Log}\left[\frac{c}{d} + x\right]} + \frac{1}{2 d} \right. \right. \\
 & \quad \left. \left. \left( \frac{d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{a d}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)} - \left( \frac{d^2 \left(\frac{a}{b} + x\right)^2}{\left(-c + \frac{a d}{b}\right)^4 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)^2} + \frac{2 d \left(\frac{a}{b} + x\right)}{\left(-c + \frac{a d}{b}\right)^3 \left(1 - \frac{d \left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)} \right) \operatorname{Log}\left[\frac{a}{b} + x\right] - \right. \right.
 \end{aligned}$$

$$\begin{aligned} & \left. \frac{\text{Log}\left[1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{ad}{b}}\right]}{\left(-c + \frac{ad}{b}\right)^2} - \frac{-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]}{2d(c+dx)^2} \right) + \frac{1}{i^3} \\ & 6a^2AbBg^3 \left( \frac{1 + \text{Log}\left[\frac{c}{d} + x\right]}{d^2(c+dx)} - \frac{c\left(1 + 2\text{Log}\left[\frac{c}{d} + x\right]\right)}{4d^2(c+dx)^2} + \frac{-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d(c+dx)} - \frac{b\text{Log}[a+bx]}{d(-bc+ad)} + \frac{b\text{Log}[c+dx]}{d(-bc+ad)}}{d} - \right. \\ & \left. \frac{c\left(-\text{Log}\left[\frac{a}{b} + x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\text{Log}[a+bx]-b(c+dx)\text{Log}[c+dx])}{(bc-ad)^2}\right)}{2d^2(c+dx)^2} - \right. \\ & \left. \frac{(c+2dx)\left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right)}{2d^2(c+dx)^2} \right) + \\ & \frac{1}{i^3} 2Ab^3Bg^3 \left( \frac{\left(\frac{a}{b} + x\right)\left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{d^3} - \frac{\left(\frac{c}{d} + x\right)\left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3} + \frac{3c\text{Log}\left[\frac{c}{d} + x\right]^2}{2d^4} + \right. \\ & \frac{3c^2\left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^4(c+dx)} - \frac{c^3\left(1 + 2\text{Log}\left[\frac{c}{d} + x\right]\right)}{4d^4(c+dx)^2} + \frac{3c^2\left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d(c+dx)} - \frac{b\text{Log}[a+bx]}{d(-bc+ad)} + \frac{b\text{Log}[c+dx]}{d(-bc+ad)}\right)}{d^3} - \\ & \frac{c^3\left(-\text{Log}\left[\frac{a}{b} + x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\text{Log}[a+bx]-b(c+dx)\text{Log}[c+dx])}{(bc-ad)^2}\right)}{2d^4(c+dx)^2} - \frac{1}{2d^4} \\ & \left. \left(-2dx + \frac{c^2(5c+6dx)}{(c+dx)^2} + 6c\text{Log}[c+dx]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\ & \left. \left. \text{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right) - \frac{3c\left(\text{Log}\left[\frac{a}{b} + x\right]\text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^4} \right) + \\ & \frac{1}{i^3} 6aAb^2Bg^3 \left( -\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2d^3} - \frac{2c\left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3(c+dx)} + \frac{c^2\left(1 + 2\text{Log}\left[\frac{c}{d} + x\right]\right)}{4d^3(c+dx)^2} - \right. \\ & \frac{2c\left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d(c+dx)} - \frac{b\text{Log}[a+bx]}{d(-bc+ad)} + \frac{b\text{Log}[c+dx]}{d(-bc+ad)}\right)}{d^2} + \\ & \left. \frac{c^2\left(-\text{Log}\left[\frac{a}{b} + x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\text{Log}[a+bx]-b(c+dx)\text{Log}[c+dx])}{(bc-ad)^2}\right)}{2d^3(c+dx)^2} + \frac{1}{2d^3} \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{c(3c+4dx)}{(c+dx)^2} + 2 \operatorname{Log}[c+dx] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) + \\
 & \left. \frac{\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} \right) + \\
 & \frac{1}{i^3} 3 a^2 b B^2 g^3 \left( -\frac{2+2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^2(c+dx)} + \frac{c\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{4 d^2(c+dx)^2} + \right. \\
 & 2 \left( \frac{1+\operatorname{Log}\left[\frac{c}{d}+x\right]}{d^2(c+dx)} - \frac{c\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{4 d^2(c+dx)^2} + \frac{-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)}}{d} - \frac{1}{2 d^2(c+dx)^2} \right. \\
 & \left. c \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \frac{1}{(bc-ad)^2} b(c+dx)(bc-ad+b(c+dx) \operatorname{Log}[a+bx] - \right. \right. \\
 & \left. \left. b(c+dx) \operatorname{Log}[c+dx]) \right) \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right] \right) - \\
 & \frac{(c+2dx)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{ae}{c+dx} + \frac{bex}{c+dx}\right]\right)^2}{2 d^2(c+dx)^2} + \\
 & \left( -d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2 b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \\
 & \left. 2 b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) / (d^2(-bc+ad)(c+dx)) + \\
 & \left( c \left( d(a+bx)(ad-b(2c+dx)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 b^2(c+dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \right. \right. \\
 & \left. \left. 2 b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \left( d(a+bx) + b(c+dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + \right. \right. \\
 & \left. \left. 2 b^2(c+dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / (2 d^2(bc-ad)^2(c+dx)^2) - \\
 & 2 \left( \left( 2(bc-ad) \operatorname{Log}\left[\frac{a}{b}+x\right] \left( 1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b(c+dx) \right. \right. \\
 & \left. \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}[a+bx] - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - \right. \\
 & \left. 2 b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) / (2 d^2(-bc+ad)(c+dx)) + \\
 & \left( c \left( -b(bc-ad)(c+dx) + (bc-ad)^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left( 1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - b^2(c+dx)^2 \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Log}[a + b x] + b^2 (c + d x)^2 \text{Log}[c + d x] + b (c + d x) \left( b (c + d x) \text{Log}\left[\frac{c}{d} + x\right]^2 - \right. \\
 & \left. 2 (b c - a d) \left( 1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - 2 b (c + d x) \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) \Big/ \left( 4 d^2 (b c - a d)^2 (c + d x)^2 \right) \Bigg) + \\
 & \frac{1}{i^3} b^3 B^2 g^3 \left( \frac{(a + b x) \left( 2 - 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2 \right) - \frac{c \text{Log}\left[\frac{c}{d} + x\right]^3}{d^4}}{b d^3} + \right. \\
 & \frac{(c + d x) \left( 2 - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2 \right) - \frac{3 c^2 \left( 2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^4 (c + d x)}}{d^4} + \\
 & \frac{c^3 \left( 1 + 2 \text{Log}\left[\frac{c}{d} + x\right] + 2 \text{Log}\left[\frac{c}{d} + x\right]^2 \right) - \frac{1}{2 d^4} \left( -2 d x + \frac{c^2 (5 c + 6 d x)}{(c + d x)^2} + 6 c \text{Log}[c + d x] \right)}{4 d^4 (c + d x)^2} - \\
 & \frac{1}{2 d^4} \left( -2 d x + \frac{c^2 (5 c + 6 d x)}{(c + d x)^2} + 6 c \text{Log}[c + d x] \right) + \\
 & \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right)^2 + \\
 & \left( 3 c^2 \left( -d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \right. \\
 & \left. \left. 2 b (c + d x) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \Big/ \left( d^4 (-b c + a d) (c + d x) \right) + \\
 & \left( c^3 \left( d (a + b x) (a d - b (2 c + d x)) \text{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c + d x)^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \right. \\
 & \left. \left. 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \left( d (a + b x) + b (c + d x) \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \right. \right. \\
 & \left. \left. 2 b^2 (c + d x)^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \Big/ \\
 & \left( 2 d^4 (b c - a d)^2 (c + d x)^2 + 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right) \right) \\
 & \left( \frac{\left( \frac{a}{b} + x \right) \left( -1 + \text{Log}\left[\frac{a}{b} + x\right] \right)}{d^3} - \frac{\left( \frac{c}{d} + x \right) \left( -1 + \text{Log}\left[\frac{c}{d} + x\right] \right)}{d^3} + \frac{3 c \text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^4} + \right. \\
 & \frac{3 c^2 \left( 1 + \text{Log}\left[\frac{c}{d} + x\right] \right)}{d^4 (c + d x)} - \frac{c^3 \left( 1 + 2 \text{Log}\left[\frac{c}{d} + x\right] \right)}{4 d^4 (c + d x)^2} + \frac{3 c^2 \left( -\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \text{Log}[a + b x]}{d (-b c + a d)} + \frac{b \text{Log}[c + d x]}{d (-b c + a d)} \right)}{d^3} - \\
 & \left. \frac{1}{2 d^4 (c + d x)^2} c^3 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(b c - a d)^2} b (c + d x) (b c - a d + b (c + d x) \text{Log}[a + b x]) - \right. \right.
 \end{aligned}
 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. b (c+d x) \operatorname{Log}[c+d x] \right) - \frac{3 c \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right)}{d^4} \Bigg) - \\
 & \frac{1}{d^4} 3 c \left( \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \right. \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) - \\
 & 2 \left( \frac{1}{b d^4} \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d}+x\right] - b c \operatorname{Log}[c+d x] + \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \\
 & \quad \left. \left( -d(a+b x) + d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] + (b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + (b c-a d) \right. \\
 & \quad \left. \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) + \left( 3 c^2 \left( 2(b c-a d) \operatorname{Log}\left[\frac{a}{b}+x\right] \left( 1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b(c+d x) \right. \right. \\
 & \quad \left. \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}[a+b x] - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \operatorname{Log}[c+d x] \right) - \right. \\
 & \quad \left. \left. 2 b(c+d x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) / \left( 2 d^4 (-b c+a d)(c+d x) \right) + \\
 & \left( c^3 \left( -b(b c-a d)(c+d x) + (b c-a d)^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left( 1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - \right. \right. \\
 & \quad b^2(c+d x)^2 \operatorname{Log}[a+b x] + b^2(c+d x)^2 \operatorname{Log}[c+d x] + \\
 & \quad \left. b(c+d x) \left( b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2(b c-a d) \left( 1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - \right. \right. \\
 & \quad \left. \left. 2 b(c+d x) \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right) \right) / \\
 & \left( 4 d^4 (b c-a d)^2 (c+d x)^2 \right) - \frac{1}{2 d^4} 3 c \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) \right) - \\
 & \left. 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \Bigg) + \\
 & \frac{1}{i^3} 3 a b^2 B^2 g^3 \left( \frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^3}{3 d^3} + \frac{2 c \left( 2 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right)}{d^3 (c+d x)} - \right. \\
 & \quad \frac{c^2 \left( 1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right)}{4 d^3 (c+d x)^2} + \frac{1}{2 d^3} \\
 & \quad \left. \left( \frac{c(3 c+4 d x)}{(c+d x)^2} + 2 \operatorname{Log}[c+d x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right] \right)^2 - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 c \left( -d (a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2 b (c+d x) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 b (c+d x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right) / \left(d^3 (-b c+a d)(c+d x)\right) - \\
 & \left(c^2 \left(d(a+b x)(a d-b(2 c+d x)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - 2 b^2 (c+d x)^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 b (c+d x) \operatorname{Log}\left[\frac{a}{b}+x\right] \left(d(a+b x)+b(c+d x) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right) + \right. \right. \\
 & \quad \left. \left. 2 b^2 (c+d x)^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right) / \\
 & \left(2 d^3 (b c-a d)^2 (c+d x)^2\right) + 2 \left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a e}{c+d x} + \frac{b e x}{c+d x}\right]\right) \\
 & \left(-\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2 d^3} - \frac{2 c\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3(c+d x)} + \frac{c^2\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{4 d^3(c+d x)^2} - \right. \\
 & \quad \left.\frac{2 c\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)} - \frac{b \operatorname{Log}[a+b x]}{d(-b c+a d)} + \frac{b \operatorname{Log}[c+d x]}{d(-b c+a d)}\right)}{d^2} + \frac{1}{2 d^3(c+d x)^2} c^2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \frac{1}{(b c-a d)^2}\right. \right. \\
 & \quad \left. \left. b(c+d x)(b c-a d+b(c+d x) \operatorname{Log}[a+b x]-b(c+d x) \operatorname{Log}[c+d x])\right)\right) + \\
 & \quad \left.\frac{\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^3}\right) + \frac{1}{d^3}\left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \right. \\
 & \quad \left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right) - \\
 & 2\left(-\left(\left(c\left(2(b c-a d) \operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+b(c+d x)\right.\right.\right. \right. \\
 & \quad \left.\left.\left.\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}[a+b x] - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \operatorname{Log}[c+d x]\right) - 2 \right.\right.\right. \right. \\
 & \quad \left.\left.\left.\left. b(c+d x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right)\right) / \left(d^3(-b c+a d)(c+d x)\right)\right) - \\
 & \left(c^2\left(-b(b c-a d)(c+d x)+(b c-a d)^2 \operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right]\right) - \right. \right. \\
 & \quad \left. \left. b^2(c+d x)^2 \operatorname{Log}[a+b x]+b^2(c+d x)^2 \operatorname{Log}[c+d x] + \right. \right. \\
 & \quad \left. \left. b(c+d x)\left(b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2(b c-a d)\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right) - \right.\right. \right.
 \end{aligned}$$

$$\left. \begin{aligned} & 2 b (c+d x) \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] \right) \Bigg) \Bigg) \Bigg) / \\ & \left( 4 d^3 (b c-a d)^2 (c+d x)^2 \right) + \frac{1}{2 d^3} \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] \right) - \right. \\ & \left. 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] + 2 \text{PolyLog} \left[ 3, \frac{b(c+d x)}{b c-a d} \right] \right) \Bigg) \Bigg) \Bigg) \end{aligned}$$

### Problem 101: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^2 \left( A + B \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{(c i + d i x)^3} dx$$

Optimal (type 4, 410 leaves, 11 steps):

$$\begin{aligned} & -\frac{B^2 g^2 (a+b x)^2}{4 d i^3 (c+d x)^2} + \frac{2 A b B g^2 (a+b x)}{d^2 i^3 (c+d x)} - \frac{2 b B^2 g^2 (a+b x)}{d^2 i^3 (c+d x)} + \frac{2 b B^2 g^2 (a+b x) \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right]}{d^2 i^3 (c+d x)} + \\ & \frac{B g^2 (a+b x)^2 \left( A + B \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)}{2 d i^3 (c+d x)^2} - \frac{g^2 (a+b x)^2 \left( A + B \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{2 d i^3 (c+d x)^2} - \\ & \frac{b g^2 (a+b x) \left( A + B \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{d^2 i^3 (c+d x)} - \frac{b^2 g^2 \text{Log} \left[ \frac{-b c-a d}{b(c+d x)} \right] \left( A + B \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right)^2}{d^3 i^3} - \\ & \frac{2 b^2 B g^2 \left( A + B \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right] \right) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{d^3 i^3} + \frac{2 b^2 B^2 g^2 \text{PolyLog} \left[ 3, \frac{d(a+b x)}{b(c+d x)} \right]}{d^3 i^3} \end{aligned}$$

Result (type 4, 3591 leaves):

$$\begin{aligned} & -\frac{A^2 (b^2 c^2 - 2 a b c d + a^2 d^2) g^2}{2 d^3 i^3 (c+d x)^2} - \frac{2 (-A^2 b^2 c g^2 + a A^2 b d g^2)}{d^3 i^3 (c+d x)} + \frac{A^2 b^2 g^2 \text{Log} [c+d x]}{d^3 i^3} + \\ & \left( a^2 B^2 g^2 \left( -7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c+d x)^2 \text{Log} [a+b x] + \right. \right. \\ & \quad \left. \left. 2 (b c-a d) (3 b c-a d+2 b d x) \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right] - 2 d (a+b x) (-2 b c+a d-b d x) \right. \right. \\ & \quad \left. \left. \text{Log} \left[ \frac{e(a+b x)}{c+d x} \right]^2 + 6 b^2 c^2 \text{Log} [c+d x] + 12 b^2 c d x \text{Log} [c+d x] + 6 b^2 d^2 x^2 \text{Log} [c+d x] \right) \right) \Bigg) \Bigg) / \\ & \left( 4 d (b c-a d)^2 i^3 (c+d x)^2 \right) + \frac{1}{i^3} 2 a^2 A B g^2 \left( \frac{\left( \frac{c}{d} + x \right) \left( 2 \text{Log} \left[ \frac{c}{d} + x \right] + 4 \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{8 (c+d x)^3 \text{Log} \left[ \frac{c}{d} + x \right]} + \frac{1}{2 d} \right) \end{aligned}$$

$$\left( \frac{d \left( \frac{a}{b} + x \right)}{\left( -c + \frac{a d}{b} \right)^3 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)} - \left( \frac{d^2 \left( \frac{a}{b} + x \right)^2}{\left( -c + \frac{a d}{b} \right)^4 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)^2} + \frac{2 d \left( \frac{a}{b} + x \right)}{\left( -c + \frac{a d}{b} \right)^3 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)} \right) \text{Log} \left[ \frac{a}{b} + x \right] -$$

$$\frac{\text{Log} \left[ 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right]}{\left( -c + \frac{a d}{b} \right)^2} \right) - \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c+d x} + \frac{b e x}{c+d x} \right]}{2 d (c+d x)^2} \right) + \frac{1}{i^3}$$

$$4 a A b B g^2 \left( \frac{1 + \text{Log} \left[ \frac{c}{d} + x \right]}{d^2 (c+d x)} - \frac{c \left( 1 + 2 \text{Log} \left[ \frac{c}{d} + x \right] \right)}{4 d^2 (c+d x)^2} + \frac{-\frac{\text{Log} \left[ \frac{a+x}{b} \right]}{d (c+d x)} - \frac{b \text{Log} [a+b x]}{d (-b c+a d)} + \frac{b \text{Log} [c+d x]}{d (-b c+a d)}}{d} - \right.$$

$$\frac{c \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \frac{b (c+d x) (b c-a d+b (c+d x) \text{Log} [a+b x]-b (c+d x) \text{Log} [c+d x])}{(b c-a d)^2} \right)}{2 d^2 (c+d x)^2} -$$

$$\left. \frac{(c+2 d x) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right)}{2 d^2 (c+d x)^2} \right) + \frac{1}{i^3}$$

$$2 A b^2 B g^2 \left( -\frac{\text{Log} \left[ \frac{c}{d} + x \right]^2}{2 d^3} - \frac{2 c \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^3 (c+d x)} + \frac{c^2 \left( 1 + 2 \text{Log} \left[ \frac{c}{d} + x \right] \right)}{4 d^3 (c+d x)^2} - \right.$$

$$\frac{2 c \left( -\frac{\text{Log} \left[ \frac{a+x}{b} \right]}{d (c+d x)} - \frac{b \text{Log} [a+b x]}{d (-b c+a d)} + \frac{b \text{Log} [c+d x]}{d (-b c+a d)} \right)}{d^2} +$$

$$\frac{c^2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \frac{b (c+d x) (b c-a d+b (c+d x) \text{Log} [a+b x]-b (c+d x) \text{Log} [c+d x])}{(b c-a d)^2} \right)}{2 d^3 (c+d x)^2} + \frac{1}{2 d^3}$$

$$\left( \frac{c (3 c+4 d x)}{(c+d x)^2} + 2 \text{Log} [c+d x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a e}{c+d x} + \frac{b e x}{c+d x} \right] \right) +$$

$$\left. \frac{\text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c+a d} \right]}{d^3} \right) +$$

$$\frac{1}{i^3} 2 a b B^2 g^2 \left( -\frac{2 + 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2}{d^2 (c+d x)} + \frac{c \left( 1 + 2 \text{Log} \left[ \frac{c}{d} + x \right] + 2 \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{4 d^2 (c+d x)^2} + \right.$$



$$\begin{aligned}
 & 2 \left( \frac{1 + \text{Log}\left[\frac{c}{d} + x\right]}{d^2 (c + d x)} - \frac{c \left(1 + 2 \text{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^2 (c + d x)^2} + \frac{-\frac{\text{Log}\left[\frac{a+x}{b}\right]}{d (c+d x)} - \frac{b \text{Log}[a+b x]}{d (-b c+a d)} + \frac{b \text{Log}[c+d x]}{d (-b c+a d)}}{d} - \frac{1}{2 d^2 (c + d x)^2} \right. \\
 & \left. c \left( -\text{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(b c - a d)^2} b (c + d x) (b c - a d + b (c + d x) \text{Log}[a + b x] - \right. \right. \\
 & \left. \left. b (c + d x) \text{Log}[c + d x]) \right) \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right) - \\
 & \frac{(c + 2 d x) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right)^2}{2 d^2 (c + d x)^2} + \\
 & \left( -d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \\
 & \left. 2 b (c + d x) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) / (d^2 (-b c + a d) (c + d x)) + \\
 & \left( c \left( d (a + b x) (a d - b (2 c + d x)) \text{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c + d x)^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \right. \\
 & \left. \left. 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \left( d (a + b x) + b (c + d x) \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \right. \right. \\
 & \left. \left. 2 b^2 (c + d x)^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) / (2 d^2 (b c - a d)^2 (c + d x)^2) - \\
 & 2 \left( \left( 2 (b c - a d) \text{Log}\left[\frac{a}{b} + x\right] \left( 1 + \text{Log}\left[\frac{c}{d} + x\right] \right) + b (c + d x) \right. \right. \\
 & \left. \left( \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a + b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \text{Log}[c + d x] \right) - \right. \\
 & \left. 2 b (c + d x) \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) / (2 d^2 (-b c + a d) (c + d x)) + \\
 & \left( c \left( -b (b c - a d) (c + d x) + (b c - a d)^2 \text{Log}\left[\frac{a}{b} + x\right] \left( 1 + 2 \text{Log}\left[\frac{c}{d} + x\right] \right) - b^2 (c + d x)^2 \right. \right. \\
 & \left. \left. \text{Log}[a + b x] + b^2 (c + d x)^2 \text{Log}[c + d x] + b (c + d x) \left( b (c + d x) \text{Log}\left[\frac{c}{d} + x\right]^2 - \right. \right. \right. \\
 & \left. \left. 2 (b c - a d) \left( 1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - 2 b (c + d x) \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \right. \right. \\
 & \left. \left. \left. \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) / (4 d^2 (b c - a d)^2 (c + d x)^2) \right) \left. \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{i^3} b^2 B^2 g^2 \left( \frac{\text{Log}\left[\frac{c}{d} + x\right]^3}{3 d^3} + \frac{2 c \left(2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^3 (c + d x)} - \right. \\
 & \frac{c^2 \left(1 + 2 \text{Log}\left[\frac{c}{d} + x\right] + 2 \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{4 d^3 (c + d x)^2} + \frac{1}{2 d^3} \\
 & \left. \left( \frac{c (3 c + 4 d x)}{(c + d x)^2} + 2 \text{Log}[c + d x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right)^2 - \right. \\
 & \left. \left( 2 c \left( -d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \right. \right. \\
 & \left. \left. \left. 2 b (c + d x) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) / \left( d^3 (-b c + a d) (c + d x) \right) - \right. \\
 & \left. \left( c^2 \left( d (a + b x) (a d - b (2 c + d x)) \text{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c + d x)^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \right. \right. \\
 & \left. \left. \left. 2 b (c + d x) \text{Log}\left[\frac{a}{b} + x\right] \left( d (a + b x) + b (c + d x) \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + \right. \right. \right. \\
 & \left. \left. \left. 2 b^2 (c + d x)^2 \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) / \right. \\
 & \left. \left( 2 d^3 (b c - a d)^2 (c + d x)^2 \right) + 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a e}{c + d x} + \frac{b e x}{c + d x}\right] \right) \right. \\
 & \left. \left( -\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^3} - \frac{2 c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + d x)} + \frac{c^2 \left(1 + 2 \text{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^3 (c + d x)^2} - \right. \right. \\
 & \left. \frac{2 c \left( -\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \text{Log}[a + b x]}{d (-b c + a d)} + \frac{b \text{Log}[c + d x]}{d (-b c + a d)} \right)}{d^2} + \frac{1}{2 d^3 (c + d x)^2} c^2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(b c - a d)} \right. \right. \\
 & \left. \left. b (c + d x) (b c - a d + b (c + d x) \text{Log}[a + b x] - b (c + d x) \text{Log}[c + d x]) \right) \right) + \\
 & \left. \frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{d^3} \right) + \frac{1}{d^3} \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \right. \\
 & \left. 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] - 2 \text{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) - \\
 & 2 \left( -\left( \left( c \left( 2 (b c - a d) \text{Log}\left[\frac{a}{b} + x\right] \left( 1 + \text{Log}\left[\frac{c}{d} + x\right] \right) + b (c + d x) \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\left( \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a + b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 2 \text{Log}[c + d x] - 2 b(c + d x) \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) / \left( d^3 (-b c + a d) (c + d x) \right) - \left( c^2 \left( -b(b c - a d)(c + d x) + (b c - a d)^2 \text{Log}\left[\frac{a}{b} + x\right] \left( 1 + 2 \text{Log}\left[\frac{c}{d} + x\right] \right) - b^2 (c + d x)^2 \text{Log}[a + b x] + b^2 (c + d x)^2 \text{Log}[c + d x] + b(c + d x) \left( b(c + d x) \text{Log}\left[\frac{c}{d} + x\right]^2 - 2(b c - a d) \left( 1 + \text{Log}\left[\frac{c}{d} + x\right] \right) - 2 b(c + d x) \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \right) \right) \right) / \left( 4 d^3 (b c - a d)^2 (c + d x)^2 \right) + \frac{1}{2 d^3} \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] \right) - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[3, \frac{b(c + d x)}{b c - a d}\right] \right) \right)$$

**Problem 113: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x) \left( A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 150 leaves, 5 steps):

$$\frac{B i n(c + d x)}{b g^2 (a + b x)} - \frac{i(c + d x) \left( A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{b g^2 (a + b x)} - \frac{d i \left( A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right) \text{Log}\left[ 1 - \frac{b(c + d x)}{d(a + b x)} \right]}{b^2 g^2} + \frac{B d i n \text{PolyLog}\left[ 2, \frac{b(c + d x)}{d(a + b x)} \right]}{b^2 g^2}$$

Result (type 4, 403 leaves):

$$\frac{1}{2 b^2 g^2} i \left( -\frac{2 (b c - a d) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)}{a + b x} + \right. \\ \left. 2 d \operatorname{Log}[a + b x] \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - \left( 2 b B c n \right. \right. \\ \left. \left. \left( -d (a + b x) \operatorname{Log}\left[ \frac{c}{d} + x \right] + d (a + b x) \operatorname{Log}\left[ \frac{d (a+b x)}{-b c + a d} \right] + (b c - a d) \left( 1 + \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right) \right) \right) / \\ \left( (b c - a d) (a + b x) \right) + B d n \left( \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 + \frac{2 a \left( 1 + \operatorname{Log}\left[ \frac{a}{b} + x \right] \right)}{a + b x} + \right. \\ \left. 2 \left( \frac{a}{a + b x} + \operatorname{Log}[a + b x] \right) \left( -\operatorname{Log}\left[ \frac{a}{b} + x \right] + \operatorname{Log}\left[ \frac{c}{d} + x \right] + \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\ \left. \left( 2 a \left( (-b c + a d) \operatorname{Log}\left[ \frac{c}{d} + x \right] + d (a + b x) \left( \operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right) \right) \right) \right) / \\ \left. \left( (b c - a d) (a + b x) \right) - 2 \left( \operatorname{Log}\left[ \frac{c}{d} + x \right] \operatorname{Log}\left[ \frac{d (a+b x)}{-b c + a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) \right)$$

**Problem 114: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 3, 89 leaves, 2 steps):

$$-\frac{B i n (c+d x)^2}{4 (b c - a d) g^3 (a + b x)^2} - \frac{i (c+d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 (b c - a d) g^3 (a + b x)^2}$$

Result (type 3, 216 leaves):

$$\left( i \left( -2 A b^2 c^2 + 2 a^2 A d^2 - b^2 B c^2 n + a^2 B d^2 n - 4 A b^2 c d x + \right. \right. \\ \left. \left. 4 a A b d^2 x - 2 b^2 B c d n x + 2 a b B d^2 n x - 2 B d^2 n (a + b x)^2 \operatorname{Log}[a + b x] - \right. \right. \\ \left. \left. 2 B (b c - a d) (b c + a d + 2 b d x) \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] + 2 a^2 B d^2 n \operatorname{Log}[c + d x] + \right. \right. \\ \left. \left. 4 a b B d^2 n x \operatorname{Log}[c + d x] + 2 b^2 B d^2 n x^2 \operatorname{Log}[c + d x] \right) \right) / \left( 4 b^2 (b c - a d) g^3 (a + b x)^2 \right)$$

**Problem 121: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{a g + b g x} dx$$

Optimal (type 4, 289 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{B d (b c - a d) i^2 n x}{2 b^2 g} + \frac{d (b c - a d) i^2 (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g} + \\
 & \frac{i^2 (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b g} - \frac{B (b c - a d)^2 i^2 n \log \left[ \frac{a+b x}{c+d x} \right]}{2 b^3 g} - \\
 & \frac{3 B (b c - a d)^2 i^2 n \log [c + d x]}{2 b^3 g} - \frac{(b c - a d)^2 i^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} + \\
 & \frac{B (b c - a d)^2 i^2 n \text{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g}
 \end{aligned}$$

Result (type 4, 651 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^3 g} \\
 & i^2 \left( 4 b^2 B c^2 n - 6 a b B c d n + 2 a^2 B d^2 n + 4 A b^2 c d x - 2 a A b d^2 x - b^2 B c d n x + a b B d^2 n x + A b^2 d^2 x^2 + \right. \\
 & B (b c - a d)^2 n \log \left[ \frac{a}{b} + x \right]^2 - 4 b^2 B c^2 n \log \left[ \frac{c}{d} + x \right] + 2 a b B c d n \log \left[ \frac{c}{d} + x \right] + \\
 & 2 A b^2 c^2 \log [a + b x] - 4 a A b c d \log [a + b x] + 2 a^2 A d^2 \log [a + b x] - \\
 & a^2 B d^2 n \log [a + b x] + 2 b^2 B c^2 n \log \left[ \frac{c}{d} + x \right] \log [a + b x] - \\
 & 4 a b B c d n \log \left[ \frac{c}{d} + x \right] \log [a + b x] + 2 a^2 B d^2 n \log \left[ \frac{c}{d} + x \right] \log [a + b x] - \\
 & 2 B n \log \left[ \frac{a}{b} + x \right] \left( a d (-2 b c + a d) + (b c - a d)^2 \log [a + b x] \right) - \\
 & 2 b^2 B c^2 n \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d (a + b x)}{-b c + a d} \right] + 4 a b B c d n \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d (a + b x)}{-b c + a d} \right] - \\
 & 2 a^2 B d^2 n \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d (a + b x)}{-b c + a d} \right] + 4 b^2 B c d x \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - 2 a b B d^2 x \\
 & \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + b^2 B d^2 x^2 \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + 2 b^2 B c^2 \log [a + b x] \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - \\
 & 4 a b B c d \log [a + b x] \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + 2 a^2 B d^2 \log [a + b x] \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + \\
 & \left. b^2 B c^2 n \log [c + d x] - 2 B (b c - a d)^2 n \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right)
 \end{aligned}$$

**Problem 122: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 259 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) i^2 n (c + d x)}{b^2 g^2 (a + b x)} + \frac{d^2 i^2 (a + b x) \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g^2} - \\
 & \frac{(b c - a d) i^2 (c + d x) \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^2 g^2 (a + b x)} - \frac{B d (b c - a d) i^2 n \text{Log}[c + d x]}{b^3 g^2} - \\
 & \frac{2 d (b c - a d) i^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log}\left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^3 g^2} + \frac{2 B d (b c - a d) i^2 n \text{PolyLog}\left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^3 g^2}
 \end{aligned}$$

Result (type 4, 712 leaves):

$$\begin{aligned}
 & \frac{1}{b^3 g^2} i^2 \left( b d^2 x \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - \right. \\
 & \left. \frac{(b c - a d)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right)}{a + b x} + \right. \\
 & \left. 2 d (b c - a d) \text{Log}[a + b x] \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - \left( b^2 B c^2 n \right. \right. \\
 & \left. \left. \left( -d (a + b x) \text{Log}\left[ \frac{c}{d} + x \right] + d (a + b x) \text{Log}\left[ \frac{d (a + b x)}{-b c + a d} \right] + (b c - a d) \left( 1 + \text{Log}\left[ \frac{a + b x}{c + d x} \right] \right) \right) \right) / \right. \\
 & \left. \left( (b c - a d) (a + b x) \right) + b B c d n \left( \text{Log}\left[ \frac{a}{b} + x \right]^2 + \frac{2 a \left( 1 + \text{Log}\left[ \frac{a}{b} + x \right] \right)}{a + b x} + \right. \right. \\
 & \left. \left. 2 \left( \frac{a}{a + b x} + \text{Log}[a + b x] \right) \left( -\text{Log}\left[ \frac{a}{b} + x \right] + \text{Log}\left[ \frac{c}{d} + x \right] + \text{Log}\left[ \frac{a + b x}{c + d x} \right] \right) + \right. \right. \\
 & \left. \left. \left( 2 a \left( (-b c + a d) \text{Log}\left[ \frac{c}{d} + x \right] + d (a + b x) \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right) \right) \right) \right) / \right. \\
 & \left. \left( (b c - a d) (a + b x) \right) - 2 \left( \text{Log}\left[ \frac{c}{d} + x \right] \text{Log}\left[ \frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog}\left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) - \\
 & B d^2 n \left( - (a + b x) \left( -1 + \text{Log}\left[ \frac{a}{b} + x \right] \right) + a \text{Log}\left[ \frac{a}{b} + x \right]^2 + \frac{a^2 \left( 1 + \text{Log}\left[ \frac{a}{b} + x \right] \right)}{a + b x} + \right. \\
 & \left. b \left( \frac{c}{d} + x \right) \left( -1 + \text{Log}\left[ \frac{c}{d} + x \right] \right) - \right. \\
 & \left. \left( b x - \frac{a^2}{a + b x} - 2 a \text{Log}[a + b x] \right) \left( -\text{Log}\left[ \frac{a}{b} + x \right] + \text{Log}\left[ \frac{c}{d} + x \right] + \text{Log}\left[ \frac{a + b x}{c + d x} \right] \right) + \right. \\
 & \left. \left( a^2 \left( (-b c + a d) \text{Log}\left[ \frac{c}{d} + x \right] + d (a + b x) \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right) \right) \right) \right) / \right. \\
 & \left. \left( (b c - a d) (a + b x) \right) - 2 a \left( \text{Log}\left[ \frac{c}{d} + x \right] \text{Log}\left[ \frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog}\left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \right) \right)
 \end{aligned}$$

**Problem 123: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 4, 242 leaves, 7 steps):

$$\begin{aligned} & - \frac{B d i^2 n (c + d x)}{b^2 g^3 (a + b x)} - \frac{B i^2 n (c + d x)^2}{4 b g^3 (a + b x)^2} - \\ & \frac{d i^2 (c + d x) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^2 g^3 (a + b x)} - \frac{i^2 (c + d x)^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b g^3 (a + b x)^2} - \\ & \frac{d^2 i^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g^3} + \frac{B d^2 i^2 n \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g^3} \end{aligned}$$

Result (type 4, 903 leaves):

$$\frac{1}{4 b^3 g^3} i^2 \left( - \left( \left( b^2 B c^2 n \left( b^2 c^2 - 4 a b c d + a^2 d^2 - 2 b^2 c d x - 2 a b d^2 x - 2 b^2 d^2 x^2 + 2 d^2 (a+b x)^2 \log\left[\frac{c}{d} + x\right] - 2 d^2 (a+b x)^2 \log\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 b^2 c^2 \log\left[\frac{a+b x}{c+d x}\right] - 4 a b c d \log\left[\frac{a+b x}{c+d x}\right] + 2 a^2 d^2 \log\left[\frac{a+b x}{c+d x}\right] \right) \right) / \left( (b c - a d)^2 (a+b x)^2 \right) - \frac{2 (b c - a d)^2 \left( A + B \log\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \log\left[\frac{a+b x}{c+d x}\right] \right)}{(a+b x)^2} + \frac{8 d (-b c + a d) \left( A + B \log\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \log\left[\frac{a+b x}{c+d x}\right] \right)}{a+b x} - 4 d^2 \log[a+b x] \left( A + B \log\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \log\left[\frac{a+b x}{c+d x}\right] \right) - \frac{1}{(b c - a d)^2 (a+b x)^2} 2 b B c d n \left( 3 a b^2 c^2 - 4 a^2 b c d + a^3 d^2 + 4 b^3 c^2 x - 6 a b^2 c d x + 2 a^2 b d^2 x - 2 d (-2 b c + a d) (a+b x)^2 \log[a+b x] + 2 (b c - a d)^2 (a+2 b x) \log\left[\frac{a+b x}{c+d x}\right] - 4 a^2 b c d \log[c+d x] + 2 a^3 d^2 \log[c+d x] - 8 a b^2 c d x \log[c+d x] + 4 a^2 b d^2 x \log[c+d x] - 4 b^3 c d x^2 \log[c+d x] + 2 a b^2 d^2 x^2 \log[c+d x] \right) + B d^2 n \left( 2 \log\left[\frac{a}{b} + x\right]^2 + \frac{8 a \left( 1 + \log\left[\frac{a}{b} + x\right] \right)}{a+b x} - \frac{a^2 \left( 1 + 2 \log\left[\frac{a}{b} + x\right] \right)}{(a+b x)^2} + 2 \left( \frac{a (3 a + 4 b x)}{(a+b x)^2} + 2 \log[a+b x] \right) \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{a+b x}{c+d x}\right] \right) + \left( 8 a \left( (-b c + a d) \log\left[\frac{c}{d} + x\right] + d (a+b x) (\log[a+b x] - \log[c+d x]) \right) \right) / \left( (b c - a d) (a+b x) \right) + \frac{1}{(a+b x)^2} 2 a^2 \left( \log\left[\frac{c}{d} + x\right] + \frac{1}{(b c - a d)^2} d (a+b x) (b c - a d + d (a+b x) \log[a+b x] - d (a+b x) \log[c+d x]) \right) - 4 \left( \log\left[\frac{c}{d} + x\right] \log\left[\frac{d(a+b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) \right)$$

**Problem 124: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^2 \left( A + B \log\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \right)}{(a g + b g x)^4} dx$$



Optimal (type 3, 93 leaves, 2 steps):

$$-\frac{B i^2 n (c+d x)^3}{9 (b c-a d) g^4 (a+b x)^3} - \frac{i^2 (c+d x)^3 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{3 (b c-a d) g^4 (a+b x)^3}$$

Result (type 3, 329 leaves):

$$\frac{1}{9 b^3 (b c-a d) g^4 (a+b x)^3} i^2 \left( -3 A b^3 c^3 + 3 a^3 A d^3 - b^3 B c^3 n + a^3 B d^3 n - 9 A b^3 c^2 d x + 9 a^2 A b d^3 x - 3 b^3 B c^2 d n x + 3 a^2 b B d^3 n x - 9 A b^3 c d^2 x^2 + 9 a A b^2 d^3 x^2 - 3 b^3 B c d^2 n x^2 + 3 a b^2 B d^3 n x^2 - 3 B d^3 n (a+b x)^3 \operatorname{Log}[a+b x] - 3 B (b c-a d) (a^2 d^2 + a b d (c+3 d x) + b^2 (c^2 + 3 c d x + 3 d^2 x^2)) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 3 a^3 B d^3 n \operatorname{Log}[c+d x] + 9 a^2 b B d^3 n x \operatorname{Log}[c+d x] + 9 a b^2 B d^3 n x^2 \operatorname{Log}[c+d x] + 3 b^3 B d^3 n x^3 \operatorname{Log}[c+d x] \right)$$

**Problem 131: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i+d i x)^3 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{a g+b g x} dx$$

Optimal (type 4, 373 leaves, 14 steps):

$$\begin{aligned} & -\frac{5 B d (b c-a d)^2 i^3 n x}{6 b^3 g} - \frac{B (b c-a d) i^3 n (c+d x)^2}{6 b^2 g} + \\ & \frac{d (b c-a d)^2 i^3 (a+b x) (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{b^4 g} + \\ & \frac{(b c-a d) i^3 (c+d x)^2 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{2 b^2 g} + \frac{i^3 (c+d x)^3 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{3 b g} - \\ & \frac{5 B (b c-a d)^3 i^3 n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{6 b^4 g} - \frac{11 B (b c-a d)^3 i^3 n \operatorname{Log}[c+d x]}{6 b^4 g} - \\ & \frac{(b c-a d)^3 i^3 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]) \operatorname{Log}\left[1-\frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g} + \frac{B (b c-a d)^3 i^3 n \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right]}{b^4 g} \end{aligned}$$

Result (type 4, 1061 leaves):

$$\begin{aligned} & \frac{1}{6 b^4 g} i^3 \left( 18 b^3 B c^3 n - 36 a b^2 B c^2 d n + 24 a^2 b B c d^2 n - 6 a^3 B d^3 n + 18 A b^3 c^2 d x - \right. \\ & 18 a A b^2 c d^2 x + 6 a^2 A b d^3 x - 7 b^3 B c^2 d n x + 12 a b^2 B c d^2 n x - 5 a^2 b B d^3 n x + 9 A b^3 c d^2 x^2 - \\ & 3 a A b^2 d^3 x^2 - b^3 B c d^2 n x^2 + a b^2 B d^3 n x^2 + 2 A b^3 d^3 x^3 + 3 B (b c - a d)^3 n \text{Log}\left[\frac{a}{b} + x\right]^2 - \\ & 18 b^3 B c^3 n \text{Log}\left[\frac{c}{d} + x\right] + 18 a b^2 B c^2 d n \text{Log}\left[\frac{c}{d} + x\right] - 6 a^2 b B c d^2 n \text{Log}\left[\frac{c}{d} + x\right] + \\ & 6 A b^3 c^3 \text{Log}[a + b x] - 18 a A b^2 c^2 d \text{Log}[a + b x] + 18 a^2 A b c d^2 \text{Log}[a + b x] - \\ & 6 a^3 A d^3 \text{Log}[a + b x] - 9 a^2 b B c d^2 n \text{Log}[a + b x] + 5 a^3 B d^3 n \text{Log}[a + b x] + \\ & 6 b^3 B c^3 n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 18 a b^2 B c^2 d n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + \\ & 18 a^2 b B c d^2 n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 6 a^3 B d^3 n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + \\ & 6 B n \text{Log}\left[\frac{a}{b} + x\right] \left( a d (3 b^2 c^2 - 3 a b c d + a^2 d^2) - (b c - a d)^3 \text{Log}[a + b x] \right) - \\ & 6 b^3 B c^3 n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 18 a b^2 B c^2 d n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\ & 18 a^2 b B c d^2 n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 6 a^3 B d^3 n \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\ & 18 b^3 B c^2 d x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 18 a b^2 B c d^2 x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\ & 6 a^2 b B d^3 x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 9 b^3 B c d^2 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 a b^2 B d^3 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\ & 2 b^3 B d^3 x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 b^3 B c^3 \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\ & 18 a b^2 B c^2 d \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 18 a^2 b B c d^2 \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\ & 6 a^3 B d^3 \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 7 b^3 B c^3 n \text{Log}[c + d x] - \\ & 3 a b^2 B c^2 d n \text{Log}[c + d x] - 6 B (b c - a d)^3 n \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \Big) \end{aligned}$$

**Problem 132: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^3 \left( A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(a g + b g x)^2} dx$$

Optimal (type 4, 390 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{B d^2 (b c - a d) i^3 n x}{2 b^3 g^2} - \frac{B (b c - a d)^2 i^3 n (c + d x)}{b^3 g^2 (a + b x)} + \\
 & \frac{2 d^2 (b c - a d) i^3 (a + b x) \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^4 g^2} - \frac{(b c - a d)^2 i^3 (c + d x) \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g^2 (a + b x)} + \\
 & \frac{d i^3 (c + d x)^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^2 g^2} - \frac{B d (b c - a d)^2 i^3 n \text{Log} \left[ \frac{a+b x}{c+d x} \right]}{2 b^4 g^2} - \\
 & \frac{5 B d (b c - a d)^2 i^3 n \text{Log} [c + d x]}{2 b^4 g^2} - \frac{3 d (b c - a d)^2 i^3 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g^2} + \\
 & \frac{3 B d (b c - a d)^2 i^3 n \text{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g^2}
 \end{aligned}$$

Result (type 4, 1120 leaves):

$$\begin{aligned}
 & \frac{1}{2 b^4 g^2} i^3 \left( 2 b d^2 (3 b c - 2 a d) x \left( A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \right. \\
 & b^2 d^3 x^2 \left( A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) - \\
 & \left. \frac{2 (b c - a d)^3 \left( A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)}{a+b x} + \right. \\
 & 6 d (b c - a d)^2 \operatorname{Log}[a+b x] \left( A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) - \left( 2 b^3 B c^3 n \right. \\
 & \left. \left( -d (a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + (b c - a d) \left( 1 + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) \right) / \\
 & \left( (b c - a d) (a+b x) \right) + B d^3 n \left( 4 a^2 - \frac{4 a b c}{d} + a b x - \frac{b^2 c x}{d} + \frac{2 a^3}{a+b x} + 3 a^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \right. \\
 & \frac{4 a b c \operatorname{Log}\left[\frac{c}{d}+x\right]}{d} - a^2 \operatorname{Log}[a+b x] + \frac{2 a^3 d \operatorname{Log}[a+b x]}{b c - a d} + 6 a^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - \\
 & 2 a^2 \operatorname{Log}\left[\frac{a}{b}+x\right] (2 + 3 \operatorname{Log}[a+b x]) - 6 a^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 4 a b x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \\
 & b^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \frac{2 a^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]}{a+b x} + 6 a^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \frac{b^2 c^2 \operatorname{Log}[c+d x]}{d^2} + \\
 & \left. \frac{2 a^3 d \operatorname{Log}[c+d x]}{-b c+a d} - 6 a^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) + 3 b^2 B c^2 d n \left( \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \right. \\
 & \frac{2 a \left( 1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right)}{a+b x} + 2 \left( \frac{a}{a+b x} + \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \\
 & \left. \left( 2 a \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x]) \right) \right) \right) / \\
 & \left( (b c - a d) (a+b x) \right) - 2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) - \\
 & 6 b B c d^2 n \left( - (a+b x) \left( -1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) + a \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \frac{a^2 \left( 1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right)}{a+b x} + \right. \\
 & b \left( \frac{c}{d}+x \right) \left( -1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - \\
 & \left( b x - \frac{a^2}{a+b x} - 2 a \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \\
 & \left. \left( a^2 \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d (a+b x) (\operatorname{Log}[a+b x] - \operatorname{Log}[c+d x]) \right) \right) \right) / \\
 & \left( (b c - a d) (a+b x) \right) - 2 a \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) \right)
 \end{aligned}$$

### Problem 133: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(a g + b g x)^3} dx$$

Optimal (type 4, 361 leaves, 9 steps):

$$\begin{aligned} & - \frac{2 B d (b c - a d) i^3 n (c + d x)}{b^3 g^3 (a + b x)} - \frac{B (b c - a d) i^3 n (c + d x)^2}{4 b^2 g^3 (a + b x)^2} + \frac{d^3 i^3 (a + b x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^4 g^3} \\ & - \frac{2 d (b c - a d) i^3 (c + d x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g^3 (a + b x)} - \frac{(b c - a d) i^3 (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^2 g^3 (a + b x)^2} \\ & - \frac{B d^2 (b c - a d) i^3 n \operatorname{Log}[c + d x]}{b^4 g^3} - \frac{3 d^2 (b c - a d) i^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^3} + \\ & - \frac{3 B d^2 (b c - a d) i^3 n \operatorname{PolyLog}\left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^3} \end{aligned}$$

Result (type 4, 1324 leaves):

$$\begin{aligned} & \frac{1}{4 b^4 g^3} \\ & i^3 \left( - \left( \left( b^3 B c^3 n \left( b^2 c^2 - 4 a b c d + a^2 d^2 - 2 b^2 c d x - 2 a b d^2 x - 2 b^2 d^2 x^2 + 2 d^2 (a + b x)^2 \operatorname{Log}\left[ \frac{c}{d} + x \right] - \right. \right. \right. \right. \\ & \quad \left. \left. \left. 2 d^2 (a + b x)^2 \operatorname{Log}\left[ \frac{d(a + b x)}{-b c + a d} \right] + 2 b^2 c^2 \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] - \right. \right. \right. \\ & \quad \left. \left. \left. 4 a b c d \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] + 2 a^2 d^2 \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] \right) \right) / \left( (b c - a d)^2 (a + b x)^2 \right) + \\ & \quad 4 b d^3 x \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] \right) - \\ & \quad \frac{2 (b c - a d)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)}{(a + b x)^2} - \\ & \quad \frac{12 d (b c - a d)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)}{a + b x} + \\ & \quad 12 d^2 (b c - a d) \operatorname{Log}[a + b x] \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] \right) - \\ & \quad \frac{1}{(b c - a d)^2 (a + b x)^2} 3 b^2 B c^2 d n \left( 3 a b^2 c^2 - 4 a^2 b c d + a^3 d^2 + 4 b^3 c^2 x - 6 a b^2 c d x + 2 a^2 b d^2 x - \right. \\ & \quad \left. 2 d (-2 b c + a d) (a + b x)^2 \operatorname{Log}[a + b x] + 2 (b c - a d)^2 (a + 2 b x) \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] - \right. \\ & \quad \left. 4 a^2 b c d \operatorname{Log}[c + d x] + 2 a^3 d^2 \operatorname{Log}[c + d x] - 8 a b^2 c d x \operatorname{Log}[c + d x] + \right. \\ & \quad \left. 4 a^2 b d^2 x \operatorname{Log}[c + d x] - 4 b^3 c d x^2 \operatorname{Log}[c + d x] + 2 a b^2 d^2 x^2 \operatorname{Log}[c + d x] \right) + \end{aligned}$$

$$\begin{aligned}
 & 3 b B c d^2 n \left( 2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \frac{8 a\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{a+b x} - \frac{a^2\left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{(a+b x)^2} + \right. \\
 & 2 \left( \frac{a\left(3 a+4 b x\right)}{(a+b x)^2} + 2 \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \\
 & \left( 8 a\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right) \right) / \\
 & \left( (b c-a d)(a+b x) + \frac{1}{(a+b x)^2} 2 a^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{1}{(b c-a d)^2} \right. \right. \\
 & \left. \left. d(a+b x)(b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x]) \right) \right) - \\
 & 4 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \left. \right) - \\
 & B d^3 n \left( -4(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right) + 6 a \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \frac{12 a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{a+b x} - \right. \\
 & \frac{a^3\left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{(a+b x)^2} + 4 b\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right) + \\
 & 2 \left( -2 b x + \frac{a^2(5 a+6 b x)}{(a+b x)^2} + 6 a \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \\
 & \left( 12 a^2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right) \right) / \\
 & \left( (b c-a d)(a+b x) + \frac{1}{(a+b x)^2} 2 a^3 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{1}{(b c-a d)^2} \right. \right. \\
 & \left. \left. d(a+b x)(b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x]) \right) \right) - \\
 & 12 a \left( \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \left. \right) \left. \right)
 \end{aligned}$$

**Problem 134: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i+d i x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(a g+b g x)^4} d x$$

Optimal (type 4, 326 leaves, 9 steps):

$$\frac{B d^2 i^3 n (c+d x)}{b^3 g^4 (a+b x)} - \frac{B d i^3 n (c+d x)^2}{4 b^2 g^4 (a+b x)^2} - \frac{B i^3 n (c+d x)^3}{9 b g^4 (a+b x)^3} - \frac{d^2 i^3 (c+d x) \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g^4 (a+b x)}$$

$$\frac{d i^3 (c+d x)^2 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^2 g^4 (a+b x)^2} - \frac{i^3 (c+d x)^3 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b g^4 (a+b x)^3}$$

$$\frac{d^3 i^3 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log\left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^4} + \frac{B d^3 i^3 n \text{PolyLog}\left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^4}$$

Result(type 4, 2243 leaves):

$$\frac{d^3 i^3 \log[a+b x] \left( A+B \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right)}{b^4 g^4} + \frac{1}{b^4 g^4 (a+b x)}$$

$$3 \left( -A b c d^2 i^3 + a A d^3 i^3 - b B c d^2 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + \right.$$

$$\left. a B d^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right) - \frac{1}{2 b^4 g^4 (a+b x)^2}$$

$$3 \left( A b^2 c^2 d i^3 - 2 a A b c d^2 i^3 + a^2 A d^3 i^3 + b^2 B c^2 d i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) - 2 a b \right.$$

$$\left. B c d^2 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + a^2 B d^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right) +$$

$$\frac{1}{3 b^4 g^4 (a+b x)^3} \left( -A b^3 c^3 i^3 + 3 a A b^2 c^2 d i^3 - 3 a^2 A b c d^2 i^3 + a^3 A d^3 i^3 - \right.$$

$$\left. b^3 B c^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + \right.$$

$$\left. 3 a b^2 B c^2 d i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) - 3 a^2 b B c d^2 i^3 \right.$$

$$\left. \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + a^3 B d^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right) +$$

$$\frac{1}{g^4} B c^3 i^3 n \left( - \frac{\left( \frac{a}{b} + x \right) \left( 3 \log\left[ \frac{a}{b} + x \right] + 9 \log\left[ \frac{a}{b} + x \right]^2 \right)}{27 (a+b x)^4 \log\left[ \frac{a}{b} + x \right]} - \frac{1}{6 b} \right.$$

$$\left( - \frac{b^2 \left( \frac{c}{d} + x \right)^2}{\left( -a + \frac{b c}{d} \right)^5 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^2} - \frac{4 b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^4 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} + \right.$$

$$\left. \left( \frac{2 b^3 \left( \frac{c}{d} + x \right)^3}{\left( -a + \frac{b c}{d} \right)^6 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^3} + \frac{6 b^2 \left( \frac{c}{d} + x \right)^2}{\left( -a + \frac{b c}{d} \right)^5 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^2} + \frac{6 b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^4 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} \right) \log\left[ \frac{c}{d} + x \right] +$$

$$\left. \frac{2 \operatorname{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right]}{\left(-a + \frac{bc}{d}\right)^3} - \frac{-\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right]}{3 b (a + b x)^3} \right) +$$

$$\frac{1}{g^4} 3 B c^2 d i^3 n \left( -\frac{1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{4 b^2 (a + b x)^2} + \frac{a \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^2 (a + b x)^3} +
 \right.$$

$$\frac{a \left( -\frac{2 \operatorname{Log}\left[\frac{c+x}{d}\right]}{(a+bx)^3} + \frac{d \left( \frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2d^2 \operatorname{Log}[a+bx] - 2d^2 \operatorname{Log}[c+dx] \right)}{(bc-ad)^3} \right)}{6 b^2} +$$

$$\frac{\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2}}{2 b^2 (a + b x)^2} -$$

$$\left. \frac{(a + 3 b x) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)}{6 b^2 (a + b x)^3} \right) + \frac{1}{g^4}$$

$$3 B c d^2 i^3 n \left( -\frac{1 + \operatorname{Log}\left[\frac{a}{b} + x\right]}{b^3 (a + b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{2 b^3 (a + b x)^2} - \frac{a^2 \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^3 (a + b x)^3} -
 \right.$$

$$\frac{(-bc + ad) \operatorname{Log}\left[\frac{c}{d} + x\right] + d(a + b x) \left( \operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right)}{b^3 (bc - ad) (a + b x)} -$$

$$\frac{a^2 \left( -\frac{2 \operatorname{Log}\left[\frac{c+x}{d}\right]}{(a+bx)^3} + \frac{d \left( \frac{(bc-ad)(-bc+3ad+2bdx)}{(a+bx)^2} + 2d^2 \operatorname{Log}[a+bx] - 2d^2 \operatorname{Log}[c+dx] \right)}{(bc-ad)^3} \right)}{6 b^3} -$$

$$\frac{a \left( \operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx)\operatorname{Log}[a+bx]-d(a+bx)\operatorname{Log}[c+dx])}{(bc-ad)^2} \right)}{b^3 (a + b x)^2} - \frac{1}{3 b^3 (a + b x)^3}$$

$$\left. \frac{(a^2 + 3 a b x + 3 b^2 x^2) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)}{3 b^3 (a + b x)^3} \right) +$$



$$\frac{1}{g^4} B d^3 i^3 n \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} + \frac{3 a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} - \frac{3 a^2 \left(1 + 2 \text{Log}\left[\frac{a}{b} + x\right]\right)}{4 b^4 (a + b x)^2} + \frac{a^3 \left(1 + 3 \text{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^4 (a + b x)^3} + \right.$$

$$\left. \left( 3 a \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) / \right.$$

$$\left. a^3 \left( -\frac{2 \text{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{d \left( \frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \text{Log}[a + b x] - 2 d^2 \text{Log}[c + d x] \right)}{(b c - a d)^3} \right) \right.$$

$$\left. \frac{(b^4 (b c - a d) (a + b x)) + \frac{3 a^2 \left( \text{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \text{Log}[a + b x] - d (a + b x) \text{Log}[c + d x])}{(b c - a d)^2} \right)}{2 b^4 (a + b x)^2} + \frac{1}{6 b^4}}{6 b^4} + \right.$$

$$\left. \left( \frac{a (11 a^2 + 27 a b x + 18 b^2 x^2)}{(a + b x)^3} + 6 \text{Log}[a + b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \right.$$

$$\left. \left. \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) - \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^4} \right)$$

### Problem 135: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x)^3 \left( A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{c i + d i x} dx$$

Optimal (type 4, 269 leaves, 6 steps):

$$\frac{g^3 (a + b x)^3 \left( A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{3 d i} - \frac{(b c - a d) g^3 (a + b x)^2 \left( 3 A + B n + 3 B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{6 d^2 i} +$$

$$\frac{(b c - a d)^2 g^3 (a + b x) \left( 6 A + 5 B n + 6 B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{6 d^3 i} +$$

$$\frac{(b c - a d)^3 g^3 \left( 6 A + 11 B n + 6 B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right) \text{Log}\left[ \frac{b c - a d}{b (c + d x)} \right]}{6 d^4 i} +$$

$$\frac{B (b c - a d)^3 g^3 n \text{PolyLog}\left[ 2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^4 i}$$

Result (type 4, 1003 leaves):

$$\begin{aligned} & \frac{1}{6 d^4 i} g^3 \left( 6 b^3 B c^3 n - 24 a b^2 B c^2 d n + 36 a^2 b B c d^2 n - 18 a^3 B d^3 n + 6 A b^3 c^2 d x - 18 a A b^2 c d^2 x + \right. \\ & 18 a^2 A b d^3 x + 5 b^3 B c^2 d n x - 12 a b^2 B c d^2 n x + 7 a^2 b B d^3 n x - 3 A b^3 c d^2 x^2 + 9 a A b^2 d^3 x^2 - \\ & b^3 B c d^2 n x^2 + a b^2 B d^3 n x^2 + 2 A b^3 d^3 x^3 - 6 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] + 18 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right] - \\ & 18 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] + 3 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 9 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \\ & 9 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 3 a^3 B d^3 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 3 a^2 b B c d^2 n \operatorname{Log}[a + b x] - \\ & 7 a^3 B d^3 n \operatorname{Log}[a + b x] + 6 b^3 B c^2 d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 18 a b^2 B c d^2 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\ & 18 a^2 b B d^3 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 b^3 B c d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\ & 9 a b^2 B d^3 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 b^3 B d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 A b^3 c^3 \operatorname{Log}[c + d x] + \\ & 18 a A b^2 c^2 d \operatorname{Log}[c + d x] - 18 a^2 A b c d^2 \operatorname{Log}[c + d x] + 6 a^3 A d^3 \operatorname{Log}[c + d x] - \\ & 5 b^3 B c^3 n \operatorname{Log}[c + d x] + 9 a b^2 B c^2 d n \operatorname{Log}[c + d x] - 6 b^3 B c^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\ & 18 a b^2 B c^2 d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 18 a^2 b B c d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\ & 6 a^3 B d^3 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 6 b^3 B c^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + \\ & 18 a b^2 B c^2 d \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 18 a^2 b B c d^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + \\ & 6 a^3 B d^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 6 B n \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \\ & \left. \left( -a d (b^2 c^2 - 3 a b c d + 3 a^2 d^2) - (b c - a d)^3 \operatorname{Log}[c + d x] + (b c - a d)^3 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) - \right. \\ & \left. 6 B (b c - a d)^3 n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right) \end{aligned}$$

**Problem 136: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{c i + d i x} dx$$

Optimal (type 4, 211 leaves, 5 steps):

$$\begin{aligned} & \frac{g^2 (a + b x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{2 d i} - \frac{(b c - a d) g^2 (a + b x) (2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])}{2 d^2 i} - \\ & \frac{(b c - a d)^2 g^2 (2 A + 3 B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]) \operatorname{Log}\left[\frac{b c - a d}{b(c + d x)}\right]}{2 d^3 i} - \\ & \frac{B (b c - a d)^2 g^2 n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)}\right]}{d^3 i} \end{aligned}$$

Result (type 4, 610 leaves):

$$\frac{1}{2 d^3 i} g^2 \left( -2 b^2 B c^2 n + 6 a b B c d n - 4 a^2 B d^2 n - 2 A b^2 c d x + 4 a A b d^2 x - b^2 B c d n x + a b B d^2 n x + A b^2 d^2 x^2 + 2 b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] - 4 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right] - b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a^2 B d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - a^2 B d^2 n \operatorname{Log}[a + b x] - 2 b^2 B c d x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 4 a b B d^2 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + b^2 B d^2 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 A b^2 c^2 \operatorname{Log}[c + d x] - 4 a A b c d \operatorname{Log}[c + d x] + 2 a^2 A d^2 \operatorname{Log}[c + d x] + b^2 B c^2 n \operatorname{Log}[c + d x] + 2 b^2 B c^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 4 a b B c d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 a^2 B d^2 n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + 2 b^2 B c^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 4 a b B c d \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] + 2 a^2 B d^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \operatorname{Log}[c + d x] - 2 B n \operatorname{Log}\left[\frac{a}{b} + x\right] \left( a d (b c - 2 a d) + (b c - a d)^2 \operatorname{Log}[c + d x] - (b c - a d)^2 \operatorname{Log}\left[\frac{b(c + d x)}{b c - a d}\right] \right) + 2 B (b c - a d)^2 n \operatorname{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] \right)$$

**Problem 137: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{c i + d i x} dx$$

Optimal (type 4, 134 leaves, 4 steps):

$$\frac{g(a + b x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{d i} + \frac{(b c - a d) g \left( A + B n + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{b c - a d}{b(c + d x)} \right]}{d^2 i} + \frac{B (b c - a d) g n \operatorname{PolyLog}\left[ 2, \frac{d(a + b x)}{b(c + d x)} \right]}{d^2 i}$$

Result (type 4, 308 leaves):

$$\begin{aligned} & \frac{1}{2 d^2 i} g \left( 2 b B c n - 2 a B d n + 2 A b d x - 2 b B c n \operatorname{Log}\left[\frac{c}{d} + x\right] + b B c n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \right. \\ & \quad a B d n \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 b B d x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 2 A b c \operatorname{Log}[c+d x] + \\ & \quad 2 a A d \operatorname{Log}[c+d x] - 2 b B c n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] + 2 a B d n \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c+d x] - \\ & \quad 2 b B c \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + 2 a B d \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\ & \quad \left. 2 B n \operatorname{Log}\left[\frac{a}{b} + x\right] \left( a d + (b c - a d) \operatorname{Log}[c+d x] + (-b c + a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + \right. \\ & \quad \left. 2 B (-b c + a d) n \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \end{aligned}$$

**Problem 143: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 (A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{(c i + d i x)^2} dx$$

Optimal (type 4, 359 leaves, 9 steps):

$$\begin{aligned} & \frac{3 B (b c - a d)^2 g^3 n (a + b x)}{d^3 i^2 (c + d x)} - \frac{(b c - a d)^2 g^3 (6 A + 5 B n) (a + b x)}{2 d^3 i^2 (c + d x)} - \\ & \frac{3 B (b c - a d)^2 g^3 (a + b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d^3 i^2 (c + d x)} + \frac{g^3 (a + b x)^3 (A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{2 d i^2 (c + d x)} - \\ & \frac{(b c - a d) g^3 (a + b x)^2 (3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{2 d^2 i^2 (c + d x)} - \\ & \frac{b (b c - a d)^2 g^3 (6 A + 5 B n + 6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right]}{2 d^4 i^2} - \\ & \frac{3 b B (b c - a d)^2 g^3 n \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{d^4 i^2} \end{aligned}$$

Result (type 4, 1109 leaves):

$$\begin{aligned}
 & \frac{1}{2 d^4 i^2} g^3 \left( -2 b^2 d (2 b c - 3 a d) x \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\
 & \quad b^3 d^2 x^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + \\
 & \quad \left. \frac{2 (b c - a d)^3 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)}{c+d x} + \right. \\
 & \quad 6 b (b c - a d)^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] + \\
 & \quad \left( 2 a^3 B d^3 n \left( b c - a d + b (c+d x) \operatorname{Log} \left[ \frac{a}{b} + x \right] + (-b c + a d) \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] - \right. \right. \\
 & \quad \left. \left. b c \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] - b d x \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) \right) / \\
 & \quad \left( (b c - a d) (c+d x) \right) + 3 a^2 b B d^2 n \left( -\operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] + \right. \\
 & \quad \left. 2 \left( -\frac{c}{c+d x} + \frac{b c \operatorname{Log} [a+b x]}{-b c + a d} + \frac{b c \operatorname{Log} [c+d x]}{b c - a d} - \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [c+d x] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right. \right. \\
 & \quad \left. \left. \left( \frac{c}{c+d x} + \operatorname{Log} [c+d x] \right) + \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) + 2 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) + \\
 & \quad b^3 B n \left( -4 c^2 + \frac{4 a c d}{b} - c d x + \frac{a d^2 x}{b} - \frac{2 c^3}{c+d x} + 4 c^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] - 3 c^2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - \right. \\
 & \quad \frac{a^2 d^2 \operatorname{Log} [a+b x]}{b^2} + \frac{2 b c^3 \operatorname{Log} [a+b x]}{-b c + a d} - 4 c d x \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] + d^2 x^2 \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] + \\
 & \quad \frac{2 c^3 \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right]}{c+d x} + c^2 \operatorname{Log} [c+d x] + \frac{2 b c^3 \operatorname{Log} [c+d x]}{b c - a d} + 6 c^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] + 6 c^2 \\
 & \quad \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \operatorname{Log} [c+d x] - \frac{2 c \operatorname{Log} \left[ \frac{a}{b} + x \right] \left( 2 a d + 3 b c \operatorname{Log} [c+d x] - 3 b c \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right)}{b} \right) + \\
 & \quad \left. 6 c^2 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) + \\
 & \quad 6 a b^2 B d n \left( d \left( \frac{a}{b} + x \right) \left( -1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right) - (c+d x) \left( -1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right) + c \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + \right. \\
 & \quad \frac{c^2 \left( 1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{c+d x} + c^2 \left( -\frac{\operatorname{Log} \left[ \frac{a}{b} + x \right]}{c+d x} + \frac{b \left( \operatorname{Log} [a+b x] - \operatorname{Log} [c+d x] \right)}{b c - a d} \right) \right) + \\
 & \quad \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \left( d x - \frac{c^2}{c+d x} - 2 c \operatorname{Log} [c+d x] \right) - \\
 & \quad \left. 2 c \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \right)
 \end{aligned}$$

**Problem 144: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 275 leaves, 8 steps):

$$\begin{aligned} & - \frac{2 B (b c - a d) g^2 n (a + b x)}{d^2 i^2 (c + d x)} + \frac{(b c - a d) g^2 (2 A + B n) (a + b x)}{d^2 i^2 (c + d x)} + \\ & \frac{2 B (b c - a d) g^2 (a + b x) \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right]}{d^2 i^2 (c + d x)} + \frac{g^2 (a + b x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{d i^2 (c + d x)} + \\ & \frac{b (b c - a d) g^2 \left( 2 A + B n + 2 B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{b c - a d}{b (c + d x)} \right]}{d^3 i^2} + \\ & \frac{2 B B (b c - a d) g^2 n \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^3 i^2} \end{aligned}$$

Result (type 4, 705 leaves):

$$\begin{aligned}
 & \frac{1}{d^3 i^2} g^2 \left( b^2 d x \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) - \right. \\
 & \quad \left. \frac{(b c - a d)^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)}{c+d x} - \right. \\
 & \quad 2 b (b c - a d) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] + \\
 & \quad \left( a^2 B d^2 n \left( b c - a d + b (c+d x) \operatorname{Log} \left[ \frac{a}{b} + x \right] + (-b c + a d) \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] - \right. \right. \\
 & \quad \quad \left. \left. b c \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] - b d x \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) \right) / \\
 & \quad \left( (b c - a d) (c+d x) \right) + a b B d n \left( -\operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] + \right. \\
 & \quad 2 \left( -\frac{c}{c+d x} + \frac{b c \operatorname{Log} [a+b x]}{-b c + a d} + \frac{b c \operatorname{Log} [c+d x]}{b c - a d} - \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [c+d x] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right. \\
 & \quad \quad \left. \left( \frac{c}{c+d x} + \operatorname{Log} [c+d x] \right) + \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) + 2 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \Big) + \\
 & \quad b^2 B n \left( d \left( \frac{a}{b} + x \right) \left( -1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right) - (c+d x) \left( -1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right) + c \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + \right. \\
 & \quad \quad \frac{c^2 \left( 1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{c+d x} + c^2 \left( -\frac{\operatorname{Log} \left[ \frac{a}{b} + x \right]}{c+d x} + \frac{b \left( \operatorname{Log} [a+b x] - \operatorname{Log} [c+d x] \right)}{b c - a d} \right) + \\
 & \quad \quad \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \left( d x - \frac{c^2}{c+d x} - 2 c \operatorname{Log} [c+d x] \right) - \\
 & \quad \quad \left. \left. 2 c \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \Big) \Big)
 \end{aligned}$$

### Problem 145: Result more than twice size of optimal antiderivative.

$$\int \frac{(a g + b g x) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^2} dx$$

Optimal (type 4, 168 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{A g (a+b x)}{d i^2 (c+d x)} + \frac{B g n (a+b x)}{d i^2 (c+d x)} - \frac{B g (a+b x) \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right]}{d i^2 (c+d x)} - \\
 & \frac{b g \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right]}{d^2 i^2} - \frac{b B g n \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^2 i^2}
 \end{aligned}$$

Result (type 4, 411 leaves):

$$\frac{1}{2 d^2 i^2} g \left( \frac{2 (b c - a d) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)}{c+d x} + \right. \\ \left. 2 b \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] + \right. \\ \left( 2 a B d n \left( b c - a d + b (c+d x) \operatorname{Log} \left[ \frac{a}{b} + x \right] + (-b c + a d) \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] - \right. \right. \\ \left. \left. b c \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] - b d x \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) \right) / \\ \left( (b c - a d) (c+d x) \right) + b B n \left( -\operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} [c+d x] + \right. \\ \left. 2 \left( -\frac{c}{c+d x} + \frac{b c \operatorname{Log} [a+b x]}{-b c + a d} + \frac{b c \operatorname{Log} [c+d x]}{b c - a d} - \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} [c+d x] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right. \right. \\ \left. \left. \left( \frac{c}{c+d x} + \operatorname{Log} [c+d x] \right) + \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) + 2 \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \Bigg)$$

**Problem 151: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 4, 382 leaves, 9 steps):

$$- \frac{3 B (b c - a d) g^3 n (a+b x)^2}{4 d^2 i^3 (c+d x)^2} - \frac{3 b B (b c - a d) g^3 n (a+b x)}{d^3 i^3 (c+d x)} + \\ \frac{b (b c - a d) g^3 (3 A + B n) (a+b x)}{d^3 i^3 (c+d x)} + \frac{3 b B (b c - a d) g^3 (a+b x) \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right]}{d^3 i^3 (c+d x)} + \\ \frac{g^3 (a+b x)^3 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{d i^3 (c+d x)^2} + \frac{(b c - a d) g^3 (a+b x)^2 \left( 3 A + B n + 3 B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 d^2 i^3 (c+d x)^2} + \\ \frac{b^2 (b c - a d) g^3 \left( 3 A + B n + 3 B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log} \left[ \frac{b c - a d}{b (c+d x)} \right]}{d^4 i^3} + \\ \frac{3 b^2 B (b c - a d) g^3 n \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^4 i^3}$$

Result (type 4, 1317 leaves):

$$\frac{1}{4 d^4 i^3} g^3 \left( 4 b^3 d x \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\ \left. \frac{2 (b c - a d)^3 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)}{(c+d x)^2} - \right.$$



$$\begin{aligned}
 & \frac{12 b (b c - a d)^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)}{c+d x} - \\
 & 12 b^2 (b c - a d) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] - \\
 & \frac{1}{(b c - a d)^2 (c+d x)^2} \left( 3 a^2 b B d^2 n \left( -b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - 2 b^2 c^2 d x + 6 a b c d^2 x - \right. \right. \\
 & \quad 4 a^2 d^3 x - 2 b (b c - 2 a d) (c+d x)^2 \operatorname{Log} [a+b x] + 2 (b c - a d)^2 (c+2 d x) \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] + \\
 & \quad 2 b^2 c^3 \operatorname{Log} [c+d x] - 4 a b c^2 d \operatorname{Log} [c+d x] + 4 b^2 c^2 d x \operatorname{Log} [c+d x] - \\
 & \quad \left. 8 a b c d^2 x \operatorname{Log} [c+d x] + 2 b^2 c d^2 x^2 \operatorname{Log} [c+d x] - 4 a b d^3 x^2 \operatorname{Log} [c+d x] \right) - \\
 & \left( a^3 B d^3 n \left( -b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - \right. \right. \\
 & \quad 2 b^2 (c+d x)^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] + 2 (b c - a d)^2 \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] + 2 b^2 c^2 \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \\
 & \quad \left. 4 b^2 c d x \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + 2 b^2 d^2 x^2 \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) \Big/ \left( (b c - a d)^2 (c+d x)^2 \right) + \\
 & 3 a b^2 B d n \left( -2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - \frac{8 c \left( 1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{c+d x} + \frac{c^2 \left( 1 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{(c+d x)^2} + \right. \\
 & \quad \left. 8 c \left( \frac{\operatorname{Log} \left[ \frac{a}{b} + x \right]}{c+d x} + \frac{b \left( \operatorname{Log} [a+b x] - \operatorname{Log} [c+d x] \right)}{-b c + a d} \right) \right) + \\
 & 2 \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \left( \frac{c \left( 3 c + 4 d x \right)}{(c+d x)^2} + 2 \operatorname{Log} [c+d x] \right) + \\
 & \frac{1}{(c+d x)^2} 2 c^2 \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \frac{1}{(b c - a d)^2} \right. \\
 & \quad \left. b (c+d x) (b c - a d + b (c+d x) \operatorname{Log} [a+b x] - b (c+d x) \operatorname{Log} [c+d x]) \right) + \\
 & 4 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) - \\
 & b^3 B n \left( -4 d \left( \frac{a}{b} + x \right) \left( -1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right) + 4 (c+d x) \left( -1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right) - \right. \\
 & \quad \left. 6 c \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - \frac{12 c^2 \left( 1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{c+d x} + \frac{c^3 \left( 1 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{(c+d x)^2} - \right. \\
 & \quad \left. 12 c^2 \left( -\frac{\operatorname{Log} \left[ \frac{a}{b} + x \right]}{c+d x} + \frac{b \left( \operatorname{Log} [a+b x] - \operatorname{Log} [c+d x] \right)}{b c - a d} \right) \right) + \\
 & 2 \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \left( -2 d x + \frac{c^2 \left( 5 c + 6 d x \right)}{(c+d x)^2} + 6 c \operatorname{Log} [c+d x] \right) +
 \end{aligned}$$

$$\frac{1}{(c+d x)^2} 2 c^3 \left( -\text{Log}\left[\frac{a}{b}+x\right] + \frac{1}{(b c-a d)^2} \right. \\ \left. b(c+d x)(b c-a d+b(c+d x) \text{Log}[a+b x]-b(c+d x) \text{Log}[c+d x]) \right) + \\ 12 c \left( \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \Bigg)$$

**Problem 152: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 4, 263 leaves, 8 steps):

$$\frac{B g^2 n (a+b x)^2}{4 d i^3 (c+d x)^2} - \frac{A b g^2 (a+b x)}{d^2 i^3 (c+d x)} + \frac{b B g^2 n (a+b x)}{d^2 i^3 (c+d x)} - \\ \frac{b B g^2 (a+b x) \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right]}{d^2 i^3 (c+d x)} - \frac{g^2 (a+b x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 d i^3 (c+d x)^2} - \\ \frac{b^2 g^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log}\left[ \frac{b c-a d}{b(c+d x)} \right]}{d^3 i^3} - \frac{b^2 B g^2 n \text{PolyLog}\left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{d^3 i^3}$$

Result (type 4, 907 leaves):

$$\begin{aligned}
 & \frac{1}{4 d^3 i^3} g^2 \left( - \frac{2 (b c - a d)^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)}{(c+d x)^2} + \right. \\
 & \quad \frac{8 b (b c - a d) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)}{c+d x} + \\
 & \quad 4 b^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] - \\
 & \quad \frac{1}{(b c - a d)^2 (c+d x)^2} 2 a b B d n \left( -b^2 c^3 + 4 a b c^2 d - 3 a^2 c d^2 - 2 b^2 c^2 d x + 6 a b c d^2 x - 4 a^2 d^3 x - \right. \\
 & \quad \left. 2 b (b c - 2 a d) (c+d x)^2 \operatorname{Log} [a+b x] + 2 (b c - a d)^2 (c+2 d x) \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] + \right. \\
 & \quad \left. 2 b^2 c^3 \operatorname{Log} [c+d x] - 4 a b c^2 d \operatorname{Log} [c+d x] + 4 b^2 c^2 d x \operatorname{Log} [c+d x] - \right. \\
 & \quad \left. 8 a b c d^2 x \operatorname{Log} [c+d x] + 2 b^2 c d^2 x^2 \operatorname{Log} [c+d x] - 4 a b d^3 x^2 \operatorname{Log} [c+d x] \right) - \\
 & \quad \left( a^2 B d^2 n \left( -b^2 c^2 + 4 a b c d - a^2 d^2 + 2 b^2 c d x + 2 a b d^2 x + 2 b^2 d^2 x^2 - \right. \right. \\
 & \quad \left. \left. 2 b^2 (c+d x)^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] + 2 (b c - a d)^2 \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] + 2 b^2 c^2 \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \right. \\
 & \quad \left. \left. 4 b^2 c d x \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + 2 b^2 d^2 x^2 \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) \right) / \left( (b c - a d)^2 (c+d x)^2 \right) + \\
 & \quad b^2 B n \left( -2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - \frac{8 c \left( 1 + \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{c+d x} + \frac{c^2 \left( 1 + 2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \right)}{(c+d x)^2} + \right. \\
 & \quad \left. 8 c \left( \frac{\operatorname{Log} \left[ \frac{a}{b} + x \right]}{c+d x} + \frac{b \left( \operatorname{Log} [a+b x] - \operatorname{Log} [c+d x] \right)}{-b c + a d} \right) \right) + \\
 & \quad 2 \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \left( \frac{c \left( 3 c + 4 d x \right)}{(c+d x)^2} + 2 \operatorname{Log} [c+d x] \right) + \\
 & \quad \frac{1}{(c+d x)^2} 2 c^2 \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \frac{1}{(b c - a d)^2} \right. \\
 & \quad \left. b (c+d x) (b c - a d + b (c+d x) \operatorname{Log} [a+b x] - b (c+d x) \operatorname{Log} [c+d x]) \right) + \\
 & \quad \left. 4 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \right)
 \end{aligned}$$

**Problem 153: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(c i + d i x)^3} dx$$

Optimal (type 3, 89 leaves, 2 steps):

$$-\frac{B g n (a+b x)^2}{4 (b c-a d) i^3 (c+d x)^2} + \frac{g (a+b x)^2 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{2 (b c-a d) i^3 (c+d x)^2}$$

Result (type 3, 216 leaves):

$$\left( g \left( 2 A b^2 c^2 - 2 a^2 A d^2 - b^2 B c^2 n + a^2 B d^2 n + 4 A b^2 c d x - 4 a A b d^2 x - 2 b^2 B c d n x + 2 a b B d^2 n x - 2 b^2 B n (c+d x)^2 \operatorname{Log}[a+b x] + 2 B (b c-a d) (b c+a d+2 b d x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2 b^2 B c^2 n \operatorname{Log}[c+d x] + 4 b^2 B c d n x \operatorname{Log}[c+d x] + 2 b^2 B d^2 n x^2 \operatorname{Log}[c+d x] \right) \right) / \left( 4 d^2 (-b c+a d) i^3 (c+d x)^2 \right)$$

### Problem 159: Result more than twice size of optimal antiderivative.

$$\int (a g+b g x)^3 (c i+d i x) \left( A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \right)^2 d x$$

Optimal (type 4, 584 leaves, 11 steps):

$$\begin{aligned} & \frac{3 B^2 (b c-a d)^4 g^3 i n^2 x}{10 b d^3} - \frac{3 B^2 (b c-a d)^3 g^3 i n^2 (c+d x)^2}{20 d^4} + \\ & \frac{b B^2 (b c-a d)^2 g^3 i n^2 (c+d x)^3}{30 d^4} - \frac{B (b c-a d)^2 g^3 i n (a+b x)^3 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{30 b^2 d} - \\ & \frac{B (b c-a d) g^3 i n (a+b x)^4 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{10 b^2} + \\ & \frac{(b c-a d) g^3 i (a+b x)^4 (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])^2}{20 b^2} + \frac{g^3 i (a+b x)^4 (c+d x) (A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])^2}{5 b} + \\ & \frac{B (b c-a d)^3 g^3 i n (a+b x)^2 (3 A+B n+3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{60 b^2 d^2} - \\ & \frac{B (b c-a d)^4 g^3 i n (a+b x) (6 A+5 B n+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])}{60 b^2 d^3} - \\ & \frac{B (b c-a d)^5 g^3 i n (6 A+11 B n+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]) \operatorname{Log}\left[\frac{b c-a d}{b (c+d x)}\right]}{60 b^2 d^4} - \\ & \frac{B^2 (b c-a d)^5 g^3 i n^2 \operatorname{Log}[c+d x]}{10 b^2 d^4} - \frac{B^2 (b c-a d)^5 g^3 i n^2 \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{10 b^2 d^4} \end{aligned}$$

Result (type 4, 3427 leaves):

$$\frac{1}{60 b^2 d^4} g^3 i \left( -6 b^5 B^2 c^5 n^2 + 36 a b^4 B^2 c^4 d n^2 - 90 a^2 b^3 B^2 c^3 d^2 n^2 + 90 a^3 b^2 B^2 c^2 d^3 n^2 - 24 a^4 b B^2 c d^4 n^2 - 6 a^5 B^2 d^5 n^2 + 60 a^3 A^2 b^2 c d^4 x - 6 A b^5 B c^4 d n x + 30 a A b^4 B c^3 d^2 n x - 60 a^2 A b^3 B c^2 d^3 n x + 30 a^3 A b^2 B c d^4 n x + 6 a^4 A b B d^5 n x + b^5 B^2 c^4 d n^2 x - 8 a b^4 B^2 c^3 d^2 n^2 x + 24 a^2 b^3 B^2 c^2 d^3 n^2 x - \right)$$

$$\begin{aligned}
 & 28 a^3 b^2 B^2 c d^4 n^2 x + 11 a^4 b B^2 d^5 n^2 x + 90 a^2 A^2 b^3 c d^4 x^2 + 30 a^3 A^2 b^2 d^5 x^2 + 3 A b^5 B c^3 d^2 n x^2 - \\
 & 15 a A b^4 B c^2 d^3 n x^2 - 15 a^2 A b^3 B c d^4 n x^2 + 27 a^3 A b^2 B d^5 n x^2 - 2 b^5 B^2 c^3 d^2 n^2 x^2 + \\
 & 12 a b^4 B^2 c^2 d^3 n^2 x^2 - 18 a^2 b^3 B^2 c d^4 n^2 x^2 + 8 a^3 b^2 B^2 d^5 n^2 x^2 + 60 a A^2 b^4 c d^4 x^3 + \\
 & 60 a^2 A^2 b^3 d^5 x^3 - 2 A b^5 B c^2 d^3 n x^3 - 20 a A b^4 B c d^4 n x^3 + 22 a^2 A b^3 B d^5 n x^3 + \\
 & 2 b^5 B^2 c^2 d^3 n^2 x^3 - 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + 15 A^2 b^5 c d^4 x^4 + 45 a A^2 b^4 d^5 x^4 - \\
 & 6 A b^5 B c d^4 n x^4 + 6 a A b^4 B d^5 n x^4 + 12 A^2 b^5 d^5 x^5 - 6 a b^4 B^2 c^4 d n^2 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 30 a^2 b^3 B^2 c^3 d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] - 60 a^3 b^2 B^2 c^2 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 30 a^4 b B^2 c d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 6 a^5 B^2 d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 15 a^4 b B^2 c d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 3 a^5 B^2 d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + \\
 & 6 b^5 B^2 c^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 30 a b^4 B^2 c^4 d n^2 \text{Log}\left[\frac{c}{d} + x\right] + 60 a^2 b^3 B^2 c^3 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] - \\
 & 30 a^3 b^2 B^2 c^2 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 6 a^4 b B^2 c d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 3 b^5 B^2 c^5 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + \\
 & 15 a b^4 B^2 c^4 d n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - 30 a^2 b^3 B^2 c^3 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + 30 a^3 b^2 B^2 c^2 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + \\
 & 30 a^4 A b B c d^4 n \text{Log}[a + b x] - 6 a^5 A B d^5 n \text{Log}[a + b x] - 3 a^2 b^3 B^2 c^3 d^2 n^2 \text{Log}[a + b x] + \\
 & 13 a^3 b^2 B^2 c^2 d^3 n^2 \text{Log}[a + b x] + a^4 b B^2 c d^4 n^2 \text{Log}[a + b x] - 11 a^5 B^2 d^5 n^2 \text{Log}[a + b x] - \\
 & 30 a^4 b B^2 c d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 6 a^5 B^2 d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\
 & 30 a^4 b B^2 c d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 6 a^5 B^2 d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 30 a^4 b B^2 c d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 6 a^5 B^2 d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & 120 a^3 A b^2 B c d^4 x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c^4 d n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 30 a b^4 B^2 c^3 d^2 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 60 a^2 b^3 B^2 c^2 d^3 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 30 a^3 b^2 B^2 c d^4 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a^4 b B^2 d^5 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 180 a^2 A b^3 B c d^4 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 60 a^3 A b^2 B d^5 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 3 b^5 B^2 c^3 d^2 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 15 a b^4 B^2 c^2 d^3 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
 & 15 a^2 b^3 B^2 c d^4 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 27 a^3 b^2 B^2 d^5 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 120 a A b^4 B c d^4 x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 a^2 A b^3 B d^5 x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
 & 2 b^5 B^2 c^2 d^3 n x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 20 a b^4 B^2 c d^4 n x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 22 a^2 b^3 B^2 d^5 n x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 30 A b^5 B c d^4 x^4 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 90 a A b^4 B d^5 x^4 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c d^4 n x^4 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 6 a b^4 B^2 d^5 n x^4 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 24 A b^5 B d^5 x^5 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 30 a^4 b B^2 c d^4 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 a^5 B^2 d^5 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] +
 \end{aligned}$$

$$\begin{aligned}
 &60 a^3 b^2 B^2 c d^4 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 90 a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 &30 a^3 b^2 B^2 d^5 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 &60 a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 15 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 &45 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 6 A b^5 B c^5 n \operatorname{Log}[c+d x] - \\
 &30 a A b^4 B c^4 d n \operatorname{Log}[c+d x] + 60 a^2 A b^3 B c^3 d^2 n \operatorname{Log}[c+d x] - 60 a^3 A b^2 B c^2 d^3 n \operatorname{Log}[c+d x] - \\
 &b^5 B^2 c^5 n^2 \operatorname{Log}[c+d x] + 11 a b^4 B^2 c^4 d n^2 \operatorname{Log}[c+d x] - 37 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c+d x] + \\
 &27 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c+d x] - 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 &30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 &60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 &30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 &60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 6 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - \\
 &30 a b^4 B^2 c^4 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + 60 a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - \\
 &60 a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\
 &6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 &60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 &6 b^2 B^2 c^2 (b^3 c^3 - 5 a b^2 c^2 d + 10 a^2 b c d^2 - 10 a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 &6 a^4 B^2 d^4 (-5 b c+a d) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 160: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^2 (c i + d i x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 dx$$

Optimal (type 4, 487 leaves, 10 steps):

$$\begin{aligned}
 & - \frac{B^2 (b c - a d)^3 g^2 i n^2 x}{3 b d^2} + \frac{B^2 (b c - a d)^2 g^2 i n^2 (c + d x)^2}{12 d^3} - \\
 & \frac{B (b c - a d)^2 g^2 i n (a + b x)^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{12 b^2 d} - \\
 & \frac{B (b c - a d) g^2 i n (a + b x)^3 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{6 b^2} + \\
 & \frac{(b c - a d) g^2 i (a + b x)^3 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{12 b^2} + \frac{g^2 i (a + b x)^3 (c + d x) \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 b} + \\
 & \frac{B (b c - a d)^3 g^2 i n (a + b x) \left( 2 A + B n + 2 B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{12 b^2 d^2} + \\
 & \frac{B (b c - a d)^4 g^2 i n \left( 2 A + 3 B n + 2 B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log} \left[ \frac{b c - a d}{b (c + d x)} \right]}{12 b^2 d^3} + \\
 & \frac{B^2 (b c - a d)^4 g^2 i n^2 \text{Log} [c + d x]}{6 b^2 d^3} + \frac{B^2 (b c - a d)^4 g^2 i n^2 \text{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{6 b^2 d^3}
 \end{aligned}$$

Result (type 4, 2520 leaves):

$$\begin{aligned}
 & \frac{1}{12 b^2 d^3} g^2 i \\
 & \left( 2 b^4 B^2 c^4 n^2 - 10 a b^3 B^2 c^3 d n^2 + 12 a^2 b^2 B^2 c^2 d^2 n^2 - 2 a^3 b B^2 c d^3 n^2 - 2 a^4 B^2 d^4 n^2 + 12 a^2 A^2 b^2 c d^3 x + \right. \\
 & \quad 2 A b^4 B c^3 d n x - 8 a A b^3 B c^2 d^2 n x + 4 a^2 A b^2 B c d^3 n x + 2 a^3 A b B d^4 n x - b^4 B^2 c^3 d n^2 x + \\
 & \quad 5 a b^3 B^2 c^2 d^2 n^2 x - 7 a^2 b^2 B^2 c d^3 n^2 x + 3 a^3 b B^2 d^4 n^2 x + 12 a A^2 b^3 c d^3 x^2 + \\
 & \quad 6 a^2 A^2 b^2 d^4 x^2 - A b^4 B c^2 d^2 n x^2 - 4 a A b^3 B c d^3 n x^2 + 5 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - \\
 & \quad 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + 4 A^2 b^4 c d^3 x^3 + 8 a A^2 b^3 d^4 x^3 - 2 A b^4 B c d^3 n x^3 + \\
 & \quad 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 + 2 a b^3 B^2 c^3 d n^2 \text{Log} \left[ \frac{a}{b} + x \right] - 8 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log} \left[ \frac{a}{b} + x \right] + \\
 & \quad 4 a^3 b B^2 c d^3 n^2 \text{Log} \left[ \frac{a}{b} + x \right] + 2 a^4 B^2 d^4 n^2 \text{Log} \left[ \frac{a}{b} + x \right] + 4 a^3 b B^2 c d^3 n^2 \text{Log} \left[ \frac{a}{b} + x \right]^2 - \\
 & \quad a^4 B^2 d^4 n^2 \text{Log} \left[ \frac{a}{b} + x \right]^2 - 2 b^4 B^2 c^4 n^2 \text{Log} \left[ \frac{c}{d} + x \right] + 8 a b^3 B^2 c^3 d n^2 \text{Log} \left[ \frac{c}{d} + x \right] - \\
 & \quad 4 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log} \left[ \frac{c}{d} + x \right] - 2 a^3 b B^2 c d^3 n^2 \text{Log} \left[ \frac{c}{d} + x \right] + b^4 B^2 c^4 n^2 \text{Log} \left[ \frac{c}{d} + x \right]^2 - \\
 & \quad 4 a b^3 B^2 c^3 d n^2 \text{Log} \left[ \frac{c}{d} + x \right]^2 + 6 a^2 b^2 B^2 c^2 d^2 n^2 \text{Log} \left[ \frac{c}{d} + x \right]^2 + 8 a^3 A b B c d^3 n \text{Log} [a + b x] - \\
 & \quad 2 a^4 A B d^4 n \text{Log} [a + b x] + a^2 b^2 B^2 c^2 d^2 n^2 \text{Log} [a + b x] + 2 a^3 b B^2 c d^3 n^2 \text{Log} [a + b x] - \\
 & \quad 3 a^4 B^2 d^4 n^2 \text{Log} [a + b x] - 8 a^3 b B^2 c d^3 n^2 \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} [a + b x] + \\
 & \quad 2 a^4 B^2 d^4 n^2 \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} [a + b x] + 8 a^3 b B^2 c d^3 n^2 \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} [a + b x] - \\
 & \quad 2 a^4 B^2 d^4 n^2 \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} [a + b x] - 8 a^3 b B^2 c d^3 n^2 \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \\
 & \quad 2 a^4 B^2 d^4 n^2 \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + 24 a^2 A b^2 B c d^3 x \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] +
 \end{aligned}$$

$$\begin{aligned}
 & 2 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 8 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 4 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 12 a^2 A b^2 B d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 4 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 5 a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 8 A b^4 B c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 16 a A b^3 B d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 8 a^3 b B^2 c d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 2 a^4 B^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 12 a^2 b^2 B^2 c d^3 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 6 a^2 b^2 B^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 4 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 8 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 - \\
 & 2 A b^4 B c^4 n \operatorname{Log}[c+d x] + 8 a A b^3 B c^3 d n \operatorname{Log}[c+d x] - 12 a^2 A b^2 B c^2 d^2 n \operatorname{Log}[c+d x] + \\
 & b^4 B^2 c^4 n^2 \operatorname{Log}[c+d x] - 6 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c+d x] + 5 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+d x] + \\
 & 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 2 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + 8 a b^3 B^2 c^3 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - \\
 & 12 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 2 b^2 B^2 c^2 (b^2 c^2 - 4 a b c d + 6 a^2 d^2) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 2 a^3 B^2 d^3 (-4 b c + a d) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 161: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x) (c i + d i x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 dx$$

Optimal (type 4, 372 leaves, 9 steps):



$$\frac{B^2 (b c - a d)^2 g i n^2 x}{3 b d} - \frac{B (b c - a d)^2 g i n (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b^2 d} -$$

$$\frac{B (b c - a d) g i n (a + b x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b^2} +$$

$$\frac{(b c - a d) g i (a + b x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{6 b^2} + \frac{g i (a + b x)^2 (c + d x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{3 b} -$$

$$\frac{B (b c - a d)^3 g i n \left( A + B n + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ \frac{b c - a d}{b (c + d x)} \right]}{3 b^2 d^2} -$$

$$\frac{B^2 (b c - a d)^3 g i n^2 \log [c + d x]}{3 b^2 d^2} - \frac{B^2 (b c - a d)^3 g i n^2 \text{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{3 b^2 d^2}$$

Result (type 4, 1606 leaves):

$$\frac{1}{6 b^2 d^2} \left( \begin{aligned} &g i \left( -2 b^3 B^2 c^3 n^2 + 2 a b^2 B^2 c^2 d n^2 + 2 a^2 b B^2 c d^2 n^2 - 2 a^3 B^2 d^3 n^2 + 6 a A^2 b^2 c d^2 x - 2 A b^3 B c^2 d n x + \right. \\ &2 a^2 A b B d^3 n x + 2 b^3 B^2 c^2 d n^2 x - 4 a b^2 B^2 c d^2 n^2 x + 2 a^2 b B^2 d^3 n^2 x + 3 A^2 b^3 c d^2 x^2 + \\ &3 a A^2 b^2 d^3 x^2 - 2 A b^3 B c d^2 n x^2 + 2 a A b^2 B d^3 n x^2 + 2 A^2 b^3 d^3 x^3 - 2 a b^2 B^2 c^2 d n^2 \text{Log}\left[\frac{a}{b} + x\right] + \\ &2 a^3 B^2 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 3 a^2 b B^2 c d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - a^3 B^2 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + \\ &2 b^3 B^2 c^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 2 a^2 b B^2 c d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] - b^3 B^2 c^3 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + \\ &3 a b^2 B^2 c^2 d n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + 6 a^2 A b B c d^2 n \text{Log}[a + b x] - 2 a^3 A B d^3 n \text{Log}[a + b x] + \\ &2 a^2 b B^2 c d^2 n^2 \text{Log}[a + b x] - 2 a^3 B^2 d^3 n^2 \text{Log}[a + b x] - 6 a^2 b B^2 c d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\ &2 a^3 B^2 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 6 a^2 b B^2 c d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\ &2 a^3 B^2 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 6 a^2 b B^2 c d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\ &2 a^3 B^2 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 12 a A b^2 B c d^2 x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\ &2 b^3 B^2 c^2 d n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 a^2 b B^2 d^3 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\ &6 A b^3 B c d^2 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a A b^2 B d^3 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\ &2 b^3 B^2 c d^2 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 a b^2 B^2 d^3 n x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\ &4 A b^3 B d^3 x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a^2 b B^2 c d^2 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\ &2 a^3 B^2 d^3 n \text{Log}[a + b x] \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 6 a b^2 B^2 c d^2 x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\ &3 b^3 B^2 c d^2 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 3 a b^2 B^2 d^3 x^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \\ &2 b^3 B^2 d^3 x^3 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 A b^3 B c^3 n \text{Log}[c + d x] - 6 a A b^2 B c^2 d n \text{Log}[c + d x] - \\ &2 b^3 B^2 c^3 n^2 \text{Log}[c + d x] + 2 a b^2 B^2 c^2 d n^2 \text{Log}[c + d x] - 2 b^3 B^2 c^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] + \\ &6 a b^2 B^2 c^2 d n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] + 2 b^3 B^2 c^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] - \\ &6 a b^2 B^2 c^2 d n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[c + d x] + 2 b^3 B^2 c^3 n \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \text{Log}[c + d x] - \\ &6 a b^2 B^2 c^2 d n \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \text{Log}[c + d x] + 2 b^3 B^2 c^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\ &6 a b^2 B^2 c^2 d n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] + 2 b^2 B^2 c^2 (b c - 3 a d) n^2 \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \\ &2 a^2 B^2 d^2 (-3 b c + a d) n^2 \text{PolyLog}\left[2, \frac{b(c + d x)}{b c - a d}\right] \end{aligned} \right)$$

### Problem 162: Result more than twice size of optimal antiderivative.

$$\int (c i + d i x) \left( A + B \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 220 leaves, 7 steps):

$$\begin{aligned} & - \frac{B (b c - a d) i n (a + b x) \left( A + B \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{b^2} + \\ & \frac{i (c + d x)^2 \left( A + B \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2}{2 d} + \frac{B^2 (b c - a d)^2 i n^2 \operatorname{Log}[c + d x]}{b^2 d} + \\ & \frac{B (b c - a d)^2 i n \left( A + B \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log} \left[ 1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d} - \frac{B^2 (b c - a d)^2 i n^2 \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^2 d} \end{aligned}$$

Result (type 4, 941 leaves):

$$\begin{aligned} & \frac{1}{2 b^2 d} i \left( -2 b^2 B^2 c^2 n^2 + 4 a b B^2 c d n^2 - 2 a^2 B^2 d^2 n^2 + 2 A^2 b^2 c d x - 2 A b^2 B c d n x + 2 a A b B d^2 n x + \right. \\ & A^2 b^2 d^2 x^2 - 2 a b B^2 c d n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] + 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] + 2 a b B^2 c d n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 - \\ & a^2 B^2 d^2 n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 + 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] - 2 a b B^2 c d n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] + \\ & b^2 B^2 c^2 n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 4 a A b B c d n \operatorname{Log}[a + b x] - 2 a^2 A B d^2 n \operatorname{Log}[a + b x] - \\ & 4 a b B^2 c d n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log}[a + b x] + 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log}[a + b x] + \\ & 4 a b B^2 c d n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log}[a + b x] - 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log}[a + b x] - \\ & 4 a b B^2 c d n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + 2 a^2 B^2 d^2 n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \\ & 4 A b^2 B c d x \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - 2 b^2 B^2 c d n x \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + \\ & 2 a b B^2 d^2 n x \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + 2 A b^2 B d^2 x^2 \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + \\ & 4 a b B^2 c d n \operatorname{Log}[a + b x] \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - 2 a^2 B^2 d^2 n \operatorname{Log}[a + b x] \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + \\ & 2 b^2 B^2 c d x \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 + b^2 B^2 d^2 x^2 \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 - 2 A b^2 B c^2 n \operatorname{Log}[c + d x] + \\ & 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log}[c + d x] - 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log}[c + d x] - \\ & 2 b^2 B^2 c^2 n \operatorname{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \operatorname{Log}[c + d x] - 2 b^2 B^2 c^2 n^2 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] - \\ & \left. 2 b^2 B^2 c^2 n^2 \operatorname{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] + 2 a B^2 d (-2 b c + a d) n^2 \operatorname{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \end{aligned}$$

**Problem 163: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{a g + b g x} dx$$

Optimal (type 4, 306 leaves, 8 steps):

$$\begin{aligned} & \frac{d i (a+b x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^2 g} + \frac{2 B (b c - a d) i n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{b c - a d}{b (c+d x)} \right]}{b^2 g} - \\ & \frac{(b c - a d) i \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \operatorname{Log}\left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^2 g} + \frac{2 B^2 (b c - a d) i n^2 \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^2 g} + \\ & \frac{2 B (b c - a d) i n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{PolyLog}\left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^2 g} + \\ & \frac{2 B^2 (b c - a d) i n^2 \operatorname{PolyLog}\left[ 3, \frac{b (c+d x)}{d (a+b x)} \right]}{b^2 g} \end{aligned}$$

Result (type 4, 1354 leaves):

$$\begin{aligned} & \frac{1}{3 b^2 g} i \left( 3 b d x \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 + \right. \\ & 3 (b c - a d) \operatorname{Log}[a+b x] \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 - \\ & 3 B n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \left( a d \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 - 2 a d \operatorname{Log}\left[ \frac{a}{b} + x \right] \right. \\ & \left. \left( 1 + \operatorname{Log}[a+b x] \right) + 2 \left( -b c + a d + \operatorname{Log}\left[ \frac{c}{d} + x \right] \left( b c + a d \operatorname{Log}[a+b x] - a d \operatorname{Log}\left[ \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \right) + \\ & \left. \left( -b d x + a d \operatorname{Log}[a+b x] \right) \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] - 2 a d \operatorname{PolyLog}\left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) + \\ & 3 b B c n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \\ & \left( \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 - 2 \operatorname{Log}[a+b x] \left( \operatorname{Log}\left[ \frac{a}{b} + x \right] - \operatorname{Log}\left[ \frac{c}{d} + x \right] - \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - \right. \\ & \left. 2 \left( \operatorname{Log}\left[ \frac{c}{d} + x \right] \operatorname{Log}\left[ \frac{d (a+b x)}{-b c + a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) - \\ & B^2 n^2 \left( a d \operatorname{Log}\left[ \frac{a}{b} + x \right]^3 - 3 d (a+b x) \left( 2 - 2 \operatorname{Log}\left[ \frac{a}{b} + x \right] + \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 \right) - \right. \\ & 3 b (c+d x) \left( 2 - 2 \operatorname{Log}\left[ \frac{c}{d} + x \right] + \operatorname{Log}\left[ \frac{c}{d} + x \right]^2 \right) - \\ & 3 d (b x - a \operatorname{Log}[a+b x]) \left( -\operatorname{Log}\left[ \frac{a}{b} + x \right] + \operatorname{Log}\left[ \frac{c}{d} + x \right] + \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\ & \left. 6 \left( a d + 2 b d x - b d x \operatorname{Log}\left[ \frac{c}{d} + x \right] - b c \operatorname{Log}[c+d x] + \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \text{Log}\left[\frac{a}{b} + x\right] \left( -d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + \\
 & (bc-ad) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - 3 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \\
 & \left( -2bc + 2ad - 2d(a+bx) \text{Log}\left[\frac{a}{b} + x\right] + ad \text{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\
 & \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \left( b(c+dx) - ad \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2ad \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) - \\
 & 3ad \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \left( \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
 & 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 3ad \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \\
 & \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Bigg) + \\
 & b^2 c n^2 \left( \text{Log}\left[\frac{a}{b} + x\right]^3 + 3 \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 3 \text{Log}[a+bx] \right. \\
 & \left. \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 + \right. \\
 & \left. 3 \text{Log}\left[\frac{a}{b} + x\right]^2 \left( -\text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 6 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \\
 & 6 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 3 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \\
 & \left( \text{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) - \\
 & \left. 6 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \Bigg)
 \end{aligned}$$

### Problem 164: Result more than twice size of optimal antiderivative.

$$\int \frac{(ci+di x) (A+B \text{Log}[e(\frac{a+bx}{c+dx})^n])^2}{(ag+bg x)^2} dx$$

Optimal (type 4, 261 leaves, 7 steps):

$$\begin{aligned}
 & -\frac{2B^2 i n^2 (c+dx)}{b g^2 (a+bx)} - \frac{2B i n (c+dx) (A+B \text{Log}[e(\frac{a+bx}{c+dx})^n])}{b g^2 (a+bx)} \\
 & \frac{i (c+dx) (A+B \text{Log}[e(\frac{a+bx}{c+dx})^n])^2}{b g^2 (a+bx)} - \frac{d i (A+B \text{Log}[e(\frac{a+bx}{c+dx})^n])^2 \text{Log}[1 - \frac{b(c+dx)}{d(a+bx)}]}{b^2 g^2} + \\
 & \frac{2B d i n (A+B \text{Log}[e(\frac{a+bx}{c+dx})^n]) \text{PolyLog}[2, \frac{b(c+dx)}{d(a+bx)}]}{b^2 g^2} + \frac{2B^2 d i n^2 \text{PolyLog}[3, \frac{b(c+dx)}{d(a+bx)}]}{b^2 g^2}
 \end{aligned}$$

Result (type 4, 1315 leaves):

$$\frac{1}{3 b^2 g^2} i \left( - \frac{3 (b c - a d) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2}{a+b x} + \right.$$

$$3 d \operatorname{Log}[a+b x] \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 +$$

$$\left( 6 b B c n \left( -A - B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] + B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \left( -d (a+b x) \operatorname{Log} \left[ \frac{c}{d} + x \right] + \right.$$

$$\left. \left. d (a+b x) \operatorname{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + (b c - a d) \left( 1 + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \right) / \left( (b c - a d) (a+b x) \right) -$$

$$\left( 3 b B^2 c n^2 \left( 2 b c - 2 a d + 2 d (a+b x) \operatorname{Log}[a+b x] + 2 (b c - a d) \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] + \right. \right.$$

$$\left. \left. b (c+d x) \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right]^2 - 2 d (a+b x) \operatorname{Log}[c+d x] \right) \right) / \left( (b c - a d) (a+b x) \right) +$$

$$3 B d n \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \left( \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 + \frac{2 a \left( 1 + \operatorname{Log} \left[ \frac{a}{b} + x \right] \right)}{a+b x} + \right.$$

$$2 \left( \frac{a}{a+b x} + \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) +$$

$$\left. \left( 2 a \left( (-b c + a d) \operatorname{Log} \left[ \frac{c}{d} + x \right] + d (a+b x) \left( \operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right) \right) \right) / \right.$$

$$\left. \left( (b c - a d) (a+b x) - 2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) +$$

$$B^2 d n^2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right]^3 + \frac{3 a \left( 2 + 2 \operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{a+b x} + 3 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 \operatorname{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + \right.$$

$$\frac{1}{a+b x} 3 \left( a + (a+b x) \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 -$$

$$3 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) + 6 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] +$$

$$\left( 3 a \left( d (a+b x) \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 + 2 \left( (-b c + a d) \operatorname{Log} \left[ \frac{c}{d} + x \right] + d (a+b x) \right. \right. \right.$$

$$\left. \left. \left( \operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right) \right) - 2 \operatorname{Log} \left[ \frac{a}{b} + x \right] \left( (b c - a d) \operatorname{Log} \left[ \frac{c}{d} + x \right] + d \right. \right.$$

$$\left. \left. (a+b x) \operatorname{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) - 2 d (a+b x) \operatorname{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) / \left. \right.$$

$$\left. \left( (b c - a d) (a+b x) + 6 \operatorname{Log} \left[ \frac{c}{d} + x \right] \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] + \right. \right.$$

$$\left. \left( 3 a \left( \operatorname{Log} \left[ \frac{c}{d} + x \right] \left( b (c+d x) \operatorname{Log} \left[ \frac{c}{d} + x \right] - 2 d (a+b x) \operatorname{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] \right) - \right. \right.$$

$$\left. \left. 2 d (a+b x) \operatorname{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) / \left( (b c - a d) (a+b x) \right) +$$

$$\begin{aligned}
 & 3 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \left( \text{Log}\left[\frac{a}{b} + x\right]^2 + \frac{2 a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{a+b x} + \right. \\
 & \left. \left( 2 a \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a+b x) \left( \text{Log}[a+b x] - \text{Log}[c+d x] \right) \right) \right) / \right. \\
 & \left. \left( (b c - a d) (a+b x) \right) - 2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) - \\
 & \left. 6 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right)
 \end{aligned}$$

### Problem 165: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x) \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(a g + b g x)^3} dx$$

Optimal (type 3, 151 leaves, 3 steps):

$$\begin{aligned}
 & -\frac{B^2 i n^2 (c+d x)^2}{4 (b c - a d) g^3 (a+b x)^2} - \\
 & \frac{B i n (c+d x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 (b c - a d) g^3 (a+b x)^2} - \frac{i (c+d x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 (b c - a d) g^3 (a+b x)^2}
 \end{aligned}$$

Result (type 3, 582 leaves):

$$\begin{aligned}
 & -\frac{1}{4 b^2 (b c - a d) g^3 (a+b x)^2} i \left( 2 b^2 B^2 n^2 (c+d x)^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 2 B d^2 n (a+b x)^2 \right. \\
 & \left. \text{Log}[a+b x] \left( 2 A + B n + 2 B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) + 2 B (b c - a d) n \right. \\
 & \left. (a d + b (c + 2 d x)) \text{Log}\left[\frac{a+b x}{c+d x}\right] \left( 2 A + B n + 2 B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \right. \\
 & \left. (b c - a d)^2 \left( 2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right]^2 - 2 B n (2 A + B n) \text{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \right. \\
 & \left. \left. 2 B^2 n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 2 B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \left( 2 A + B n - 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) \right) + 2 d (b c - a d) \\
 & (a+b x) \left( 2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right]^2 - 2 B n (2 A + B n) \text{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\
 & \left. 2 B^2 n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 2 B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \left( 2 A + B n - 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) - \\
 & \left. 2 B d^2 n (a+b x)^2 \left( 2 A + B n + 2 B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \text{Log}[c+d x] \right)
 \end{aligned}$$

**Problem 166: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x) \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(a g + b g x)^4} dx$$

Optimal (type 3, 307 leaves, 7 steps):

$$\begin{aligned} & \frac{B^2 d i n^2 (c + d x)^2}{4 (b c - a d)^2 g^4 (a + b x)^2} - \frac{2 b B^2 i n^2 (c + d x)^3}{27 (b c - a d)^2 g^4 (a + b x)^3} + \\ & \frac{B d i n (c + d x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{2 (b c - a d)^2 g^4 (a + b x)^2} - \frac{2 b B i n (c + d x)^3 \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{9 (b c - a d)^2 g^4 (a + b x)^3} + \\ & \frac{d i (c + d x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2}{2 (b c - a d)^2 g^4 (a + b x)^2} - \frac{b i (c + d x)^3 \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2}{3 (b c - a d)^2 g^4 (a + b x)^3} \end{aligned}$$

Result (type 3, 1015 leaves):



$$\begin{aligned}
 & \frac{1}{g^4} i \left( \left( B^2 n^2 (-2 b c^3 + 3 a c^2 d - 3 b c^2 d x + 6 a c d^2 x + 3 a d^3 x^2 + b d^3 x^3) \text{Log} \left[ \frac{a+b x}{c+d x} \right]^2 \right) / \right. \\
 & \quad \left( 6 (-b c + a d)^2 (a+b x)^3 \right) + \frac{B d^2 n \left( 6 A + 5 B n + 6 B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right)}{18 b^2 (b c - a d) (a+b x)} + \\
 & \quad \left( B d^3 n \text{Log} [a+b x] \left( 6 A + 5 B n + 6 B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \right) / \\
 & \quad \left( 18 b^2 (b c - a d)^2 \right) + \frac{1}{18 b^2 (b c - a d) (a+b x)^3} \\
 & \quad B n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \left( -12 A b^2 c^2 + 6 a A b c d + 6 a^2 A d^2 - 4 b^2 B c^2 n + 5 a b B c d n + 5 a^2 B d^2 n - \right. \\
 & \quad 18 A b^2 c d x + 18 a A b d^2 x - 3 b^2 B c d n x + 15 a b B d^2 n x + 6 b^2 B d^2 n x^2 - 12 b^2 B c^2 \\
 & \quad \left. \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + 6 a b B c d \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\
 & \quad 6 a^2 B d^2 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) - 18 b^2 B c d x \\
 & \quad \left. \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + 18 a b B d^2 x \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) - \\
 & \quad \frac{1}{27 b^2 (a+b x)^3} (b c - a d) \left( 9 A^2 + 6 A B n + 2 B^2 n^2 + 18 A B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\
 & \quad \left. 6 B^2 n \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + 9 B^2 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) - \\
 & \quad \frac{1}{36 b^2 (a+b x)^2} d \left( 18 A^2 + 6 A B n - B^2 n^2 + 36 A B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\
 & \quad \left. 6 B^2 n \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + 18 B^2 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) - \\
 & \quad \left. \left( B d^3 n \left( 6 A + 5 B n + 6 B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \text{Log} [c+d x] \right) / \left( 18 b^2 (b c - a d)^2 \right) \right)
 \end{aligned}$$

**Problem 168: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^3 (c i + d i x)^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 766 leaves, 17 steps):

$$\begin{aligned} & \frac{3 B^2 (b c-a d)^5 g^3 i^2 n^2 x}{20 b^2 d^3} + \frac{B^2 (b c-a d)^2 g^3 i^2 n^2 (a+b x)^4}{60 b^3} - \frac{3 B^2 (b c-a d)^4 g^3 i^2 n^2 (c+d x)^2}{40 b d^4} + \\ & \frac{B^2 (b c-a d)^3 g^3 i^2 n^2 (c+d x)^3}{60 d^4} - \frac{B (b c-a d)^3 g^3 i^2 n (a+b x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{90 b^3 d} - \\ & \frac{B (b c-a d)^2 g^3 i^2 n (a+b x)^4 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{20 b^3} - \\ & \frac{B (b c-a d) g^3 i^2 n (a+b x)^4 (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{15 b^2} + \\ & \frac{(b c-a d)^2 g^3 i^2 (a+b x)^4 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{60 b^3} + \\ & \frac{(b c-a d) g^3 i^2 (a+b x)^4 (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{15 b^2} + \\ & \frac{g^3 i^2 (a+b x)^4 (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{6 b} + \\ & \frac{B (b c-a d)^4 g^3 i^2 n (a+b x)^2 \left(3 A+B n+3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{180 b^3 d^2} - \\ & \frac{B (b c-a d)^5 g^3 i^2 n (a+b x) \left(6 A+5 B n+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{180 b^3 d^3} - \\ & \frac{B (b c-a d)^6 g^3 i^2 n \left(6 A+11 B n+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[\frac{b c-a d}{b(c+d x)}\right]}{180 b^3 d^4} - \\ & \frac{B^2 (b c-a d)^6 g^3 i^2 n^2 \operatorname{Log}[c+d x]}{20 b^3 d^4} - \frac{B^2 (b c-a d)^6 g^3 i^2 n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{b(c+d x)}\right]}{30 b^3 d^4} \end{aligned}$$

Result (type 4, 4611 leaves):

$$\begin{aligned} & \frac{1}{360 b^3 d^4} \\ & g^3 i^2 \left( -12 b^6 B^2 c^6 n^2 + 84 a b^5 B^2 c^5 d n^2 - 252 a^2 b^4 B^2 c^4 d^2 n^2 + 240 a^3 b^3 B^2 c^3 d^3 n^2 + 12 a^4 b^2 B^2 c^2 d^4 n^2 - \right. \\ & 84 a^5 b B^2 c d^5 n^2 + 12 a^6 B^2 d^6 n^2 + 360 a^3 A^2 b^3 c^2 d^4 x - 12 A b^6 B c^5 d n x + 72 a A b^5 B c^4 d^2 n x - \\ & 180 a^2 A b^4 B c^3 d^3 n x + 60 a^3 A b^3 B c^2 d^4 n x + 72 a^4 A b^2 B c d^5 n x - 12 a^5 A b B d^6 n x + \\ & 8 b^6 B^2 c^5 d n^2 x - 54 a b^5 B^2 c^4 d^2 n^2 x + 154 a^2 b^4 B^2 c^3 d^3 n^2 x - 194 a^3 b^3 B^2 c^2 d^4 n^2 x + \\ & 102 a^4 b^2 B^2 c d^5 n^2 x - 16 a^5 b B^2 d^6 n^2 x + 540 a^2 A^2 b^4 c^2 d^4 x^2 + 360 a^3 A^2 b^3 c d^5 x^2 + \\ & 6 A b^6 B c^4 d^2 n x^2 - 36 a A b^5 B c^3 d^3 n x^2 - 180 a^2 A b^4 B c^2 d^4 n x^2 + 204 a^3 A b^3 B c d^5 n x^2 + \\ & 6 a^4 A b^2 B d^6 n x^2 - 7 b^6 B^2 c^4 d^2 n^2 x^2 + 46 a b^5 B^2 c^3 d^3 n^2 x^2 - 60 a^2 b^4 B^2 c^2 d^4 n^2 x^2 + \\ & 10 a^3 b^3 B^2 c d^5 n^2 x^2 + 11 a^4 b^2 B^2 d^6 n^2 x^2 + 360 a A^2 b^5 c^2 d^4 x^3 + 720 a^2 A^2 b^4 c d^5 x^3 + \\ & 120 a^3 A^2 b^3 d^6 x^3 - 4 A b^6 B c^3 d^3 n x^3 - 156 a A b^5 B c^2 d^4 n x^3 + 84 a^2 A b^4 B c d^5 n x^3 + \\ & 76 a^3 A b^3 B d^6 n x^3 + 6 b^6 B^2 c^3 d^3 n^2 x^3 + 6 a b^5 B^2 c^2 d^4 n^2 x^3 - 30 a^2 b^4 B^2 c d^5 n^2 x^3 + \\ & 18 a^3 b^3 B^2 d^6 n^2 x^3 + 90 A^2 b^6 c^2 d^4 x^4 + 540 a A^2 b^5 c d^5 x^4 + 270 a^2 A^2 b^4 d^6 x^4 - 42 A b^6 B c^2 d^4 n x^4 - \\ & 36 a A b^5 B c d^5 n x^4 + 78 a^2 A b^4 B d^6 n x^4 + 6 b^6 B^2 c^2 d^4 n^2 x^4 - 12 a b^5 B^2 c d^5 n^2 x^4 + 6 a^2 b^4 B^2 d^6 n^2 x^4 + \\ & 144 A^2 b^6 c d^5 x^5 + 216 a A^2 b^5 d^6 x^5 - 24 A b^6 B c d^5 n x^5 + 24 a A b^5 B d^6 n x^5 + 60 A^2 b^6 d^6 x^6 - \end{aligned}$$

$$\begin{aligned}
 & 12 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]+72 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-180 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]+ \\
 & 60 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]+72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]+ \\
 & 90 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-36 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+6 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+ \\
 & 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 60 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-72 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+12 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 6 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+36 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-90 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+ \\
 & 120 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+180 a^4 A b^2 B c^2 d^4 n \operatorname{Log}[a+b x]-72 a^5 A b B c d^5 n \operatorname{Log}[a+b x]+ \\
 & 12 a^6 A B d^6 n \operatorname{Log}[a+b x]-6 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}[a+b x]+32 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}[a+b x]+ \\
 & 66 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}[a+b x]-108 a^5 b B^2 c d^5 n^2 \operatorname{Log}[a+b x]+16 a^6 B^2 d^6 n^2 \operatorname{Log}[a+b x]- \\
 & 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]- \\
 & 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]+12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 180 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+72 a^5 b B^2 c d^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]- \\
 & 12 a^6 B^2 d^6 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+720 a^3 A b^3 B c^2 d^4 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 12 b^6 B^2 c^5 d n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+72 a b^5 B^2 c^4 d^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 180 a^2 b^4 B^2 c^3 d^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+60 a^3 b^3 B^2 c^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 72 a^4 b^2 B^2 c d^5 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-12 a^5 b B^2 d^6 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+720 a^3 A b^3 B c d^5 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 6 b^6 B^2 c^4 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-36 a b^5 B^2 c^3 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 180 a^2 b^4 B^2 c^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+204 a^3 b^3 B^2 c d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 6 a^4 b^2 B^2 d^6 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+720 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 1440 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+240 a^3 A b^3 B d^6 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 4 b^6 B^2 c^3 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-156 a b^5 B^2 c^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 84 a^2 b^4 B^2 c d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+76 a^3 b^3 B^2 d^6 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 180 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+
 \end{aligned}$$

$$\begin{aligned}
 & 540 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 42 b^6 B^2 c^2 d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 36 a b^5 B^2 c d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 78 a^2 b^4 B^2 d^6 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 288 A b^6 B c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 432 a A b^5 B d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 24 b^6 B^2 c d^5 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 24 a b^5 B^2 d^6 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 120 A b^6 B d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 180 a^4 b^2 B^2 c^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 72 a^5 b B^2 c d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 12 a^6 B^2 d^6 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 360 a^3 b^3 B^2 c^2 d^4 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 360 a^3 b^3 B^2 c d^5 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 360 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 720 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 120 a^3 b^3 B^2 d^6 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 90 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 270 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 144 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 216 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 12 A b^6 B c^6 n \operatorname{Log}[c+d x] - 72 a A b^5 B c^5 d n \operatorname{Log}[c+d x] + 180 a^2 A b^4 B c^4 d^2 n \operatorname{Log}[c+d x] - \\
 & 240 a^3 A b^3 B c^3 d^3 n \operatorname{Log}[c+d x] - 8 b^6 B^2 c^6 n^2 \operatorname{Log}[c+d x] + 60 a b^5 B^2 c^5 d n^2 \operatorname{Log}[c+d x] - \\
 & 186 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}[c+d x] + 128 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}[c+d x] + 6 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}[c+d x] - \\
 & 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 12 b^6 B^2 c^6 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 72 a b^5 B^2 c^5 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\
 & 180 a^2 b^4 B^2 c^4 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - \\
 & 240 a^3 b^3 B^2 c^3 d^3 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 240 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 12 b^3 B^2 c^3 \left(b^3 c^3 - 6 a b^2 c^2 d + 15 a^2 b c d^2 - 20 a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] -
 \end{aligned}$$

$$12 a^4 B^2 d^4 (15 b^2 c^2 - 6 a b c d + a^2 d^2) n^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right]$$

**Problem 169: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^2 (c i + d i x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 819 leaves, 15 steps):

$$\begin{aligned} & - \frac{B^2 (bc - ad)^4 g^2 i^2 n^2 x}{10 b^2 d^2} - \frac{B^2 (bc - ad)^3 g^2 i^2 n^2 (c + dx)^2}{20 b d^3} + \\ & \frac{B^2 (bc - ad)^2 g^2 i^2 n^2 (c + dx)^3}{30 d^3} - \frac{B (bc - ad)^3 g^2 i^2 n (a + bx)^2 (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])}{30 b^3 d} - \\ & \frac{B (bc - ad)^2 g^2 i^2 n (a + bx)^3 (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])}{15 b^3} - \\ & \frac{B (bc - ad)^3 g^2 i^2 n (c + dx)^2 (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])}{5 b d^3} + \\ & \frac{4 B (bc - ad)^2 g^2 i^2 n (c + dx)^3 (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])}{15 d^3} - \\ & \frac{b B (bc - ad) g^2 i^2 n (c + dx)^4 (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])}{10 d^3} + \\ & \frac{(bc - ad)^2 g^2 i^2 (a + bx)^3 (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])^2}{30 b^3} + \\ & \frac{(bc - ad) g^2 i^2 (a + bx)^3 (c + dx) (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])^2}{10 b^2} + \\ & \frac{g^2 i^2 (a + bx)^3 (c + dx)^2 (A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])^2}{5 b} + \\ & \frac{B (bc - ad)^4 g^2 i^2 n (a + bx) (2A + Bn + 2B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right])}{30 b^3 d^2} + \\ & \frac{B (bc - ad)^5 g^2 i^2 n (2A + 3Bn + 2B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]) \text{Log}\left[ \frac{bc - ad}{b(c + dx)} \right]}{30 b^3 d^3} + \\ & \frac{B^2 (bc - ad)^5 g^2 i^2 n^2 \text{Log}\left[ \frac{a + b x}{c + d x} \right]}{30 b^3 d^3} + \frac{B^2 (bc - ad)^5 g^2 i^2 n^2 \text{Log}[c + dx]}{10 b^3 d^3} + \\ & \frac{B^2 (bc - ad)^5 g^2 i^2 n^2 \text{PolyLog}\left[2, \frac{d(a + b x)}{b(c + d x)}\right]}{15 b^3 d^3} \end{aligned}$$

Result (type 4, 3366 leaves):

$$\frac{1}{60 b^3 d^3}$$

$$\begin{aligned}
& g^2 i^2 \left( 4 b^5 B^2 c^5 n^2 - 24 a b^4 B^2 c^4 d n^2 + 20 a^2 b^3 B^2 c^3 d^2 n^2 + 20 a^3 b^2 B^2 c^2 d^3 n^2 - 24 a^4 b B^2 c d^4 n^2 + \right. \\
& 4 a^5 B^2 d^5 n^2 + 60 a^2 A^2 b^3 c^2 d^3 x + 4 A b^5 B c^4 d n x - 20 a A b^4 B c^3 d^2 n x + 20 a^3 A b^2 B c d^4 n x - \\
& 4 a^4 A b B d^5 n x - 4 b^5 B^2 c^4 d n^2 x + 22 a b^4 B^2 c^3 d^2 n^2 x - 36 a^2 b^3 B^2 c^2 d^3 n^2 x + 22 a^3 b^2 B^2 c d^4 n^2 x - \\
& 4 a^4 b B^2 d^5 n^2 x + 60 a A^2 b^4 c^2 d^3 x^2 + 60 a^2 A^2 b^3 c d^4 x^2 - 2 A b^5 B c^3 d^2 n x^2 - 30 a A b^4 B c^2 d^3 n x^2 + \\
& 30 a^2 A b^3 B c d^4 n x^2 + 2 a^3 A b^2 B d^5 n x^2 + 3 b^5 B^2 c^3 d^2 n^2 x^2 - 3 a b^4 B^2 c^2 d^3 n^2 x^2 - \\
& 3 a^2 b^3 B^2 c d^4 n^2 x^2 + 3 a^3 b^2 B^2 d^5 n^2 x^2 + 20 A^2 b^5 c^2 d^3 x^3 + 80 a A^2 b^4 c d^4 x^3 + 20 a^2 A^2 b^3 d^5 x^3 - \\
& 12 A b^5 B c^2 d^3 n x^3 + 12 a^2 A b^3 B d^5 n x^3 + 2 b^5 B^2 c^2 d^3 n^2 x^3 - 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + \\
& 30 A^2 b^5 c d^4 x^4 + 30 a A^2 b^4 d^5 x^4 - 6 A b^5 B c d^4 n x^4 + 6 a A b^4 B d^5 n x^4 + 12 A^2 b^5 d^5 x^5 + \\
& 4 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 20 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 20 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - \\
& 4 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] + 20 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 10 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \\
& 2 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 4 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 20 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \\
& 20 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 4 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \\
& 10 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 20 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 40 a^3 A b^2 B c^2 d^3 n \operatorname{Log}[a + b x] - \\
& 20 a^4 A b B c d^4 n \operatorname{Log}[a + b x] + 4 a^5 A B d^5 n \operatorname{Log}[a + b x] + 2 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[a + b x] + \\
& 18 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[a + b x] - 24 a^4 b B^2 c d^4 n^2 \operatorname{Log}[a + b x] + 4 a^5 B^2 d^5 n^2 \operatorname{Log}[a + b x] - \\
& 40 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 20 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] - \\
& 4 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 40 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 20 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] + 4 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \\
& 40 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 20 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - \\
& 4 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 120 a^2 A b^3 B c^2 d^3 x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 4 b^5 B^2 c^4 d n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 20 a b^4 B^2 c^3 d^2 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 20 a^3 b^2 B^2 c d^4 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 4 a^4 b B^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 120 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 120 a^2 A b^3 B c d^4 x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
& 2 b^5 B^2 c^3 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 30 a b^4 B^2 c^2 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 30 a^2 b^3 B^2 c d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 2 a^3 b^2 B^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 40 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 160 a A b^4 B c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 40 a^2 A b^3 B d^5 x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 12 b^5 B^2 c^2 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 12 a^2 b^3 B^2 d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 60 A b^5 B c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
& 60 a A b^4 B d^5 x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 b^5 B^2 c d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] +
\end{aligned}$$

$$\begin{aligned}
 & 6 a b^4 B^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+24 A b^5 B d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 4 \theta a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-2 \theta a^4 b B^2 c d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 4 a^5 B^2 d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+6 \theta a^2 b^3 B^2 c^2 d^3 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 6 \theta a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+6 \theta a^2 b^3 B^2 c d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 2 \theta b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+8 \theta a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 2 \theta a^2 b^3 B^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+3 \theta b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 3 \theta a b^4 B^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-4 A b^5 B c^5 n \operatorname{Log}[c+d x]+ \\
 & 2 \theta a A b^4 B c^4 d n \operatorname{Log}[c+d x]-4 \theta a^2 A b^3 B c^3 d^2 n \operatorname{Log}[c+d x]+4 b^5 B^2 c^5 n^2 \operatorname{Log}[c+d x]- \\
 & 24 a b^4 B^2 c^4 d n^2 \operatorname{Log}[c+d x]+18 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c+d x]+2 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c+d x]+ \\
 & 4 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-2 \theta a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
 & 4 \theta a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]-4 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
 & 2 \theta a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-4 \theta a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
 & 4 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]+2 \theta a b^4 B^2 c^4 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]- \\
 & 4 \theta a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]-4 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \\
 & 2 \theta a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-4 \theta a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
 & 4 b^3 B^2 c^3\left(b^2 c^2-5 a b c d+10 a^2 d^2\right) n^2 \operatorname{PolyLog}\left[2,\frac{d(a+b x)}{-b c+a d}\right]- \\
 & 4 a^3 B^2 d^3\left(10 b^2 c^2-5 a b c d+a^2 d^2\right) n^2 \operatorname{PolyLog}\left[2,\frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 170: Result more than twice size of optimal antiderivative.**

$$\int(a g+b g x)(c i+d i x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 d x$$

Optimal (type 4, 635 leaves, 14 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^3 g i^2 n^2 x}{12 b^2 d} + \frac{B^2 (b c - a d)^2 g i^2 n^2 (c + d x)^2}{12 b d^2} - \\ & \frac{B (b c - a d)^3 g i^2 n (a + b x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{6 b^3 d} - \\ & \frac{B (b c - a d)^2 g i^2 n (a + b x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{6 b^3} + \\ & \frac{B (b c - a d)^2 g i^2 n (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{4 b d^2} - \\ & \frac{B (b c - a d) g i^2 n (c + d x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{6 d^2} + \\ & \frac{(b c - a d)^2 g i^2 (a + b x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{12 b^3} + \\ & \frac{(b c - a d) g i^2 (a + b x)^2 (c + d x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{6 b^2} + \\ & \frac{g i^2 (a + b x)^2 (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 b} - \\ & \frac{B (b c - a d)^4 g i^2 n \left( A + B n + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{b c - a d}{b (c + d x)} \right]}{6 b^3 d^2} - \frac{B^2 (b c - a d)^4 g i^2 n^2 \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right]}{12 b^3 d^2} - \\ & \frac{B^2 (b c - a d)^4 g i^2 n^2 \operatorname{Log}[c + d x]}{4 b^3 d^2} - \frac{B^2 (b c - a d)^4 g i^2 n^2 \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{6 b^3 d^2} \end{aligned}$$

Result (type 4, 2518 leaves):

$$\begin{aligned} & \frac{1}{12 b^3 d^2} \\ & g i^2 \left( -2 b^4 B^2 c^4 n^2 - 2 a b^3 B^2 c^3 d n^2 + 12 a^2 b^2 B^2 c^2 d^2 n^2 - 10 a^3 b B^2 c d^3 n^2 + 2 a^4 B^2 d^4 n^2 + 12 a A^2 b^3 c^2 \right. \\ & \quad d^2 x - 2 A b^4 B c^3 d n x - 4 a A b^3 B c^2 d^2 n x + 8 a^2 A b^2 B c d^3 n x - 2 a^3 A b B d^4 n x + 3 b^4 B^2 c^3 d n^2 x - \\ & \quad 7 a b^3 B^2 c^2 d^2 n^2 x + 5 a^2 b^2 B^2 c d^3 n^2 x - a^3 b B^2 d^4 n^2 x + 6 A^2 b^4 c^2 d^2 x^2 + 12 a A^2 b^3 c d^3 x^2 - \\ & \quad 5 A b^4 B c^2 d^2 n x^2 + 4 a A b^3 B c d^3 n x^2 + a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + \\ & \quad a^2 b^2 B^2 d^4 n^2 x^2 + 8 A^2 b^4 c d^3 x^3 + 4 a A^2 b^3 d^4 x^3 - 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + \\ & \quad 3 A^2 b^4 d^4 x^4 - 2 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[ \frac{a}{b} + x \right] - 4 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[ \frac{a}{b} + x \right] + \\ & \quad 8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[ \frac{a}{b} + x \right] - 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[ \frac{a}{b} + x \right] + 6 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 - \\ & \quad 4 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 + a^4 B^2 d^4 n^2 \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 + 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[ \frac{c}{d} + x \right] + \\ & \quad 4 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[ \frac{c}{d} + x \right] - 8 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[ \frac{c}{d} + x \right] + 2 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[ \frac{c}{d} + x \right] - \\ & \quad b^4 B^2 c^4 n^2 \operatorname{Log}\left[ \frac{c}{d} + x \right]^2 + 4 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[ \frac{c}{d} + x \right]^2 + 12 a^2 A b^2 B c^2 d^2 n \operatorname{Log}[a + b x] - \\ & \quad 8 a^3 A b B c d^3 n \operatorname{Log}[a + b x] + 2 a^4 A B d^4 n \operatorname{Log}[a + b x] + 5 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[a + b x] - \end{aligned}$$



$$\begin{aligned}
 & 6 a^3 b B^2 c d^3 n^2 \operatorname{Log}[a+b x] + a^4 B^2 d^4 n^2 \operatorname{Log}[a+b x] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \\
 & 8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] - 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x] + \\
 & 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] + \\
 & 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x] - 12 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
 & 8 a^3 b B^2 c d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - 2 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \\
 & 24 a A b^3 B c^2 d^2 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 2 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 4 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 8 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 2 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 12 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 24 a A b^3 B c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 5 b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 4 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 16 A b^4 B c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 8 a A b^3 B d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 12 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 8 a^3 b B^2 c d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2 a^4 B^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 12 a b^3 B^2 c^2 d^2 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 6 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 12 a b^3 B^2 c d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 8 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 4 a b^3 B^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2 A b^4 B c^4 n \operatorname{Log}[c+d x] - \\
 & 8 a A b^3 B c^3 d n \operatorname{Log}[c+d x] - 3 b^4 B^2 c^4 n^2 \operatorname{Log}[c+d x] + 2 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c+d x] + \\
 & a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+d x] - 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - \\
 & 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + 2 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - \\
 & 8 a b^3 B^2 c^3 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + 2 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 8 a b^3 B^2 c^3 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 b^3 B^2 c^3 (b c-4 a d) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] -
 \end{aligned}$$

$$2 a^2 B^2 d^2 (6 b^2 c^2 - 4 a b c d + a^2 d^2) n^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]$$

**Problem 171: Result more than twice size of optimal antiderivative.**

$$\int (c i + d i x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 361 leaves, 11 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^2 i^2 n^2 x}{3 b^2} - \frac{2 B (b c - a d)^2 i^2 n (a + b x) \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b^3} - \\ & \frac{B (b c - a d) i^2 n (c + d x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b d} + \frac{i^2 (c + d x)^3 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{3 d} + \\ & \frac{B^2 (b c - a d)^3 i^2 n^2 \text{Log}\left[ \frac{a+b x}{c+d x} \right]}{3 b^3 d} + \frac{B^2 (b c - a d)^3 i^2 n^2 \text{Log}[c + d x]}{b^3 d} + \\ & \frac{2 B (b c - a d)^3 i^2 n \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log}\left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{3 b^3 d} - \\ & \frac{2 B^2 (b c - a d)^3 i^2 n^2 \text{PolyLog}\left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{3 b^3 d} \end{aligned}$$

Result (type 4, 1589 leaves):

$$\begin{aligned} & i^2 \left( c^2 x \left( A + B \left( \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 + \right. \\ & c d x^2 \left( A + B \left( \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 + \\ & \frac{1}{3} d^2 x^3 \left( A + B \left( \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 + \\ & 2 B c^2 n \left( A + B \left( \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right) \\ & \left( x \text{Log}\left[ \frac{a+b x}{c+d x} \right] + \frac{(b c - a d) (a d \text{Log}[a+b x] - b c \text{Log}[c+d x])}{b^2 c d - a b d^2} \right) + \\ & 2 B d^2 n \left( A + B \left( \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right) \left( \frac{1}{3} x^3 \text{Log}\left[ \frac{a+b x}{c+d x} \right] - \frac{1}{6 b^3 d^3} \right. \\ & \left. (b d (b c - a d) x (-2 b c - 2 a d + b d x) - 2 a^3 d^3 \text{Log}[a+b x] + 2 b^3 c^3 \text{Log}[c+d x]) \right) + \\ & 4 B c d n \left( A + B \left( \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right) \\ & \left( \frac{1}{2} x^2 \text{Log}\left[ \frac{a+b x}{c+d x} \right] - \frac{1}{2} (b c - a d) \left( \frac{x}{b d} + \frac{a^2 \text{Log}[a+b x]}{b^2 (b c - a d)} - \frac{c^2 \text{Log}[c+d x]}{d^2 (b c - a d)} \right) \right) + \\ & B^2 c^2 n^2 \left( x \text{Log}\left[ \frac{a+b x}{c+d x} \right]^2 - \frac{1}{b d} \left( -a d \text{Log}\left[ \frac{a}{b} + x \right]^2 - b c \text{Log}\left[ \frac{c}{d} + x \right]^2 + 2 a d \text{Log}\left[ \frac{a}{b} + x \right] \text{Log}[a+b x] - \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]+2 a d \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]- \\
 & 2 a d \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+2 b c \operatorname{Log}\left[\frac{c}{d}+x\right] \\
 & \operatorname{Log}[c+d x]+2 b c \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x]+2 b c \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \\
 & 2 b c \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\left.\right\}+2 B^2 c d n^2 \\
 & \left(\frac{1}{2} x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2-\frac{1}{2 b^2 d^2}\left(-2 d(-b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)+a^2 d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-\right.\right. \\
 & 2 b(b c-a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\right. \\
 & \left.\left.\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\left(a^2 d^2 \operatorname{Log}[a+b x]-b(d(-b c+a d) x+b c^2 \operatorname{Log}[c+d x])\right)\right)- \\
 & 2 b^2 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)- \\
 & 2 a^2 d^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right\}+ \\
 & B^2 d^2 n^2\left(\frac{1}{3} x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2-\frac{1}{6 b^3 d^3}\left(4 d(-b c+a d)(b c+a d)(a+b x)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)-\right.\right. \\
 & 2 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+4 b(b c-a d)(b c+a d)(c+d x)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)- \\
 & 2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+d^2(b c-a d)\left(b x(2 a-b x)+2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-2 a^2 \operatorname{Log}[a+b x]\right)+ \\
 & b^2(b c-a d)\left(d x(-2 c+d x)-2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+2 c^2 \operatorname{Log}[c+d x]\right)- \\
 & 2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \\
 & \left.(b d(b c-a d) x(-2 b c-2 a d+b d x)-2 a^3 d^3 \operatorname{Log}[a+b x]+2 b^3 c^3 \operatorname{Log}[c+d x]\right)+ \\
 & 4 b^3 c^3\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)+ \\
 & 4 a^3 d^3\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right\}
 \end{aligned}$$

### Problem 172: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i+d i x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{a g+b g x} d x$$

Optimal (type 4, 572 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{B d (b c - a d) i^2 n (a + b x) \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g} + \\
 & \frac{d (b c - a d) i^2 (a + b x) \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^3 g} + \frac{i^2 (c + d x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 b g} + \\
 & \frac{2 B (b c - a d)^2 i^2 n \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log}\left[ \frac{b c - a d}{b (c+d x)} \right]}{b^3 g} + \frac{B^2 (b c - a d)^2 i^2 n^2 \text{Log}[c + d x]}{b^3 g} + \\
 & \frac{B (b c - a d)^2 i^2 n \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log}\left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} - \\
 & \frac{(b c - a d)^2 i^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \text{Log}\left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} + \\
 & \frac{2 B^2 (b c - a d)^2 i^2 n^2 \text{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^3 g} - \frac{B^2 (b c - a d)^2 i^2 n^2 \text{PolyLog}\left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} + \\
 & \frac{2 B (b c - a d)^2 i^2 n \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog}\left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g} + \\
 & \frac{2 B^2 (b c - a d)^2 i^2 n^2 \text{PolyLog}\left[ 3, \frac{b (c+d x)}{d (a+b x)} \right]}{b^3 g}
 \end{aligned}$$

Result (type 4, 2784 leaves):

$$\begin{aligned}
 & \frac{1}{12 b^3 g} i^2 \left( 12 b d (2 b c - a d) x \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 + \right. \\
 & \quad 6 b^2 d^2 x^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\
 & \quad 12 (b c - a d)^2 \text{Log}[a + b x] \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 - \\
 & \quad 24 b B c n \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \left( a d \text{Log}\left[ \frac{a}{b} + x \right]^2 - 2 a d \text{Log}\left[ \frac{a}{b} + x \right] \right. \\
 & \quad \left. \left( 1 + \text{Log}[a + b x] \right) + 2 \left( -b c + a d + \text{Log}\left[ \frac{c}{d} + x \right] \left( b c + a d \text{Log}[a + b x] - a d \text{Log}\left[ \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \right) + \\
 & \quad \left. \left( -b d x + a d \text{Log}[a + b x] \right) \text{Log}\left[ \frac{a+b x}{c+d x} \right] - 2 a d \text{PolyLog}\left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) + \\
 & \quad 12 b^2 B c^2 n \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left( \text{Log}\left[ \frac{a}{b} + x \right]^2 - 2 \text{Log}[a + b x] \left( \text{Log}\left[ \frac{a}{b} + x \right] - \text{Log}\left[ \frac{c}{d} + x \right] - \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - \right. \\
 & \quad \left. 2 \left( \text{Log}\left[ \frac{c}{d} + x \right] \text{Log}\left[ \frac{d (a+b x)}{-b c + a d} \right] + \text{PolyLog}\left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) + \\
 & \quad 6 B n \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log}\left[ \frac{a+b x}{c+d x} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -4 a d^2 (a+b x) \left( -1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 a b d (c+d x) \left( -1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + \right. \\
 & d^2 \left( b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a+b x] \right) - \\
 & 2 d^2 \left( b x (-2 a + b x) + 2 a^2 \operatorname{Log}[a+b x] \right) \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \\
 & b^2 \left( d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c+d x] \right) - \\
 & 4 a^2 d^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \left. \right) - \\
 & 8 b B^2 c n^2 \left( a d \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 3 d (a+b x) \left( 2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \right. \\
 & 3 b (c+d x) \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - \\
 & 3 d (b x - a \operatorname{Log}[a+b x]) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 + \\
 & 6 \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c+d x] + \right. \\
 & \operatorname{Log}\left[\frac{a}{b} + x\right] \left( -d (a+b x) + d (a+b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + \\
 & (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \left. \right) - 3 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left( -2 b c + 2 a d - 2 d (a+b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + a d \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right. \\
 & 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \left( b (c+d x) - a d \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] \right) - 2 a d \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \left. \right) - \\
 & 3 a d \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + \right. \\
 & 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \left. \right) + 3 a d \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \right. \\
 & 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \left. \right) \left. \right) + \\
 & B^2 n^2 \left( 4 a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^3 - 12 a d^2 (a+b x) \left( 2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \right. \\
 & 3 d^2 (a+b x) \left( 7 a - b x + (-6 a + 2 b x) \operatorname{Log}\left[\frac{a}{b} + x\right] + 2 (a - b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right) - \\
 & 12 a b d (c+d x) \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) - \\
 & 3 b^2 (c+d x) \left( 7 c - d x + (-6 c + 2 d x) \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 (c - d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) + \\
 & 6 d^2 \left( b x (-2 a + b x) + 2 a^2 \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 - \\
 & 6 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -4 a d^2 (a+b x) \left( -1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 a^2 d^2 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 4 a b d (c+d x) \right. \\
 & \quad \left. \left( -1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + d^2 \left( b x (2 a - b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b} + x\right] - 2 a^2 \operatorname{Log}[a+b x] \right) + \right. \\
 & \quad \left. b^2 \left( d x (-2 c + d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 c^2 \operatorname{Log}[c+d x] \right) - \right. \\
 & \quad \left. 4 a^2 d^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) + \\
 6 & \left( 2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - 2 a b d^2 x \operatorname{Log}\left[\frac{c}{d} + x\right] + b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d} + x\right] - \right. \\
 & \quad a^2 d^2 \operatorname{Log}[a+b x] - b^2 c^2 \operatorname{Log}[c+d x] - 2 a b c d \operatorname{Log}[c+d x] - \\
 & \quad \operatorname{Log}\left[\frac{a}{b} + x\right] \left( b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \operatorname{Log}\left[\frac{c}{d} + x\right] + \right. \\
 & \quad \left. \left. (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + 2 (b^2 c^2 - a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + \right. \\
 & \quad 4 a d \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c+d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \\
 & \quad \left. \left( -d(a+b x) + d(a+b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + (b c - a d) \right. \\
 & \quad \left. \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) - 2 a^2 d^2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - \right. \\
 & \quad \left. 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) + \\
 12 & a^2 d^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - \right. \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \right) + \\
 4 & b^2 B^2 c^2 n^2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \right. \\
 & \quad 3 \operatorname{Log}[a+b x] \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 + \\
 & \quad 3 \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( -\operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + 6 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + \\
 & \quad 6 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - 3 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \quad \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) - \\
 & \quad \left. 6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \right)
 \end{aligned}$$

Problem 173: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i + d i x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(a g + b g x)^2} dx$$

Optimal (type 4, 472 leaves, 11 steps):

$$\begin{aligned} & - \frac{2 B^2 (b c - a d) i^2 n^2 (c + d x)}{b^2 g^2 (a + b x)} - \frac{2 B (b c - a d) i^2 n (c + d x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^2 g^2 (a + b x)} + \\ & \frac{d^2 i^2 (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^3 g^2} - \frac{(b c - a d) i^2 (c + d x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^2 g^2 (a + b x)} + \\ & \frac{2 B d (b c - a d) i^2 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ \frac{b c - a d}{b (c + d x)} \right]}{b^3 g^2} - \\ & \frac{2 d (b c - a d) i^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \log \left[ 1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g^2} + \\ & \frac{2 B^2 d (b c - a d) i^2 n^2 \text{PolyLog} \left[ 2, \frac{d (a + b x)}{b (c + d x)} \right]}{b^3 g^2} + \\ & \frac{4 B d (b c - a d) i^2 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog} \left[ 2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g^2} + \\ & \frac{4 B^2 d (b c - a d) i^2 n^2 \text{PolyLog} \left[ 3, \frac{b (c + d x)}{d (a + b x)} \right]}{b^3 g^2} \end{aligned}$$

Result (type 4, 3257 leaves):

$$\begin{aligned} & \frac{d^2 i^2 x \left( A + B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{b^2 g^2} + \\ & \frac{2 d (b c - a d) i^2 \log [a + b x] \left( A + B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{b^3 g^2} + \frac{1}{b^3 g^2 (a + b x)} \\ & \left( -A^2 b^2 c^2 i^2 + 2 a A^2 b c d i^2 - a^2 A^2 d^2 i^2 - 2 A b^2 B c^2 i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\ & \quad 4 a A b B c d i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) - 2 a^2 A B d^2 i^2 \\ & \quad \left. \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) - b^2 B^2 c^2 i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 + 2 a b B^2 \right. \\ & \quad \left. c d i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 - a^2 B^2 d^2 i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) + \\ & \left( B^2 c^2 i^2 n^2 \left( -2 b c + 2 a d - 2 d (a + b x) \log [a + b x] + (-2 b c + 2 a d) \log \left[ \frac{a+b x}{c+d x} \right] - \right. \right. \\ & \quad \left. \left. b (c + d x) \log \left[ \frac{a+b x}{c+d x} \right]^2 + 2 d (a + b x) \log [c + d x] \right) \right) / (b (b c - a d) g^2 (a + b x)) + \frac{1}{g^2} \end{aligned}$$

$$2 B c^2 i^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) \left( - \frac{\left( \frac{a}{b} + x \right) \left( \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{\left( a + b x \right)^2 \text{Log} \left[ \frac{a}{b} + x \right]} - \frac{\frac{b \left( \frac{c}{d} + x \right) \text{Log} \left[ \frac{c}{d} + x \right]}{\left( -a + \frac{b c}{d} \right)^2 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} + \frac{\text{Log} \left[ 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right]}{-a + \frac{b c}{d}} - \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right]}{b \left( a + b x \right)} \right) +$$

$$\frac{1}{g^2} 2 B d^2 i^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) \left( \frac{\left( \frac{a}{b} + x \right) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^2} - \frac{a \text{Log} \left[ \frac{a}{b} + x \right]^2}{b^3} - \frac{a^2 \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^3 \left( a + b x \right)} - \frac{\left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{b^2} - \frac{\left( a^2 \left( \left( -b c + a d \right) \text{Log} \left[ \frac{c}{d} + x \right] + d \left( a + b x \right) \left( \text{Log} \left[ a + b x \right] - \text{Log} \left[ c + d x \right] \right) \right)}{\left( b^3 \left( b c - a d \right) \left( a + b x \right) \right) + \frac{1}{b^3}} \right) \left( b x - \frac{a^2}{a + b x} - 2 a \text{Log} \left[ a + b x \right] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) + \frac{2 a \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d \left( a + b x \right)}{-b c + a d} \right] + \text{PolyLog} \left[ 2, \frac{b \left( c + d x \right)}{b c - a d} \right] \right)}{b^3} \right) + \frac{1}{g^2}$$

$$4 B c d i^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) \left( \frac{\text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^2} + \frac{a \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^2 \left( a + b x \right)} + \frac{\left( a \left( \left( -b c + a d \right) \text{Log} \left[ \frac{c}{d} + x \right] + d \left( a + b x \right) \left( \text{Log} \left[ a + b x \right] - \text{Log} \left[ c + d x \right] \right) \right)}{\left( b^2 \left( b c - a d \right) \left( a + b x \right) \right) + \frac{1}{b^2}} \right) \left( \frac{a}{a + b x} + \text{Log} \left[ a + b x \right] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) - \frac{\text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d \left( a + b x \right)}{-b c + a d} \right] + \text{PolyLog} \left[ 2, \frac{b \left( c + d x \right)}{b c - a d} \right]}{b^2} \right) +$$

$$\frac{1}{g^2} B^2 d^2 i^2 n^2 \left( - \frac{2 a \text{Log} \left[ \frac{a}{b} + x \right]^3}{3 b^3} + \frac{\left( a + b x \right) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^3} - \right)$$



$$\begin{aligned}
 & \frac{a^2 \left( 2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^3 (a + b x)} + \frac{(c + d x) \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{b^2 d} + \frac{1}{b^3} \\
 & \left( b x - \frac{a^2}{a + b x} - 2 a \operatorname{Log}[a + b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2 + \\
 & \left( a^2 \left( -b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) / \left( b^3 (b c - a d) (a + b x) \right) + \\
 & 2 \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \left( \frac{\left(\frac{a}{b} + x\right) (-1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{b^2} - \right. \\
 & \quad \frac{a \operatorname{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 (1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{b^3 (a + b x)} - \frac{\left(\frac{c}{d} + x\right) (-1 + \operatorname{Log}\left[\frac{c}{d} + x\right])}{b^2} - \\
 & \quad \left. \left( a^2 \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) \right) / \\
 & \quad \left( b^3 (b c - a d) (a + b x) \right) + \frac{2 a \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right)}{b^3} \Bigg) - \\
 & 2 \left( \frac{1}{b^3 d} \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c + d x] + \operatorname{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
 & \quad \left. \left( -d (a + b x) + d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + (b c - a d) \right. \\
 & \quad \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \Bigg) + \left( a^2 \left( d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + \right. \right. \right. \\
 & \quad \left. \left. d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + \right. \\
 & \quad \left. \left. d (a + b x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \Bigg) / \\
 & \quad \left( 2 b^3 (b c - a d) (a + b x) \right) - \frac{1}{b^3} a \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) \right) - \\
 & \quad \left( 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) \Bigg) - \\
 & \quad \frac{1}{b^3} 2 a \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - \right. \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right) \Bigg) + \\
 & \frac{1}{g^2} 2 B^2 c d i^2 n^2 \left( \frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^3}{3 b^2} + \frac{a \left( 2 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^2 (a + b x)} + \frac{1}{b^2} \right)
 \end{aligned}$$



$$\begin{aligned} & - \frac{2 B^2 d i^2 n^2 (c+d x)}{b^2 g^3 (a+b x)} - \frac{B^2 i^2 n^2 (c+d x)^2}{4 b g^3 (a+b x)^2} - \frac{2 B d i^2 n (c+d x) \left( A+B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^2 g^3 (a+b x)} - \\ & \frac{B i^2 n (c+d x)^2 \left( A+B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b g^3 (a+b x)^2} - \frac{d i^2 (c+d x) \left( A+B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^2 g^3 (a+b x)} - \\ & \frac{i^2 (c+d x)^2 \left( A+B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 b g^3 (a+b x)^2} - \frac{d^2 i^2 \left( A+B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \log \left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^3 g^3} + \\ & \frac{2 B d^2 i^2 n \left( A+B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog} \left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^3 g^3} + \frac{2 B^2 d^2 i^2 n^2 \text{PolyLog} \left[ 3, \frac{b(c+d x)}{d(a+b x)} \right]}{b^3 g^3} \end{aligned}$$

Result (type 4, 4257 leaves):

$$\begin{aligned} & \frac{d^2 i^2 \log [a+b x] \left( A+B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{b^3 g^3} + \frac{1}{b^3 g^3 (a+b x)} \\ & 2 \left( -A^2 b c d i^2 + a A^2 d^2 i^2 - 2 A b B c d i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) + 2 a A B d^2 i^2 \right. \\ & \quad \left. \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) - b B^2 c d i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \right. \\ & \quad \left. a B^2 d^2 i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) + \frac{1}{2 b^3 g^3 (a+b x)^2} \\ & \left( -A^2 b^2 c^2 i^2 + 2 a A^2 b c d i^2 - a^2 A^2 d^2 i^2 - 2 A b^2 B c^2 i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\ & \quad 4 a A b B c d i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) - 2 a^2 A B d^2 i^2 \\ & \quad \left. \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) - b^2 B^2 c^2 i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 + 2 a b B^2 \right. \\ & \quad \left. c d i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 - a^2 B^2 d^2 i^2 \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) - \\ & \left( B^2 c^2 i^2 n^2 \left( b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a+b x)^2 \log [a+b x] + \right. \right. \\ & \quad 2 (b c - a d) (b c - 3 a d - 2 b d x) \log \left[ \frac{a+b x}{c+d x} \right] + 2 b (c+d x) (b c - 2 a d - b d x) \log \left[ \frac{a+b x}{c+d x} \right]^2 + \\ & \quad \left. \left. 6 a^2 d^2 \log [c+d x] + 12 a b d^2 x \log [c+d x] + 6 b^2 d^2 x^2 \log [c+d x] \right) \right) / \\ & \left( 4 b (b c - a d)^2 g^3 (a+b x)^2 + \frac{1}{g^3} 2 B c^2 i^2 n \left( A+B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right) \right) \\ & \left( - \frac{\left( \frac{a}{b} + x \right) \left( 2 \log \left[ \frac{a}{b} + x \right] + 4 \log \left[ \frac{a}{b} + x \right]^2 \right)}{8 (a+b x)^3 \log \left[ \frac{a}{b} + x \right]} - \frac{1}{2 b} \right) \end{aligned}$$

$$\left( \frac{b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{bc}{d} \right)^3 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right)} - \left( \frac{b^2 \left( \frac{c}{d} + x \right)^2}{\left( -a + \frac{bc}{d} \right)^4 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right)^2} + \frac{2 b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{bc}{d} \right)^3 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right)} \right) \text{Log} \left[ \frac{c}{d} + x \right] -$$

$$\frac{\text{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right]}{\left( -a + \frac{bc}{d} \right)^2} \right) - \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right]}{2 b (a + b x)^2} \right) +$$

$$\frac{1}{g^3} 4 B c d i^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) \left( - \frac{1 + \text{Log} \left[ \frac{a}{b} + x \right]}{b^2 (a + b x)} + \right.$$

$$\frac{a \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] \right)}{4 b^2 (a + b x)^2} - \frac{(-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + d (a + b x) (\text{Log} [a + b x] - \text{Log} [c + d x])}{b^2 (b c - a d) (a + b x)} -$$

$$\frac{a \left( \text{Log} \left[ \frac{c}{d} + x \right] + \frac{d (a + b x) (b c - a d + d (a + b x) \text{Log} [a + b x] - d (a + b x) \text{Log} [c + d x])}{(b c - a d)^2} \right)}{2 b^2 (a + b x)^2} -$$

$$\left. \frac{(a + 2 b x) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)}{2 b^2 (a + b x)^2} \right) +$$

$$\frac{1}{g^3} 2 B d^2 i^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right)$$

$$\left( \frac{\text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^3} + \frac{2 a \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^3 (a + b x)} - \frac{a^2 \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] \right)}{4 b^3 (a + b x)^2} + \right.$$

$$\left. \frac{\left( 2 a \left( (-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + d (a + b x) (\text{Log} [a + b x] - \text{Log} [c + d x]) \right) \right)}{b^3 (b c - a d) (a + b x)} + \frac{a^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] + \frac{d (a + b x) (b c - a d + d (a + b x) \text{Log} [a + b x] - d (a + b x) \text{Log} [c + d x])}{(b c - a d)^2} \right)}{2 b^3 (a + b x)^2} \right) +$$

$$\frac{1}{2 b^3} \left( \frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \text{Log} [a + b x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) -$$

$$\frac{\text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right]}{b^3} \right) +$$

$$\frac{1}{g^3} 2 B^2 c d i^2 n^2 \left( - \frac{2 + 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2}{b^2 (a + b x)} + \frac{a \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] + 2 \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{4 b^2 (a + b x)^2} + \right.$$

$$\left. 2 \left( - \frac{1 + \text{Log} \left[ \frac{a}{b} + x \right]}{b^2 (a + b x)} + \frac{a \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] \right)}{4 b^2 (a + b x)^2} - \left( (-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + \right. \right.$$

$$\begin{aligned}
 & \frac{d (a+b x) (\text{Log}[a+b x] - \text{Log}[c+d x])}{(b^2 (b c - a d) (a+b x))} - \\
 & \frac{a \left( \text{Log}\left[\frac{c}{d} + x\right] + \frac{d (a+b x) (b c - a d + d (a+b x) \text{Log}[a+b x] - d (a+b x) \text{Log}[c+d x])}{(b c - a d)^2} \right)}{2 b^2 (a+b x)^2} \Bigg) \\
 & \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) - \\
 & \frac{(a+2 b x) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right)^2}{2 b^2 (a+b x)^2} - \\
 & 2 \left( \left( d (a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a+b x) (\text{Log}[a+b x] - \text{Log}[c+d x]) \right) \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a+b x) \text{Log}\left[\frac{b (c+d x)}{b c - a d}\right] \right) \right) - \\
 & \frac{2 d (a+b x) \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right]}{(2 b^2 (b c - a d) (a+b x))} + \\
 & \left( a \left( -d (-b c + a d) (a+b x) + (b c - a d)^2 \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right) \text{Log}\left[\frac{c}{d} + x\right] + d^2 (a+b x)^2 \right. \right. \\
 & \quad \left. \left. \text{Log}[a+b x] - d^2 (a+b x)^2 \text{Log}[c+d x] + d (a+b x) \left( d (a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + \right. \right. \right. \\
 & \quad \left. \left. \left. 2 (b c - a d) \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - 2 d (a+b x) \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c+d x)}{b c - a d}\right] + \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \right) \right) \right) \Bigg) / \left( 4 b^2 (b c - a d)^2 (a+b x)^2 \right) + \\
 & \left( -b (c+d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] + \right. \\
 & \quad \left. 2 d (a+b x) \text{PolyLog}\left[2, \frac{b (c+d x)}{b c - a d}\right] \right) / (b^2 (b c - a d) (a+b x)) + \\
 & \left( a \left( b (c+d x) (-2 a d + b (c-d x)) \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a+b x)^2 \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] \left( b (c+d x) + d (a+b x) \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] \right) \right) + \right. \\
 & \quad \left. \left. 2 d^2 (a+b x)^2 \text{PolyLog}\left[2, \frac{b (c+d x)}{b c - a d}\right] \right) \Bigg) / \left( 2 b^2 (b c - a d)^2 (a+b x)^2 \right) + \\
 & \frac{1}{g^3} B^2 d^2 i^2 n^2 \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^3}{3 b^3} + \frac{2 a \left( 2 + 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b^3 (a+b x)} - \right. \\
 & \quad \left. \frac{a^2 \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] + 2 \text{Log}\left[\frac{a}{b} + x\right]^2 \right)}{4 b^3 (a+b x)^2} + \frac{1}{2 b^3} \right)
 \end{aligned}$$

$$\left( \frac{a (3 a + 4 b x)}{(a + b x)^2} + 2 \operatorname{Log}[a + b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2 -$$

$$\left( 2 a \left( -b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) / (b^3 (b c - a d) (a + b x)) -$$

$$\left( a^2 \left( b (c + d x) (-2 a d + b (c - d x)) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a + b x)^2 \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 d (a + b x) \operatorname{Log}\left[\frac{c}{d} + x\right] \left( b (c + d x) + d (a + b x) \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \right) + 2 d^2 (a + b x)^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) /$$

$$\left( 2 b^3 (b c - a d)^2 (a + b x)^2 \right) + 2 \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)$$

$$\left( \frac{\operatorname{Log}\left[\frac{a}{b} + x\right]^2}{2 b^3} + \frac{2 a (1 + \operatorname{Log}\left[\frac{a}{b} + x\right])}{b^3 (a + b x)} - \frac{a^2 (1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right])}{4 b^3 (a + b x)^2} \right) +$$

$$\left( 2 a \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) / (b^3 (b c - a d) (a + b x)) +$$

$$\frac{a^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{2 b^3 (a + b x)^2} -$$

$$\left. \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^3} \right) -$$

$$2 \left( - \left( \left( a \left( d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\operatorname{Log}[a + b x] - \operatorname{Log}[c + d x]) \right) \right) - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) /$$

$$(b^3 (b c - a d) (a + b x)) - \left( a^2 \left( -d (-b c + a d) (a + b x) + (b c - a d)^2 (1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]) \operatorname{Log}\left[\frac{c}{d} + x\right] + d^2 (a + b x)^2 \operatorname{Log}[a + b x] - d^2 (a + b x)^2 \operatorname{Log}[c + d x] + d (a + b x) \left( d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 (b c - a d) \left( 1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) - 2 d (a + b x) \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right) \right) /$$

$$\left( 4 b^3 (b c - a d)^2 (a + b x)^2 \right) + \frac{1}{2 b^3} \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - \right.$$

$$\begin{aligned} & 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \Big) + \\ & \frac{1}{b^3}\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]-\right. \\ & \left.2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right) \Big) \end{aligned}$$

### Problem 175: Result more than twice size of optimal antiderivative.

$$\int \frac{(c i+d i x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(a g+b g x)^4} d x$$

Optimal (type 3, 157 leaves, 3 steps):

$$\begin{aligned} & -\frac{2 B^2 i^2 n^2(c+d x)^3}{27(b c-a d) g^4(a+b x)^3}- \\ & \frac{2 B i^2 n(c+d x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{9(b c-a d) g^4(a+b x)^3}-\frac{i^2(c+d x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{3(b c-a d) g^4(a+b x)^3} \end{aligned}$$

Result (type 3, 774 leaves):

$$\begin{aligned} & -\frac{1}{27 b^3(b c-a d) g^4(a+b x)^3} i^2\left(9 b^3 B^2 n^2(c+d x)^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+\right. \\ & 6 B d^3 n(a+b x)^3 \operatorname{Log}[a+b x]\left(3 A+B n+3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+ \\ & 6 B(b c-a d) n\left(a^2 d^2+a b d(c+3 d x)+b^2\left(c^2+3 c d x+3 d^2 x^2\right)\right) \\ & \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\left(3 A+B n+3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+ \\ & (b c-a d)^3\left(9 A^2+6 A B n+2 B^2 n^2+9 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-6 B n(3 A+B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+\right. \\ & \left.9 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(3 A+B n-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)+3 d(b c-a d)^2 \\ & (a+b x)\left(9 A^2+6 A B n+2 B^2 n^2+9 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-6 B n(3 A+B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+\right. \\ & \left.9 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(3 A+B n-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)+3 d^2(b c-a d) \\ & (a+b x)^2\left(9 A^2+6 A B n+2 B^2 n^2+9 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-6 B n(3 A+B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+\right. \\ & \left.9 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(3 A+B n-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)- \\ & \left.6 B d^3 n(a+b x)^3\left(3 A+B n+3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \operatorname{Log}[c+d x]\right) \end{aligned}$$

**Problem 176: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(a g + b g x)^5} dx$$

Optimal (type 3, 319 leaves, 7 steps):

$$\begin{aligned} & \frac{2 B^2 d i^2 n^2 (c+d x)^3}{27 (b c - a d)^2 g^5 (a+b x)^3} - \frac{b B^2 i^2 n^2 (c+d x)^4}{32 (b c - a d)^2 g^5 (a+b x)^4} + \\ & \frac{2 B d i^2 n (c+d x)^3 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{9 (b c - a d)^2 g^5 (a+b x)^3} - \frac{b B i^2 n (c+d x)^4 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{8 (b c - a d)^2 g^5 (a+b x)^4} + \\ & \frac{d i^2 (c+d x)^3 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{3 (b c - a d)^2 g^5 (a+b x)^3} - \frac{b i^2 (c+d x)^4 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 (b c - a d)^2 g^5 (a+b x)^4} \end{aligned}$$

Result (type 3, 982 leaves):



$$\begin{aligned}
 & \frac{1}{864 b^3 (b c - a d)^2 g^5 (a + b x)^4} \\
 & i^2 \left( -72 b^3 B^2 n^2 (c + d x)^3 (3 b c - 4 a d - b d x) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 12 B d^3 (b c - a d) n (a + b x)^3 \right. \\
 & \quad \left( 12 A + 7 B n + 12 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 12 B d^4 n (a + b x)^4 \operatorname{Log}[a + b x] \\
 & \quad \left( 12 A + 7 B n + 12 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - 4 d (b c - a d)^3 (a + b x) \\
 & \quad \left( 144 A^2 + 60 A B n + 11 B^2 n^2 + 144 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 12 B n (24 A + 5 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 144 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 12 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 24 A + 5 B n - 24 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - \\
 & \quad 6 d^2 (b c - a d)^2 (a + b x)^2 \left( 72 A^2 + 12 A B n - 5 B^2 n^2 + 72 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - \right. \\
 & \quad \left. 12 B n (12 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 72 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \\
 & \quad \left. 12 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 12 A + B n - 12 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - \\
 & \quad 27 (b c - a d)^4 \left( 8 A^2 + 4 A B n + B^2 n^2 + 8 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 4 B n (4 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 8 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 4 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 4 A + B n - 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
 & \quad 12 B (b c - a d) n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left( 12 B d^3 n (a + b x)^3 + 6 d^2 (-b c + a d) (a + b x)^2 \right. \\
 & \quad \left. \left( 12 A + B n + 12 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 12 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) - \right. \\
 & \quad \left. 9 (b c - a d)^3 \left( 4 A + B n + 4 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) - \right. \\
 & \quad \left. 4 d (b c - a d)^2 (a + b x) \left( 24 A + 5 B n + 24 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \right) - \\
 & \quad \left. 12 B d^4 n (a + b x)^4 \left( 12 A + 7 B n + 12 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \operatorname{Log}[c + d x] \right)
 \end{aligned}$$

**Problem 177: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^2 (A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])^2}{(a g + b g x)^6} dx$$

Optimal (type 3, 493 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{2 B^2 d^2 i^2 n^2 (c+d x)^3}{27 (b c-a d)^3 g^6 (a+b x)^3} + \frac{b B^2 d i^2 n^2 (c+d x)^4}{16 (b c-a d)^3 g^6 (a+b x)^4} - \frac{2 b^2 B^2 i^2 n^2 (c+d x)^5}{125 (b c-a d)^3 g^6 (a+b x)^5} - \\
 & \frac{2 B d^2 i^2 n (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{9 (b c-a d)^3 g^6 (a+b x)^3} + \frac{b B d i^2 n (c+d x)^4 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{4 (b c-a d)^3 g^6 (a+b x)^4} - \\
 & \frac{2 b^2 B i^2 n (c+d x)^5 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{25 (b c-a d)^3 g^6 (a+b x)^5} - \frac{d^2 i^2 (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{3 (b c-a d)^3 g^6 (a+b x)^3} + \\
 & \frac{b d i^2 (c+d x)^4 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 (b c-a d)^3 g^6 (a+b x)^4} - \frac{b^2 i^2 (c+d x)^5 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{5 (b c-a d)^3 g^6 (a+b x)^5}
 \end{aligned}$$

Result (type 3, 1107 leaves):

$$\begin{aligned}
 & \frac{1}{54000 b^3 (b c - a d)^3 g^6 (a + b x)^5} \\
 & i^2 \left( -1800 b^3 B^2 n^2 (c + d x)^3 (10 a^2 d^2 + 5 a b d (-3 c + d x) + b^2 (6 c^2 - 3 c d x + d^2 x^2)) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \\
 & 30 B d^3 (b c - a d)^2 n (a + b x)^3 \left( 60 A - 13 B n + 60 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) - \\
 & 60 B d^4 (b c - a d) n (a + b x)^4 \left( 60 A + 47 B n + 60 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) - \\
 & 60 B d^5 n (a + b x)^5 \operatorname{Log}[a + b x] \left( 60 A + 47 B n + 60 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) - \\
 & 20 d^2 (b c - a d)^3 (a + b x)^2 \left( 900 A^2 + 60 A B n - 43 B^2 n^2 + 900 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - \right. \\
 & \quad \left. 60 B n (30 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 900 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \\
 & \quad \left. 60 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 30 A + B n - 30 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) - 135 d (b c - a d)^4 (a + b x) \\
 & \left( 200 A^2 + 60 A B n + 7 B^2 n^2 + 200 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 20 B n (20 A + 3 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 200 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 20 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 20 A + 3 B n - 20 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) - 432 \\
 & (b c - a d)^5 \left( 25 A^2 + 10 A B n + 2 B^2 n^2 + 25 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 10 B n (5 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 25 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 10 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 5 A + B n - 5 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) + \\
 & 60 B (b c - a d) n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left( 30 B d^3 (b c - a d) n (a + b x)^3 - 60 B d^4 n (a + b x)^4 + \right. \\
 & \quad \left. 45 d (-b c + a d)^3 (a + b x) \left( 20 A + 3 B n + 20 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 20 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) - \right. \\
 & \quad \left. 72 (b c - a d)^4 \left( 5 A + B n + 5 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 5 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) - \right. \\
 & \quad \left. 20 d^2 (b c - a d)^2 (a + b x)^2 \left( 30 A + B n + 30 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) \right) + \\
 & \left. 60 B d^5 n (a + b x)^5 \left( 60 A + 47 B n + 60 B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]\right) \right) \operatorname{Log}[c + d x] \right)
 \end{aligned}$$

**Problem 178: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^3 (c i + d i x)^3 \left( A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2 dx$$

Optimal (type 4, 1172 leaves, 22 steps):

$$\begin{aligned}
 & \frac{5 B^2 (b c - a d)^6 g^3 i^3 n^2 x}{84 b^3 d^3} + \frac{B^2 (b c - a d)^3 g^3 i^3 n^2 (a + b x)^4}{140 b^4} - \frac{29 B^2 (b c - a d)^5 g^3 i^3 n^2 (c + d x)^2}{840 b^2 d^4} + \\
 & \frac{47 B^2 (b c - a d)^4 g^3 i^3 n^2 (c + d x)^3}{1260 b d^4} - \frac{13 B^2 (b c - a d)^3 g^3 i^3 n^2 (c + d x)^4}{420 d^4} +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{b B^2 (b c - a d)^2 g^3 i^3 n^2 (c + d x)^5}{105 d^4} - \frac{B (b c - a d)^4 g^3 i^3 n (a + b x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{210 b^4 d} - \\
 & \frac{3 B (b c - a d)^3 g^3 i^3 n (a + b x)^4 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{140 b^4} - \\
 & \frac{B (b c - a d)^2 g^3 i^3 n (a + b x)^4 (c + d x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{35 b^3} + \\
 & \frac{2 B (b c - a d)^4 g^3 i^3 n (c + d x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{21 b d^4} - \\
 & \frac{3 B (b c - a d)^3 g^3 i^3 n (c + d x)^4 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{14 d^4} + \\
 & \frac{6 b B (b c - a d)^2 g^3 i^3 n (c + d x)^5 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{35 d^4} - \\
 & \frac{b^2 B (b c - a d) g^3 i^3 n (c + d x)^6 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{21 d^4} + \\
 & \frac{(b c - a d)^3 g^3 i^3 (a + b x)^4 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{140 b^4} + \\
 & \frac{(b c - a d)^2 g^3 i^3 (a + b x)^4 (c + d x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{35 b^3} + \\
 & \frac{(b c - a d) g^3 i^3 (a + b x)^4 (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{14 b^2} + \\
 & \frac{g^3 i^3 (a + b x)^4 (c + d x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{7 b} + \\
 & \frac{B (b c - a d)^5 g^3 i^3 n (a + b x)^2 \left( 3 A + B n + 3 B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{420 b^4 d^2} - \\
 & \frac{B (b c - a d)^6 g^3 i^3 n (a + b x) \left( 6 A + 5 B n + 6 B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{420 b^4 d^3} - \\
 & \frac{B (b c - a d)^7 g^3 i^3 n \left( 6 A + 11 B n + 6 B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{b c - a d}{b (c + d x)} \right]}{420 b^4 d^4} - \\
 & \frac{B^2 (b c - a d)^7 g^3 i^3 n^2 \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right]}{210 b^4 d^4} - \frac{11 B^2 (b c - a d)^7 g^3 i^3 n^2 \operatorname{Log}[c + d x]}{420 b^4 d^4} - \\
 & \frac{B^2 (b c - a d)^7 g^3 i^3 n^2 \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{70 b^4 d^4}
 \end{aligned}$$

Result (type 4, 5652 leaves):

$$\frac{1}{2520 b^4 d^4} g^3 i^3$$

$$\begin{aligned}
 & \left( -36 b^7 B^2 c^7 n^2 + 288 a b^6 B^2 c^6 d n^2 - 1008 a^2 b^5 B^2 c^5 d^2 n^2 + 756 a^3 b^4 B^2 c^4 d^3 n^2 + 756 a^4 b^3 B^2 c^3 d^4 n^2 - \right. \\
 & 1008 a^5 b^2 B^2 c^2 d^5 n^2 + 288 a^6 b B^2 c d^6 n^2 - 36 a^7 B^2 d^7 n^2 + 2520 a^3 A^2 b^4 c^3 d^4 x - 36 A b^7 B c^6 d n x + \\
 & 252 a A b^6 B c^5 d^2 n x - 756 a^2 A b^5 B c^4 d^3 n x + 756 a^4 A b^3 B c^2 d^5 n x - 252 a^5 A b^2 B c d^6 n x + \\
 & 36 a^6 A b B d^7 n x + 36 b^7 B^2 c^6 d n^2 x - 270 a b^6 B^2 c^5 d^2 n^2 x + 876 a^2 b^5 B^2 c^4 d^3 n^2 x - \\
 & 1284 a^3 b^4 B^2 c^3 d^4 n^2 x + 876 a^4 b^3 B^2 c^2 d^5 n^2 x - 270 a^5 b^2 B^2 c d^6 n^2 x + 36 a^6 b B^2 d^7 n^2 x + \\
 & 3780 a^2 A^2 b^5 c^3 d^4 x^2 + 3780 a^3 A^2 b^4 c^2 d^5 x^2 + 18 A b^7 B c^5 d^2 n x^2 - 126 a A b^6 B c^4 d^3 n x^2 - \\
 & 1512 a^2 A b^5 B c^3 d^4 n x^2 + 1512 a^3 A b^4 B c^2 d^5 n x^2 + 126 a^4 A b^3 B c d^6 n x^2 - 18 a^5 A b^2 B d^7 n x^2 - \\
 & 27 b^7 B^2 c^5 d^2 n^2 x^2 + 201 a b^6 B^2 c^4 d^3 n^2 x^2 - 174 a^2 b^5 B^2 c^3 d^4 n^2 x^2 - 174 a^3 b^4 B^2 c^2 d^5 n^2 x^2 + \\
 & 201 a^4 b^3 B^2 c d^6 n^2 x^2 - 27 a^5 b^2 B^2 d^7 n^2 x^2 + 2520 a A^2 b^6 c^3 d^4 x^3 + 7560 a^2 A^2 b^5 c^2 d^5 x^3 + \\
 & 2520 a^3 A^2 b^4 c d^6 x^3 - 12 A b^7 B c^4 d^3 n x^3 - 1176 a A b^6 B c^3 d^4 n x^3 + 1176 a^3 A b^4 B c d^6 n x^3 + \\
 & 12 a^4 A b^3 B d^7 n x^3 + 22 b^7 B^2 c^4 d^3 n^2 x^3 + 152 a b^6 B^2 c^3 d^4 n^2 x^3 - 348 a^2 b^5 B^2 c^2 d^5 n^2 x^3 + \\
 & 152 a^3 b^4 B^2 c d^6 n^2 x^3 + 22 a^4 b^3 B^2 d^7 n^2 x^3 + 630 A^2 b^7 c^3 d^4 x^4 + 5670 a A^2 b^6 c^2 d^5 x^4 + \\
 & 5670 a^2 A^2 b^5 c d^6 x^4 + 630 a^3 A^2 b^4 d^7 x^4 - 306 A b^7 B c^3 d^4 n x^4 - 882 a A b^6 B c^2 d^5 n x^4 + \\
 & 882 a^2 A b^5 B c d^6 n x^4 + 306 a^3 A b^4 B d^7 n x^4 + 60 b^7 B^2 c^3 d^4 n^2 x^4 - 60 a b^6 B^2 c^2 d^5 n^2 x^4 - \\
 & 60 a^2 b^5 B^2 c d^6 n^2 x^4 + 60 a^3 b^4 B^2 d^7 n^2 x^4 + 1512 A^2 b^7 c^2 d^5 x^5 + 4536 a A^2 b^6 c d^6 x^5 + \\
 & 1512 a^2 A^2 b^5 d^7 x^5 - 360 A b^7 B c^2 d^5 n x^5 + 360 a^2 A b^5 B d^7 n x^5 + 24 b^7 B^2 c^2 d^5 n^2 x^5 - \\
 & 48 a b^6 B^2 c d^6 n^2 x^5 + 24 a^2 b^5 B^2 d^7 n^2 x^5 + 1260 A^2 b^7 c d^6 x^6 + 1260 a A^2 b^6 d^7 x^6 - \\
 & 120 A b^7 B c d^6 n x^6 + 120 a A b^6 B d^7 n x^6 + 360 A^2 b^7 d^7 x^7 - 36 a b^6 B^2 c^6 d n^2 \text{Log}\left[\frac{a}{b} + x\right] + \\
 & 252 a^2 b^5 B^2 c^5 d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] - 756 a^3 b^4 B^2 c^4 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 756 a^5 b^2 B^2 c^2 d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right] - \\
 & 252 a^6 b B^2 c d^6 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 36 a^7 B^2 d^7 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 630 a^4 b^3 B^2 c^3 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & 378 a^5 b^2 B^2 c^2 d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + 126 a^6 b B^2 c d^6 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 18 a^7 B^2 d^7 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + \\
 & 36 b^7 B^2 c^7 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 252 a b^6 B^2 c^6 d n^2 \text{Log}\left[\frac{c}{d} + x\right] + 756 a^2 b^5 B^2 c^5 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] - \\
 & 756 a^4 b^3 B^2 c^3 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] + 252 a^5 b^2 B^2 c^2 d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 36 a^6 b B^2 c d^6 n^2 \text{Log}\left[\frac{c}{d} + x\right] - \\
 & 18 b^7 B^2 c^7 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + 126 a b^6 B^2 c^6 d n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - 378 a^2 b^5 B^2 c^5 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + \\
 & 630 a^3 b^4 B^2 c^4 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + 1260 a^4 A b^3 B c^3 d^4 n \text{Log}[a + b x] - \\
 & 756 a^5 A b^2 B c^2 d^5 n \text{Log}[a + b x] + 252 a^6 A b B c d^6 n \text{Log}[a + b x] - 36 a^7 A B d^7 n \text{Log}[a + b x] - \\
 & 18 a^2 b^5 B^2 c^5 d^2 n^2 \text{Log}[a + b x] + 114 a^3 b^4 B^2 c^4 d^3 n^2 \text{Log}[a + b x] + \\
 & 642 a^4 b^3 B^2 c^3 d^4 n^2 \text{Log}[a + b x] - 990 a^5 b^2 B^2 c^2 d^5 n^2 \text{Log}[a + b x] + 288 a^6 b B^2 c d^6 n^2 \text{Log}[a + b x] - \\
 & 36 a^7 B^2 d^7 n^2 \text{Log}[a + b x] - 1260 a^4 b^3 B^2 c^3 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\
 & 756 a^5 b^2 B^2 c^2 d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] - 252 a^6 b B^2 c d^6 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\
 & 36 a^7 B^2 d^7 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 1260 a^4 b^3 B^2 c^3 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 756 a^5 b^2 B^2 c^2 d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + 252 a^6 b B^2 c d^6 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 36 a^7 B^2 d^7 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 1260 a^4 b^3 B^2 c^3 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & 756 a^5 b^2 B^2 c^2 d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 252 a^6 b B^2 c d^6 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] +
 \end{aligned}$$

$$\begin{aligned}
& 36 a^7 B^2 d^7 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+5040 a^3 A b^4 B c^3 d^4 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 36 b^7 B^2 c^6 d n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+252 a b^6 B^2 c^5 d^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 756 a^2 b^5 B^2 c^4 d^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+756 a^4 b^3 B^2 c^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 252 a^5 b^2 B^2 c d^6 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+36 a^6 b B^2 d^7 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 7560 a^2 A b^5 B c^3 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+7560 a^3 A b^4 B c^2 d^5 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 18 b^7 B^2 c^5 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-126 a b^6 B^2 c^4 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 1512 a^2 b^5 B^2 c^3 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+1512 a^3 b^4 B^2 c^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 126 a^4 b^3 B^2 c d^6 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-18 a^5 b^2 B^2 d^7 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 5040 a A b^6 B c^3 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+15120 a^2 A b^5 B c^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 5040 a^3 A b^4 B c d^6 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-12 b^7 B^2 c^4 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 1176 a b^6 B^2 c^3 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+1176 a^3 b^4 B^2 c d^6 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 12 a^4 b^3 B^2 d^7 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+1260 A b^7 B c^3 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 11340 a A b^6 B c^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+11340 a^2 A b^5 B c d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 1260 a^3 A b^4 B d^7 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-306 b^7 B^2 c^3 d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 882 a b^6 B^2 c^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+882 a^2 b^5 B^2 c d^6 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 306 a^3 b^4 B^2 d^7 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+3024 A b^7 B c^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 9072 a A b^6 B c d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+3024 a^2 A b^5 B d^7 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 360 b^7 B^2 c^2 d^5 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+360 a^2 b^5 B^2 d^7 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 2520 A b^7 B c d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+2520 a A b^6 B d^7 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 120 b^7 B^2 c d^6 n x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+120 a b^6 B^2 d^7 n x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 720 A b^7 B d^7 x^7 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+1260 a^4 b^3 B^2 c^3 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
& 756 a^5 b^2 B^2 c^2 d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
& 252 a^6 b B^2 c d^6 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-36 a^7 B^2 d^7 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+
\end{aligned}$$

$$\begin{aligned}
 & 2520 a^3 b^4 B^2 c^3 d^4 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 3780 a^2 b^5 B^2 c^3 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 3780 a^3 b^4 B^2 c^2 d^5 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2520 a b^6 B^2 c^3 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 7560 a^2 b^5 B^2 c^2 d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2520 a^3 b^4 B^2 c d^6 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 630 b^7 B^2 c^3 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 5670 a b^6 B^2 c^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 5670 a^2 b^5 B^2 c d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 630 a^3 b^4 B^2 d^7 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 1512 b^7 B^2 c^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 4536 a b^6 B^2 c d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 1512 a^2 b^5 B^2 d^7 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 1260 b^7 B^2 c d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 1260 a b^6 B^2 d^7 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 360 b^7 B^2 d^7 x^7 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 36 A b^7 B c^7 n \operatorname{Log}[c+d x] - 252 a A b^6 B c^6 d n \operatorname{Log}[c+d x] + 756 a^2 A b^5 B c^5 d^2 n \operatorname{Log}[c+d x] - \\
 & 1260 a^3 A b^4 B c^4 d^3 n \operatorname{Log}[c+d x] - 36 b^7 B^2 c^7 n^2 \operatorname{Log}[c+d x] + 288 a b^6 B^2 c^6 d n^2 \operatorname{Log}[c+d x] - \\
 & 990 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}[c+d x] + 642 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}[c+d x] + \\
 & 114 a^4 b^3 B^2 c^3 d^4 n^2 \operatorname{Log}[c+d x] - 18 a^5 b^2 B^2 c^2 d^5 n^2 \operatorname{Log}[c+d x] - \\
 & 36 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 252 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] - \\
 & 756 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + 1260 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x] + \\
 & 36 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 252 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 756 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 1260 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] + \\
 & 36 b^7 B^2 c^7 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - 252 a b^6 B^2 c^6 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + \\
 & 756 a^2 b^5 B^2 c^5 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] - \\
 & 1260 a^3 b^4 B^2 c^4 d^3 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x] + 36 b^7 B^2 c^7 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 252 a b^6 B^2 c^6 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 756 a^2 b^5 B^2 c^5 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] - \\
 & 1260 a^3 b^4 B^2 c^4 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 36 b^4 B^2 c^4 \left(b^3 c^3 - 7 a b^2 c^2 d + 21 a^2 b c d^2 - 35 a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 & 36 a^4 B^2 d^4 \left(-35 b^3 c^3 + 21 a b^2 c^2 d - 7 a^2 b c d^2 + a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 179: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x)^2 (c i + d i x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 976 leaves, 20 steps):

$$\begin{aligned} & - \frac{7 B^2 (b c - a d)^5 g^2 i^3 n^2 x}{180 b^3 d^2} - \frac{7 B^2 (b c - a d)^4 g^2 i^3 n^2 (c + d x)^2}{360 b^2 d^3} - \frac{B^2 (b c - a d)^3 g^2 i^3 n^2 (c + d x)^3}{60 b d^3} + \\ & \frac{B^2 (b c - a d)^2 g^2 i^3 n^2 (c + d x)^4}{60 d^3} - \frac{B (b c - a d)^4 g^2 i^3 n (a + b x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{60 b^4 d} - \\ & \frac{B (b c - a d)^3 g^2 i^3 n (a + b x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{30 b^4} - \\ & \frac{B (b c - a d)^4 g^2 i^3 n (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{10 b^2 d^3} + \\ & \frac{B (b c - a d)^3 g^2 i^3 n (c + d x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{45 b d^3} + \\ & \frac{7 B (b c - a d)^2 g^2 i^3 n (c + d x)^4 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{60 d^3} - \\ & \frac{b B (b c - a d) g^2 i^3 n (c + d x)^5 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{15 d^3} + \\ & \frac{(b c - a d)^3 g^2 i^3 (a + b x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2}{60 b^4} + \\ & \frac{(b c - a d)^2 g^2 i^3 (a + b x)^3 (c + d x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2}{20 b^3} + \\ & \frac{(b c - a d) g^2 i^3 (a + b x)^3 (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2}{10 b^2} + \\ & \frac{g^2 i^3 (a + b x)^3 (c + d x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2}{6 b} + \\ & \frac{B (b c - a d)^5 g^2 i^3 n (a + b x) \left( 2 A + B n + 2 B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)}{60 b^4 d^2} + \\ & \frac{B (b c - a d)^6 g^2 i^3 n \left( 2 A + 3 B n + 2 B \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{b c - a d}{b (c + d x)} \right]}{60 b^4 d^3} + \\ & \frac{B^2 (b c - a d)^6 g^2 i^3 n^2 \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right]}{36 b^4 d^3} + \frac{11 B^2 (b c - a d)^6 g^2 i^3 n^2 \operatorname{Log}[c + d x]}{180 b^4 d^3} + \\ & \frac{B^2 (b c - a d)^6 g^2 i^3 n^2 \operatorname{PolyLog}\left[ 2, \frac{d (a + b x)}{b (c + d x)} \right]}{30 b^4 d^3} \end{aligned}$$

Result (type 4, 4611 leaves):

$$\frac{1}{360 b^4 d^3}$$



$$\begin{aligned}
 & g^2 i^3 \left( 12 b^6 B^2 c^6 n^2 - 84 a b^5 B^2 c^5 d n^2 + 12 a^2 b^4 B^2 c^4 d^2 n^2 + 240 a^3 b^3 B^2 c^3 d^3 n^2 - 252 a^4 b^2 B^2 c^2 d^4 n^2 + \right. \\
 & 84 a^5 b B^2 c d^5 n^2 - 12 a^6 B^2 d^6 n^2 + 360 a^2 A^2 b^4 c^3 d^3 x + 12 A b^6 B c^5 d n x - 72 a A b^5 B c^4 d^2 n x - \\
 & 60 a^2 A b^4 B c^3 d^3 n x + 180 a^3 A b^3 B c^2 d^4 n x - 72 a^4 A b^2 B c d^5 n x + 12 a^5 A b B d^6 n x - \\
 & 16 b^6 B^2 c^5 d n^2 x + 102 a b^5 B^2 c^4 d^2 n^2 x - 194 a^2 b^4 B^2 c^3 d^3 n^2 x + 154 a^3 b^3 B^2 c^2 d^4 n^2 x - \\
 & 54 a^4 b^2 B^2 c d^5 n^2 x + 8 a^5 b B^2 d^6 n^2 x + 360 a A^2 b^5 c^3 d^3 x^2 + 540 a^2 A^2 b^4 c^2 d^4 x^2 - 6 A b^6 B c^4 d^2 n x^2 - \\
 & 204 a A b^5 B c^3 d^3 n x^2 + 180 a^2 A b^4 B c^2 d^4 n x^2 + 36 a^3 A b^3 B c d^5 n x^2 - 6 a^4 A b^2 B d^6 n x^2 + \\
 & 11 b^6 B^2 c^4 d^2 n^2 x^2 + 10 a b^5 B^2 c^3 d^3 n^2 x^2 - 60 a^2 b^4 B^2 c^2 d^4 n^2 x^2 + 46 a^3 b^3 B^2 c d^5 n^2 x^2 - \\
 & 7 a^4 b^2 B^2 d^6 n^2 x^2 + 120 A^2 b^6 c^3 d^3 x^3 + 720 a A^2 b^5 c^2 d^4 x^3 + 360 a^2 A^2 b^4 c d^5 x^3 - 76 A b^6 B c^3 d^3 n x^3 - \\
 & 84 a A b^5 B c^2 d^4 n x^3 + 156 a^2 A b^4 B c d^5 n x^3 + 4 a^3 A b^3 B d^6 n x^3 + 18 b^6 B^2 c^3 d^3 n^2 x^3 - \\
 & 30 a b^5 B^2 c^2 d^4 n^2 x^3 + 6 a^2 b^4 B^2 c d^5 n^2 x^3 + 6 a^3 b^3 B^2 d^6 n^2 x^3 + 270 A^2 b^6 c^2 d^4 x^4 + \\
 & 540 a A^2 b^5 c d^5 x^4 + 90 a^2 A^2 b^4 d^6 x^4 - 78 A b^6 B c^2 d^4 n x^4 + 36 a A b^5 B c d^5 n x^4 + 42 a^2 A b^4 B d^6 n x^4 + \\
 & 6 b^6 B^2 c^2 d^4 n^2 x^4 - 12 a b^5 B^2 c d^5 n^2 x^4 + 6 a^2 b^4 B^2 d^6 n^2 x^4 + 216 A^2 b^6 c d^5 x^5 + 144 a A^2 b^5 d^6 x^5 - \\
 & 24 A b^6 B c d^5 n x^5 + 24 a A b^5 B d^6 n x^5 + 60 A^2 b^6 d^6 x^6 + 12 a b^5 B^2 c^5 d n^2 \text{Log}\left[\frac{a}{b} + x\right] - \\
 & 72 a^2 b^4 B^2 c^4 d^2 n^2 \text{Log}\left[\frac{a}{b} + x\right] - 60 a^3 b^3 B^2 c^3 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 180 a^4 b^2 B^2 c^2 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right] - \\
 & 72 a^5 b B^2 c d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 12 a^6 B^2 d^6 n^2 \text{Log}\left[\frac{a}{b} + x\right] + 120 a^3 b^3 B^2 c^3 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & 90 a^4 b^2 B^2 c^2 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + 36 a^5 b B^2 c d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - 6 a^6 B^2 d^6 n^2 \text{Log}\left[\frac{a}{b} + x\right]^2 - \\
 & 12 b^6 B^2 c^6 n^2 \text{Log}\left[\frac{c}{d} + x\right] + 72 a b^5 B^2 c^5 d n^2 \text{Log}\left[\frac{c}{d} + x\right] + 60 a^2 b^4 B^2 c^4 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right] - \\
 & 180 a^3 b^3 B^2 c^3 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] + 72 a^4 b^2 B^2 c^2 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] - 12 a^5 b B^2 c d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] + \\
 & 6 b^6 B^2 c^6 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 - 36 a b^5 B^2 c^5 d n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + 90 a^2 b^4 B^2 c^4 d^2 n^2 \text{Log}\left[\frac{c}{d} + x\right]^2 + \\
 & 240 a^3 A b^3 B c^3 d^3 n \text{Log}[a + b x] - 180 a^4 A b^2 B c^2 d^4 n \text{Log}[a + b x] + \\
 & 72 a^5 A b B c d^5 n \text{Log}[a + b x] - 12 a^6 A B d^6 n \text{Log}[a + b x] + 6 a^2 b^4 B^2 c^4 d^2 n^2 \text{Log}[a + b x] + \\
 & 128 a^3 b^3 B^2 c^3 d^3 n^2 \text{Log}[a + b x] - 186 a^4 b^2 B^2 c^2 d^4 n^2 \text{Log}[a + b x] + 60 a^5 b B^2 c d^5 n^2 \text{Log}[a + b x] - \\
 & 8 a^6 B^2 d^6 n^2 \text{Log}[a + b x] - 240 a^3 b^3 B^2 c^3 d^3 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\
 & 180 a^4 b^2 B^2 c^2 d^4 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] - 72 a^5 b B^2 c d^5 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + \\
 & 12 a^6 B^2 d^6 n^2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] + 240 a^3 b^3 B^2 c^3 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 180 a^4 b^2 B^2 c^2 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] + 72 a^5 b B^2 c d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - \\
 & 12 a^6 B^2 d^6 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}[a + b x] - 240 a^3 b^3 B^2 c^3 d^3 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & 180 a^4 b^2 B^2 c^2 d^4 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] - 72 a^5 b B^2 c d^5 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + \\
 & 12 a^6 B^2 d^6 n^2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a + b x)}{-b c + a d}\right] + 720 a^2 A b^4 B c^3 d^3 x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + \\
 & 12 b^6 B^2 c^5 d n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 72 a b^5 B^2 c^4 d^2 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
 & 60 a^2 b^4 B^2 c^3 d^3 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] + 180 a^3 b^3 B^2 c^2 d^4 n x \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] -
 \end{aligned}$$

$$\begin{aligned}
 & 72 a^4 b^2 B^2 c d^5 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 12 a^5 b B^2 d^6 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 720 a A b^5 B c^3 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 1080 a^2 A b^4 B c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 6 b^6 B^2 c^4 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 204 a b^5 B^2 c^3 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 180 a^2 b^4 B^2 c^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 36 a^3 b^3 B^2 c d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 6 a^4 b^2 B^2 d^6 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 240 A b^6 B c^3 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 1440 a A b^5 B c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 720 a^2 A b^4 B c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 76 b^6 B^2 c^3 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 84 a b^5 B^2 c^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 156 a^2 b^4 B^2 c d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 4 a^3 b^3 B^2 d^6 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 540 A b^6 B c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 1080 a A b^5 B c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 180 a^2 A b^4 B d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 78 b^6 B^2 c^2 d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 36 a b^5 B^2 c d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 42 a^2 b^4 B^2 d^6 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 432 A b^6 B c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 288 a A b^5 B d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 24 b^6 B^2 c d^5 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 24 a b^5 B^2 d^6 n x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 120 A b^6 B d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 240 a^3 b^3 B^2 c^3 d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - \\
 & 180 a^4 b^2 B^2 c^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 72 a^5 b B^2 c d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 12 a^6 B^2 d^6 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + \\
 & 360 a^2 b^4 B^2 c^3 d^3 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 360 a b^5 B^2 c^3 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 540 a^2 b^4 B^2 c^2 d^4 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 120 b^6 B^2 c^3 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 720 a b^5 B^2 c^2 d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 360 a^2 b^4 B^2 c d^5 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 270 b^6 B^2 c^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 540 a b^5 B^2 c d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 90 a^2 b^4 B^2 d^6 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 216 b^6 B^2 c d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + \\
 & 144 a b^5 B^2 d^6 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 60 b^6 B^2 d^6 x^6 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 - \\
 & 12 A b^6 B c^6 n \operatorname{Log}[c+d x] + 72 a A b^5 B c^5 d n \operatorname{Log}[c+d x] - 180 a^2 A b^4 B c^4 d^2 n \operatorname{Log}[c+d x] + \\
 & 16 b^6 B^2 c^6 n^2 \operatorname{Log}[c+d x] - 108 a b^5 B^2 c^5 d n^2 \operatorname{Log}[c+d x] + 66 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}[c+d x] + \\
 & 32 a^3 b^3 B^2 c^3 d^3 n^2 \operatorname{Log}[c+d x] - 6 a^4 b^2 B^2 c^2 d^4 n^2 \operatorname{Log}[c+d x] +
 \end{aligned}$$

$$\begin{aligned}
 & 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] + \\
 & 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[c + d x] - 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] + \\
 & 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[c + d x] - \\
 & 12 b^6 B^2 c^6 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c + d x] + 72 a b^5 B^2 c^5 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c + d x] - \\
 & 180 a^2 b^4 B^2 c^4 d^2 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c + d x] - 12 b^6 B^2 c^6 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \\
 & 72 a b^5 B^2 c^5 d n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] - 180 a^2 b^4 B^2 c^4 d^2 n^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] - \\
 & 12 b^4 B^2 c^4 (b^2 c^2 - 6 a b c d + 15 a^2 d^2) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + \\
 & 12 a^3 B^2 d^3 (-20 b^3 c^3 + 15 a b^2 c^2 d - 6 a^2 b c d^2 + a^3 d^3) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]
 \end{aligned}$$

**Problem 180: Result more than twice size of optimal antiderivative.**

$$\int (a g + b g x) (c i + d i x)^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 dx$$

Optimal (type 4, 786 leaves, 19 steps):

$$\begin{aligned} & \frac{B^2 (b c - a d)^4 g i^3 n^2 x}{60 b^3 d} + \frac{B^2 (b c - a d)^3 g i^3 n^2 (c + d x)^2}{30 b^2 d^2} + \\ & \frac{B^2 (b c - a d)^2 g i^3 n^2 (c + d x)^3}{30 b d^2} - \frac{B (b c - a d)^4 g i^3 n (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{10 b^4 d} - \\ & \frac{B (b c - a d)^3 g i^3 n (a + b x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{10 b^4} + \\ & \frac{3 B (b c - a d)^3 g i^3 n (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{20 b^2 d^2} + \\ & \frac{B (b c - a d)^2 g i^3 n (c + d x)^3 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{30 b d^2} - \\ & \frac{B (b c - a d) g i^3 n (c + d x)^4 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{10 d^2} + \\ & \frac{(b c - a d)^3 g i^3 (a + b x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{20 b^4} + \\ & \frac{(b c - a d)^2 g i^3 (a + b x)^2 (c + d x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{10 b^3} + \\ & \frac{3 (b c - a d) g i^3 (a + b x)^2 (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{20 b^2} + \\ & \frac{g i^3 (a + b x)^2 (c + d x)^3 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{5 b} - \\ & \frac{B (b c - a d)^5 g i^3 n \left( A + B n + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ \frac{b c - a d}{b (c + d x)} \right]}{10 b^4 d^2} - \frac{B^2 (b c - a d)^5 g i^3 n^2 \log \left[ \frac{a+b x}{c+d x} \right]}{12 b^4 d^2} - \\ & \frac{11 B^2 (b c - a d)^5 g i^3 n^2 \log [c + d x]}{60 b^4 d^2} - \frac{B^2 (b c - a d)^5 g i^3 n^2 \text{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{10 b^4 d^2} \end{aligned}$$

Result (type 4, 3427 leaves):

$$\begin{aligned} & \frac{1}{60 b^4 d^2} \\ & g i^3 \left( -6 b^5 B^2 c^5 n^2 - 24 a b^4 B^2 c^4 d n^2 + 90 a^2 b^3 B^2 c^3 d^2 n^2 - 90 a^3 b^2 B^2 c^2 d^3 n^2 + 36 a^4 b B^2 c d^4 n^2 - \right. \\ & 6 a^5 B^2 d^5 n^2 + 60 a A^2 b^4 c^3 d^2 x - 6 A b^5 B c^4 d n x - 30 a A b^4 B c^3 d^2 n x + 60 a^2 A b^3 B c^2 d^3 n x - \\ & 30 a^3 A b^2 B c d^4 n x + 6 a^4 A b B d^5 n x + 11 b^5 B^2 c^4 d n^2 x - 28 a b^4 B^2 c^3 d^2 n^2 x + 24 a^2 b^3 B^2 c^2 d^3 n^2 x - \\ & 8 a^3 b^2 B^2 c d^4 n^2 x + a^4 b B^2 d^5 n^2 x + 30 A^2 b^5 c^3 d^2 x^2 + 90 a A^2 b^4 c^2 d^3 x^2 - 27 A b^5 B c^3 d^2 n x^2 + \\ & 15 a A b^4 B c^2 d^3 n x^2 + 15 a^2 A b^3 B c d^4 n x^2 - 3 a^3 A b^2 B d^5 n x^2 + 8 b^5 B^2 c^3 d^2 n^2 x^2 - \\ & 18 a b^4 B^2 c^2 d^3 n^2 x^2 + 12 a^2 b^3 B^2 c d^4 n^2 x^2 - 2 a^3 b^2 B^2 d^5 n^2 x^2 + 60 A^2 b^5 c^2 d^3 x^3 + \\ & 60 a A^2 b^4 c d^4 x^3 - 22 A b^5 B c^2 d^3 n x^3 + 20 a A b^4 B c d^4 n x^3 + 2 a^2 A b^3 B d^5 n x^3 + 2 b^5 B^2 c^2 d^3 n^2 x^3 - \\ & 4 a b^4 B^2 c d^4 n^2 x^3 + 2 a^2 b^3 B^2 d^5 n^2 x^3 + 45 A^2 b^5 c d^4 x^4 + 15 a A^2 b^4 d^5 x^4 - 6 A b^5 B c d^4 n x^4 + \\ & \left. 6 a A b^4 B d^5 n x^4 + 12 A^2 b^5 d^5 x^5 - 6 a b^4 B^2 c^4 d n^2 \log \left[ \frac{a}{b} + x \right] - 30 a^2 b^3 B^2 c^3 d^2 n^2 \log \left[ \frac{a}{b} + x \right] + \right. \end{aligned}$$

$$\begin{aligned}
 & 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]-30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]+6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]+ \\
 & 30 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-30 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+15 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2- \\
 & 3 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+30 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]-6 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 3 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+15 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+60 a^2 A b^3 B c^3 d^2 n \operatorname{Log}[a+b x]- \\
 & 60 a^3 A b^2 B c^2 d^3 n \operatorname{Log}[a+b x]+30 a^4 A B c d^4 n \operatorname{Log}[a+b x]-6 a^5 A B d^5 n \operatorname{Log}[a+b x]+ \\
 & 27 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[a+b x]-37 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[a+b x]+11 a^4 b B^2 c d^4 n^2 \operatorname{Log}[a+b x]- \\
 & a^5 B^2 d^5 n^2 \operatorname{Log}[a+b x]-60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+ \\
 & 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]-30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+ \\
 & 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]+30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]- \\
 & 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]-60 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 60 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-30 a^4 b B^2 c d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 6 a^5 B^2 d^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+120 a A b^4 B c^3 d^2 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 6 b^5 B^2 c^4 d n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-30 a b^4 B^2 c^3 d^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 60 a^2 b^3 B^2 c^2 d^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-30 a^3 b^2 B^2 c d^4 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 6 a^4 b B^2 d^5 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+60 A b^5 B c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 180 a A b^4 B c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-27 b^5 B^2 c^3 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 15 a b^4 B^2 c^2 d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+15 a^2 b^3 B^2 c d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 3 a^3 b^2 B^2 d^5 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+120 A b^5 B c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 120 a A b^4 B c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-22 b^5 B^2 c^2 d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 20 a b^4 B^2 c d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+2 a^2 b^3 B^2 d^5 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 90 A b^5 B c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+30 a A b^4 B d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 6 b^5 B^2 c d^4 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+6 a b^4 B^2 d^5 n x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 24 A b^5 B d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+60 a^2 b^3 B^2 c^3 d^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-
 \end{aligned}$$

$$\begin{aligned}
 & 60 a^3 b^2 B^2 c^2 d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+30 a^4 b B^2 c d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 6 a^5 B^2 d^5 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+60 a b^4 B^2 c^3 d^2 x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 30 b^5 B^2 c^3 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+90 a b^4 B^2 c^2 d^3 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 60 b^5 B^2 c^2 d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+60 a b^4 B^2 c d^4 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 45 b^5 B^2 c d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+15 a b^4 B^2 d^5 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 12 b^5 B^2 d^5 x^5 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+6 A b^5 B c^5 n \operatorname{Log}[c+d x]-30 a A b^4 B c^4 d n \operatorname{Log}[c+d x]- \\
 & 11 b^5 B^2 c^5 n^2 \operatorname{Log}[c+d x]+a b^4 B^2 c^4 d n^2 \operatorname{Log}[c+d x]+13 a^2 b^3 B^2 c^3 d^2 n^2 \operatorname{Log}[c+d x]- \\
 & 3 a^3 b^2 B^2 c^2 d^3 n^2 \operatorname{Log}[c+d x]-6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+ \\
 & 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]+6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]- \\
 & 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+6 b^5 B^2 c^5 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]- \\
 & 30 a b^4 B^2 c^4 d n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]+6 b^5 B^2 c^5 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
 & 30 a b^4 B^2 c^4 d n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+6 b^4 B^2 c^4(b c-5 a d) n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 6 a^2 B^2 d^2\left(-10 b^3 c^3+10 a b^2 c^2 d-5 a^2 b c d^2+a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 181: Result more than twice size of optimal antiderivative.**

$$\int (c i+d i x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 d x$$

Optimal (type 4, 454 leaves, 15 steps):

$$\frac{5 B^2 (b c - a d)^3 i^3 n^2 x}{12 b^3} + \frac{B^2 (b c - a d)^2 i^3 n^2 (c + d x)^2}{12 b^2 d} - \frac{B (b c - a d)^3 i^3 n (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^4} - \frac{B (b c - a d)^2 i^3 n (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{4 b^2 d} - \frac{B (b c - a d) i^3 n (c + d x)^3 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{6 b d} + \frac{i^3 (c + d x)^4 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{4 d} + \frac{5 B^2 (b c - a d)^4 i^3 n^2 \log \left[ \frac{a+b x}{c+d x} \right]}{12 b^4 d} + \frac{11 B^2 (b c - a d)^4 i^3 n^2 \log [c + d x]}{12 b^4 d} + \frac{B (b c - a d)^4 i^3 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{2 b^4 d} - \frac{B^2 (b c - a d)^4 i^3 n^2 \text{PolyLog} \left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{2 b^4 d}$$

Result (type 4, 2348 leaves):

$$\frac{1}{12 b^4 d} i^3 \left( -18 b^4 B^2 c^4 n^2 + 54 a b^3 B^2 c^3 d n^2 - 60 a^2 b^2 B^2 c^2 d^2 n^2 + 30 a^3 b B^2 c d^3 n^2 - 6 a^4 B^2 d^4 n^2 + 12 A^2 b^4 c^3 d x - 18 A b^4 B c^3 d n x + 36 a A b^3 B c^2 d^2 n x - 24 a^2 A b^2 B c d^3 n x + 6 a^3 A b B d^4 n x + 7 b^4 B^2 c^3 d n^2 x - 19 a b^3 B^2 c^2 d^2 n^2 x + 17 a^2 b^2 B^2 c d^3 n^2 x - 5 a^3 b B^2 d^4 n^2 x + 18 A^2 b^4 c^2 d^2 x^2 - 9 A b^4 B c^2 d^2 n x^2 + 12 a A b^3 B c d^3 n x^2 - 3 a^2 A b^2 B d^4 n x^2 + b^4 B^2 c^2 d^2 n^2 x^2 - 2 a b^3 B^2 c d^3 n^2 x^2 + a^2 b^2 B^2 d^4 n^2 x^2 + 12 A^2 b^4 c d^3 x^3 - 2 A b^4 B c d^3 n x^3 + 2 a A b^3 B d^4 n x^3 + 3 A^2 b^4 d^4 x^4 - 18 a b^3 B^2 c^3 d n^2 \log \left[ \frac{a}{b} + x \right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \log \left[ \frac{a}{b} + x \right] - 24 a^3 b B^2 c d^3 n^2 \log \left[ \frac{a}{b} + x \right] + 6 a^4 B^2 d^4 n^2 \log \left[ \frac{a}{b} + x \right] + 12 a b^3 B^2 c^3 d n^2 \log \left[ \frac{a}{b} + x \right]^2 - 18 a^2 b^2 B^2 c^2 d^2 n^2 \log \left[ \frac{a}{b} + x \right]^2 + 12 a^3 b B^2 c d^3 n^2 \log \left[ \frac{a}{b} + x \right]^2 - 3 a^4 B^2 d^4 n^2 \log \left[ \frac{a}{b} + x \right]^2 + 18 b^4 B^2 c^4 n^2 \log \left[ \frac{c}{d} + x \right] - 36 a b^3 B^2 c^3 d n^2 \log \left[ \frac{c}{d} + x \right] + 24 a^2 b^2 B^2 c^2 d^2 n^2 \log \left[ \frac{c}{d} + x \right] - 6 a^3 b B^2 c d^3 n^2 \log \left[ \frac{c}{d} + x \right] + 3 b^4 B^2 c^4 n^2 \log \left[ \frac{c}{d} + x \right]^2 + 24 a A b^3 B c^3 d n \log [a + b x] - 36 a^2 A b^2 B c^2 d^2 n \log [a + b x] + 24 a^3 A b B c d^3 n \log [a + b x] - 6 a^4 A B d^4 n \log [a + b x] + 9 a^2 b^2 B^2 c^2 d^2 n^2 \log [a + b x] - 14 a^3 b B^2 c d^3 n^2 \log [a + b x] + 5 a^4 B^2 d^4 n^2 \log [a + b x] - 24 a b^3 B^2 c^3 d n^2 \log \left[ \frac{a}{b} + x \right] \log [a + b x] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \log \left[ \frac{a}{b} + x \right] \log [a + b x] - 24 a^3 b B^2 c d^3 n^2 \log \left[ \frac{a}{b} + x \right] \log [a + b x] + 6 a^4 B^2 d^4 n^2 \log \left[ \frac{a}{b} + x \right] \log [a + b x] + 24 a b^3 B^2 c^3 d n^2 \log \left[ \frac{c}{d} + x \right] \log [a + b x] - 36 a^2 b^2 B^2 c^2 d^2 n^2 \log \left[ \frac{c}{d} + x \right] \log [a + b x] + 24 a^3 b B^2 c d^3 n^2 \log \left[ \frac{c}{d} + x \right] \log [a + b x] - 6 a^4 B^2 d^4 n^2 \log \left[ \frac{c}{d} + x \right] \log [a + b x] - 24 a b^3 B^2 c^3 d n^2 \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d(a+b x)}{-b c + a d} \right] + 36 a^2 b^2 B^2 c^2 d^2 n^2 \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d(a+b x)}{-b c + a d} \right] - 24 a^3 b B^2 c d^3 n^2 \log \left[ \frac{c}{d} + x \right] \log \left[ \frac{d(a+b x)}{-b c + a d} \right] +$$

$$\begin{aligned}
 & 6 a^4 B^2 d^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+24 A b^4 B c^3 d x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 18 b^4 B^2 c^3 d n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+36 a b^3 B^2 c^2 d^2 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]- \\
 & 24 a^2 b^2 B^2 c d^3 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+6 a^3 b B^2 d^4 n x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 36 A b^4 B c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-9 b^4 B^2 c^2 d^2 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 12 a b^3 B^2 c d^3 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-3 a^2 b^2 B^2 d^4 n x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 24 A b^4 B c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-2 b^4 B^2 c d^3 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 2 a b^3 B^2 d^4 n x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+6 A b^4 B d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 24 a b^3 B^2 c^3 d n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-36 a^2 b^2 B^2 c^2 d^2 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 24 a^3 b B^2 c d^3 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-6 a^4 B^2 d^4 n \operatorname{Log}[a+b x] \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+ \\
 & 12 b^4 B^2 c^3 d x \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+18 b^4 B^2 c^2 d^2 x^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+ \\
 & 12 b^4 B^2 c d^3 x^3 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+3 b^4 B^2 d^4 x^4 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2- \\
 & 6 A b^4 B c^4 n \operatorname{Log}[c+d x]-7 b^4 B^2 c^4 n^2 \operatorname{Log}[c+d x]+10 a b^3 B^2 c^3 d n^2 \operatorname{Log}[c+d x]- \\
 & 3 a^2 b^2 B^2 c^2 d^2 n^2 \operatorname{Log}[c+d x]+6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
 & 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-6 b^4 B^2 c^4 n \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \operatorname{Log}[c+d x]- \\
 & 6 b^4 B^2 c^4 n^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-6 b^4 B^2 c^4 n^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\
 & 6 a B^2 d\left(-4 b^3 c^3+6 a b^2 c^2 d-4 a^2 b c d^2+a^3 d^3\right) n^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]
 \end{aligned}$$

**Problem 182: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i+d i x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{a g+b g x} d x$$

Optimal (type 4, 762 leaves, 26 steps):



$$\begin{aligned} & \frac{B^2 d (b c - a d)^2 i^3 n^2 x}{3 b^3 g} - \frac{5 B d (b c - a d)^2 i^3 n (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b^4 g} - \\ & \frac{B (b c - a d) i^3 n (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 b^2 g} + \\ & \frac{d (b c - a d)^2 i^3 (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^4 g} + \frac{(b c - a d) i^3 (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 b^2 g} + \\ & \frac{i^3 (c + d x)^3 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{3 b g} + \frac{2 B (b c - a d)^3 i^3 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ \frac{b c - a d}{b (c+d x)} \right]}{b^4 g} + \\ & \frac{B^2 (b c - a d)^3 i^3 n^2 \log \left[ \frac{a+b x}{c+d x} \right]}{3 b^4 g} + \frac{2 B^2 (b c - a d)^3 i^3 n^2 \log [c + d x]}{b^4 g} + \\ & \frac{5 B (b c - a d)^3 i^3 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{3 b^4 g} - \\ & \frac{(b c - a d)^3 i^3 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \log \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g} + \\ & \frac{2 B^2 (b c - a d)^3 i^3 n^2 \text{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^4 g} - \frac{5 B^2 (b c - a d)^3 i^3 n^2 \text{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{3 b^4 g} + \\ & \frac{2 B (b c - a d)^3 i^3 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g} + \\ & \frac{2 B^2 (b c - a d)^3 i^3 n^2 \text{PolyLog} \left[ 3, \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g} \end{aligned}$$

Result (type 4, 5616 leaves):

$$\begin{aligned} & \frac{1}{b^3 g} d (3 b^2 c^2 - 3 a b c d + a^2 d^2) i^3 x \left( A + B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 + \\ & \frac{d^2 (3 b c - a d) i^3 x^2 \left( A + B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{2 b^2 g} + \\ & \frac{d^3 i^3 x^3 \left( A + B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{3 b g} + \\ & \frac{(b c - a d)^3 i^3 \log [a + b x] \left( A + B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{b^4 g} + \\ & \frac{1}{g} 2 B c^3 i^3 n \left( A + B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\ & \left( \frac{\log \left[ \frac{a}{b} + x \right]^2}{2 b} + \frac{\log [a + b x] \left( -\log \left[ \frac{a}{b} + x \right] + \log \left[ \frac{c}{d} + x \right] + \log \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right)}{b} \right) - \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[1 - \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right] + \text{PolyLog}\left[2, \frac{b\left(\frac{c+x}{d}\right)}{-a + \frac{bc}{d}}\right]\right)}{b} \right) + \frac{1}{g} 2 B d^3 i^3 n \\
 & \left( A + B \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) \left( \frac{a^2\left(\frac{a}{b} + x\right)\left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} - \frac{a^3 \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} - \right. \\
 & \frac{a^2\left(\frac{c}{d} + x\right)\left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} - \frac{a\left(-\frac{1}{2} b\left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a+b x]}{b^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{a+b x}{b}\right]\right)}{b^2} + \\
 & \left. - \frac{\frac{1}{3} b\left(\frac{a^2 x}{b^3} - \frac{a x^2}{2 b^2} + \frac{x^3}{3 b} - \frac{a^3 \text{Log}[a+b x]}{b^4}\right) + \frac{1}{3} x^3 \text{Log}\left[\frac{a+b x}{b}\right]}{b} \right) + \\
 & \frac{a\left(-\frac{1}{2} d\left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c+d x]}{d^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c+d x}{d}\right]\right)}{b^2} - \\
 & \left. - \frac{\frac{1}{3} d\left(\frac{c^2 x}{d^3} - \frac{c x^2}{2 d^2} + \frac{x^3}{3 d} - \frac{c^3 \text{Log}[c+d x]}{d^4}\right) + \frac{1}{3} x^3 \text{Log}\left[\frac{c+d x}{d}\right]}{b} \right) + \\
 & \left( \frac{a^2 x}{b^3} - \frac{a x^2}{2 b^2} + \frac{x^3}{3 b} - \frac{a^3 \text{Log}[a+b x]}{b^4} \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) + \\
 & \left. \frac{a^3\left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^4} \right) \right) + \\
 & \frac{1}{g} 6 B c d^2 i^3 n \left( A + B \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) \left( -\frac{a\left(\frac{a}{b} + x\right)\left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} + \right. \\
 & \frac{a^2 \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^3} + \frac{a\left(\frac{c}{d} + x\right)\left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} + \frac{-\frac{1}{2} b\left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a+b x]}{b^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{a+b x}{b}\right]}{b} - \\
 & \left. - \frac{\frac{1}{2} d\left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c+d x]}{d^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c+d x}{d}\right]}{b} \right) + \\
 & \left( -\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a+b x]}{b^3} \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) - \\
 & \left. \frac{a^2\left(\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^3} \right) \right) + \\
 & \frac{1}{g} 6 B c^2 d i^3 n \left( A + B \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) \\
 & \left( \frac{\left(\frac{a}{b} + x\right)\left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b} - \frac{a \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} - \frac{\left(\frac{c}{d} + x\right)\left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b} \right) + \\
 & \left( \frac{x}{b} - \frac{a \text{Log}[a+b x]}{b^2} \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{a \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^2} \right) + \\
 & \frac{1}{g} B^2 c^3 i^3 n^2 \left( \frac{\text{Log} \left[ \frac{a}{b} + x \right]^3}{3b} + \frac{\text{Log} [a+bx] \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)^2}{b} + \right. \\
 & 2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right) \\
 & \left. \left( \frac{\text{Log} \left[ \frac{a}{b} + x \right]^2}{2b} - \frac{\text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \text{PolyLog} \left[ 2, \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right]}{b} \right) + \frac{1}{b} \right. \\
 & 2 \left( \frac{1}{2} \text{Log} \left[ \frac{c}{d} + x \right]^2 \text{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] + \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] - \right. \\
 & \left. \text{PolyLog} \left[ 3, \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{bc}{d}} \right] \right) - \frac{1}{b} 2 \left( \frac{1}{2} \text{Log} \left[ \frac{a}{b} + x \right]^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{bd \left( \frac{c+x}{d} \right)}{bc-ad} \right] \right) \right) - \\
 & \left. \left. \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, -\frac{d(a+bx)}{bc-ad} \right] + \text{PolyLog} \left[ 3, -\frac{d(a+bx)}{bc-ad} \right] \right) \right) + \\
 & \frac{1}{g} B^2 d^3 i^3 n^2 \left( -\frac{a^3 \text{Log} \left[ \frac{a}{b} + x \right]^3}{3b^4} + \frac{a^2 (a+bx) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^4} - \frac{1}{4b^4} \right. \\
 & a(a+bx) \left( -7a+bx + (6a-2bx) \text{Log} \left[ \frac{a}{b} + x \right] - 2(a-bx) \text{Log} \left[ \frac{a}{b} + x \right]^2 \right) + \\
 & \frac{a^2 (c+dx) \left( 2 - 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{b^3 d} - \frac{1}{4b^2 d^2} \\
 & a(c+dx) \left( -7c+dx + (6c-2dx) \text{Log} \left[ \frac{c}{d} + x \right] - 2(c-dx) \text{Log} \left[ \frac{c}{d} + x \right]^2 \right) + \\
 & \frac{1}{54b^4} \left( bx(66a^2 - 15abx + 4b^2x^2) - 6bx(6a^2 - 3abx + 2b^2x^2) \text{Log} \left[ \frac{a}{b} + x \right] + \right. \\
 & 18(a^3 + b^3x^3) \text{Log} \left[ \frac{a}{b} + x \right]^2 - 66a^3 \text{Log} [a+bx] \left. \right) + \frac{1}{54b^3 d^3} \left( dx(66c^2 - 15cdx + 4d^2x^2) - \right. \\
 & \left. 6dx(6c^2 - 3cdx + 2d^2x^2) \text{Log} \left[ \frac{c}{d} + x \right] + 18(c^3 + d^3x^3) \text{Log} \left[ \frac{c}{d} + x \right]^2 - 66c^3 \text{Log} [c+dx] \right) + \\
 & \left( \frac{a^2 x}{b^3} - \frac{a x^2}{2b^2} + \frac{x^3}{3b} - \frac{a^3 \text{Log} [a+bx]}{b^4} \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)^2 + \\
 & 2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{a^2 \left( \frac{a}{b} + x \right) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^3} - \frac{a^3 \text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^4} - \frac{a^2 \left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{b^3} - \right. \\
 & \frac{a \left( -\frac{1}{2} b \left( -\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a+b x]}{b^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{a+b x}{b} \right] \right)}{b^2} + \\
 & \left. - \frac{\frac{1}{3} b \left( \frac{a^2 x}{b^3} - \frac{a x^2}{2 b^2} + \frac{x^3}{3 b} - \frac{a^3 \text{Log}[a+b x]}{b^4} \right) + \frac{1}{3} x^3 \text{Log} \left[ \frac{a+b x}{b} \right]}{b} \right) + \\
 & \frac{a \left( -\frac{1}{2} d \left( -\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c+d x]}{d^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{c+d x}{d} \right] \right)}{b^2} - \\
 & \left. - \frac{\frac{1}{3} d \left( \frac{c^2 x}{d^3} - \frac{c x^2}{2 d^2} + \frac{x^3}{3 d} - \frac{c^3 \text{Log}[c+d x]}{d^4} \right) + \frac{1}{3} x^3 \text{Log} \left[ \frac{c+d x}{d} \right]}{b} \right) + \\
 & \frac{a^3 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+b x)}{-b c+a d} \right] + \text{PolyLog} \left[ 2, \frac{b(c+d x)}{b c-a d} \right] \right)}{b^4} \Bigg) - 2 \left( \frac{1}{b^4 d} \right. \\
 & a^2 \left( a d + 2 b d x - b d x \text{Log} \left[ \frac{c}{d} + x \right] - b c \text{Log} [c+d x] + \text{Log} \left[ \frac{a}{b} + x \right] \left( -d(a+b x) + d(a+b x) \right. \right. \\
 & \left. \left. \text{Log} \left[ \frac{c}{d} + x \right] + (b c - a d) \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] \right) + (b c - a d) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] \right) - \\
 & \frac{1}{4 b^4 d^2} a \left( -2 a b c d - 3 b^2 c d x - 3 a b d^2 x + b^2 d^2 x^2 + 2 a b d^2 x \text{Log} \left[ \frac{c}{d} + x \right] - \right. \\
 & b^2 d^2 x^2 \text{Log} \left[ \frac{c}{d} + x \right] + a^2 d^2 \text{Log} [a+b x] + b^2 c^2 \text{Log} [c+d x] + 2 a b c d \text{Log} [c+d x] + \\
 & \left. \text{Log} \left[ \frac{a}{b} + x \right] \left( b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \text{Log} \left[ \frac{c}{d} + x \right] + (-2 b^2 c^2 + \right. \right. \\
 & \left. \left. 2 a^2 d^2) \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] \right) + (-2 b^2 c^2 + 2 a^2 d^2) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] \right) + \\
 & \frac{1}{108 b^4 d^3} \left( 36 a b^2 c^2 d + 48 b^3 c^2 d x + 36 a b^2 c d^2 x + 48 a^2 b d^3 x - 15 b^3 c d^2 x^2 - \right. \\
 & 15 a b^2 d^3 x^2 + 8 b^3 d^3 x^3 - 36 a^2 b d^3 x \text{Log} \left[ \frac{c}{d} + x \right] + 18 a b^2 d^3 x^2 \text{Log} \left[ \frac{c}{d} + x \right] - \\
 & 12 b^3 d^3 x^3 \text{Log} \left[ \frac{c}{d} + x \right] - 18 a^2 b c d^2 \text{Log} [a+b x] - 12 a^3 d^3 \text{Log} [a+b x] - \\
 & 12 b^3 c^3 \text{Log} [c+d x] - 18 a b^2 c^2 d \text{Log} [c+d x] - 36 a^2 b c d^2 \text{Log} [c+d x] + \\
 & 6 \text{Log} \left[ \frac{a}{b} + x \right] \left( -b^2 d (6 a c^2 + b x (6 c^2 - 3 c d x + 2 d^2 x^2)) + 6 d^3 (a^3 + b^3 x^3) \text{Log} \left[ \frac{c}{d} + x \right] + \right. \\
 & \left. 6 (b^3 c^3 - a^3 d^3) \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] + 36 (b^3 c^3 - a^3 d^3) \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] \right) - \\
 & \frac{1}{2 b^4} a^3 \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{b(c+d x)}{b c-a d} \right] \right) - 2 \text{Log} \left[ \frac{a}{b} + x \right] \right. \\
 & \left. \text{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c+a d} \right] + 2 \text{PolyLog} \left[ 3, \frac{d(a+b x)}{-b c+a d} \right] \right) \Bigg) -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{b^4} a^3 \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] - \right. \\
 & \quad \left. 2 \text{PolyLog} \left[ 3, \frac{b(c+dx)}{bc-ad} \right] \right) + \\
 & \frac{1}{g} 3 B^2 c d^2 i^3 n^2 \left( \frac{a^2 \text{Log} \left[ \frac{a}{b} + x \right]^3}{3 b^3} - \frac{a(a+bx) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^3} + \frac{1}{4 b^3} \right. \\
 & \quad (a+bx) \left( -7a+bx + (6a-2bx) \text{Log} \left[ \frac{a}{b} + x \right] - 2(a-bx) \text{Log} \left[ \frac{a}{b} + x \right]^2 \right) - \\
 & \quad \frac{a(c+dx) \left( 2 - 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{b^2 d} + \frac{1}{4 b d^2} \\
 & \quad (c+dx) \left( -7c+dx + (6c-2dx) \text{Log} \left[ \frac{c}{d} + x \right] - 2(c-dx) \text{Log} \left[ \frac{c}{d} + x \right]^2 \right) + \\
 & \quad \left( -\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \text{Log}[a+bx]}{b^3} \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right)^2 + \\
 & \quad 2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right) \\
 & \quad \left( -\frac{a \left( \frac{a}{b} + x \right) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^2} + \frac{a^2 \text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^3} + \right. \\
 & \quad \frac{a \left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{b^2} + \frac{-\frac{1}{2} b \left( -\frac{ax}{b^2} + \frac{x^2}{2b} + \frac{a^2 \text{Log}[a+bx]}{b^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{a+bx}{b} \right]}{b} - \\
 & \quad \left. \frac{-\frac{1}{2} d \left( -\frac{cx}{d^2} + \frac{x^2}{2d} + \frac{c^2 \text{Log}[c+dx]}{d^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{c+dx}{d} \right]}{b} - \right. \\
 & \quad \left. \frac{a^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog} \left[ 2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^3} \right) - 2 \left( -\frac{1}{b^3 d} \right. \\
 & \quad a \left( ad + 2bdx - bdx \text{Log} \left[ \frac{c}{d} + x \right] - bc \text{Log}[c+dx] + \text{Log} \left[ \frac{a}{b} + x \right] \left( -d(a+bx) + d(a+bx) \right. \right. \\
 & \quad \left. \left. \text{Log} \left[ \frac{c}{d} + x \right] + (bc-ad) \text{Log} \left[ \frac{b(c+dx)}{bc-ad} \right] \right) + (bc-ad) \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \\
 & \quad \frac{1}{4 b^3 d^2} \left( -2abcd - 3b^2cdx - 3abd^2x + b^2d^2x^2 + 2abd^2x \text{Log} \left[ \frac{c}{d} + x \right] - \right. \\
 & \quad b^2d^2x^2 \text{Log} \left[ \frac{c}{d} + x \right] + a^2d^2 \text{Log}[a+bx] + b^2c^2 \text{Log}[c+dx] + 2abcd \text{Log}[c+dx] + \\
 & \quad \text{Log} \left[ \frac{a}{b} + x \right] \left( bd(2ac+bx(2c-dx)) - 2d^2(a^2-b^2x^2) \text{Log} \left[ \frac{c}{d} + x \right] + (-2b^2c^2 + 2a^2d^2) \right. \\
 & \quad \left. \text{Log} \left[ \frac{b(c+dx)}{bc-ad} \right] \right) + (-2b^2c^2 + 2a^2d^2) \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right) + \frac{1}{2 b^3} \\
 & \quad a^2 \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{b(c+dx)}{bc-ad} \right] \right) - 2 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d(a+bx)}{-bc+ad} \right] \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] + \frac{1}{b^3} a^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \\
 & \left. 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) + \\
 & \frac{1}{g} 3 B^2 c^2 d i^3 n^2 \left( -\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^2} + \frac{(a+b x)\left(2-2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^2} + \right. \\
 & \left. \frac{(c+d x)\left(2-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{b d} + \right. \\
 & \left. \left(\frac{x}{b}-\frac{a \operatorname{Log}[a+b x]}{b^2}\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)^2 + \right. \\
 & \left. 2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right) \right. \\
 & \left. \left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b}-\frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^2}-\frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b} + \right. \right. \\
 & \left. \left. \frac{a\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^2}\right) - \right. \\
 & \left. 2\left(\frac{1}{b^2 d}\left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right]-b c \operatorname{Log}[c+d x]+\operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \right. \\
 & \left. \left. \left(-d(a+b x)+d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right]+(b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)+(b c-a d) \right. \right. \\
 & \left. \left. \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-\frac{1}{2 b^2} a\left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)\right) - \right. \right. \\
 & \left. \left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right) - \right. \\
 & \left. \frac{1}{b^2} a\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]- \right. \right. \\
 & \left. \left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right) \right)
 \end{aligned}$$

**Problem 183: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i+d i x)^3\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(a g+b g x)^2} d x$$

Optimal (type 4, 739 leaves, 17 steps):

$$\begin{aligned}
 & - \frac{2 B^2 (b c - a d)^2 i^3 n^2 (c + d x)}{b^3 g^2 (a + b x)} - \frac{B d^2 (b c - a d) i^3 n (a + b x) \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^4 g^2} \\
 & \frac{2 B (b c - a d)^2 i^3 n (c + d x) \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g^2 (a + b x)} + \\
 & \frac{2 d^2 (b c - a d) i^3 (a + b x) \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^4 g^2} - \\
 & \frac{(b c - a d)^2 i^3 (c + d x) \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^3 g^2 (a + b x)} + \frac{d i^3 (c + d x)^2 \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 b^2 g^2} + \\
 & \frac{4 B d (b c - a d)^2 i^3 n \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log\left[ \frac{b c - a d}{b (c + d x)} \right]}{b^4 g^2} + \frac{B^2 d (b c - a d)^2 i^3 n^2 \log(c + d x)}{b^4 g^2} + \\
 & \frac{B d (b c - a d)^2 i^3 n \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log\left[ 1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^4 g^2} - \\
 & \frac{3 d (b c - a d)^2 i^3 \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \log\left[ 1 - \frac{b (c + d x)}{d (a + b x)} \right]}{b^4 g^2} + \\
 & \frac{4 B^2 d (b c - a d)^2 i^3 n^2 \text{PolyLog}\left[ 2, \frac{d (a + b x)}{b (c + d x)} \right]}{b^4 g^2} - \frac{B^2 d (b c - a d)^2 i^3 n^2 \text{PolyLog}\left[ 2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^4 g^2} + \\
 & \frac{6 B d (b c - a d)^2 i^3 n \left( A + B \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog}\left[ 2, \frac{b (c + d x)}{d (a + b x)} \right]}{b^4 g^2} + \\
 & \frac{6 B^2 d (b c - a d)^2 i^3 n^2 \text{PolyLog}\left[ 3, \frac{b (c + d x)}{d (a + b x)} \right]}{b^4 g^2}
 \end{aligned}$$

Result (type 4, 5470 leaves):

$$\begin{aligned}
 & \frac{d^2 (3 b c - 2 a d) i^3 x \left( A + B \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{b^3 g^2} + \\
 & \frac{d^3 i^3 x^2 \left( A + B \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{2 b^2 g^2} + \frac{1}{b^4 g^2} \\
 & 3 d (b c - a d)^2 i^3 \log[a + b x] \left( A + B \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 + \\
 & \frac{1}{b^4 g^2 (a + b x)} \left( -A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3 - 2 A b^3 B c^3 i^3 \right. \\
 & \quad \left. \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + 6 a A b^2 B c^2 d i^3 \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right) - \\
 & 6 a^2 A b B c d^2 i^3 \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + 2 a^3 A B d^3 i^3 \\
 & \quad \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) - b^3 B^2 c^3 i^3 \left( \log\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right)^2 +
 \end{aligned}$$

$$\begin{aligned}
 & 3 a b^2 B^2 c^2 d i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - 3 a^2 b B^2 c d^2 i^3 \\
 & \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + a^3 B^2 d^3 i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\
 & \left( B^2 c^3 i^3 n^2 \left( -2 b c + 2 a d - 2 d (a+b x) \text{Log} [a+b x] + (-2 b c + 2 a d) \text{Log} \left[ \frac{a+b x}{c+d x} \right] - \right. \right. \\
 & \left. \left. b (c+d x) \text{Log} \left[ \frac{a+b x}{c+d x} \right]^2 + 2 d (a+b x) \text{Log} [c+d x] \right) \right) / (b (b c - a d) g^2 (a+b x)) + \frac{1}{g^2} \\
 & 2 B c^3 i^3 n \left( A+B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \left( - \frac{\left( \frac{a}{b} + x \right) \left( \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{(a+b x)^2 \text{Log} \left[ \frac{a}{b} + x \right]} - \right. \\
 & \left. \frac{\frac{b \left( \frac{c}{d} + x \right) \text{Log} \left[ \frac{c}{d} + x \right]}{\left( -a + \frac{b c}{d} \right)^2 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} + \frac{\text{Log} \left[ 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right]}{-a + \frac{b c}{d}} - \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right]}{b (a+b x)} \right) + \\
 & \frac{1}{g^2} 2 B d^3 i^3 n \left( A+B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( - \frac{2 a \left( \frac{a}{b} + x \right) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^3} + \frac{3 a^2 \text{Log} \left[ \frac{a}{b} + x \right]^2}{2 b^4} + \frac{a^3 \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{b^4 (a+b x)} + \right. \\
 & \left. \frac{2 a \left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{b^3} + \frac{-\frac{1}{2} b \left( -\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log} [a+b x]}{b^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{a+b x}{b} \right]}{b^2} + \right. \\
 & \left. \left( a^3 \left( (-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + d (a+b x) \left( \text{Log} [a+b x] - \text{Log} [c+d x] \right) \right) \right) / \right. \\
 & \left. \left( b^4 (b c - a d) (a+b x) - \frac{-\frac{1}{2} d \left( -\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log} [c+d x]}{d^3} \right) + \frac{1}{2} x^2 \text{Log} \left[ \frac{c+d x}{d} \right]}{b^2} + \right. \right. \\
 & \left. \left. \frac{1}{2 b^4} \left( -4 a b x + b^2 x^2 + \frac{2 a^3}{a+b x} + 6 a^2 \text{Log} [a+b x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \right. \right. \right. \\
 & \left. \left. \left. \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right) - \frac{3 a^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + \text{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right)}{b^4} \right) + \\
 & \frac{1}{g^2} 6 B c d^2 i^3 n \left( A+B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2} - \frac{a \text{Log}\left[\frac{a}{b} + x\right]^2}{b^3} - \frac{a^2 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3 (a + b x)} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^2} \right. \\
 & \left. \left( a^2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\text{Log}[a + b x] - \text{Log}[c + d x]\right) \right) \right) / \right. \\
 & \left. \left( b^3 (b c - a d) (a + b x) \right) + \frac{1}{b^3} \right. \\
 & \left. \left( b x - \frac{a^2}{a + b x} - 2 a \text{Log}[a + b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) + \right. \\
 & \left. \frac{2 a \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right)}{b^3} \right) + \\
 & \frac{1}{g^2} 6 B c^2 d i^3 n \left( A + B \left( \text{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \\
 & \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} + \frac{a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2 (a + b x)} + \right. \\
 & \left. \left( a \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left(\text{Log}[a + b x] - \text{Log}[c + d x]\right) \right) \right) / \right. \\
 & \left. \left( b^2 (b c - a d) (a + b x) \right) + \frac{1}{b^2} \right. \\
 & \left. \left( \frac{a}{a + b x} + \text{Log}[a + b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) - \right. \\
 & \left. \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]}{b^2} \right) + \\
 & \frac{1}{g^2} B^2 d^3 i^3 n^2 \left( \frac{a^2 \text{Log}\left[\frac{a}{b} + x\right]^3}{b^4} - \frac{2 a (a + b x) \left(2 - 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{b^4} + \right. \\
 & \frac{a^3 \left(2 + 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{b^4 (a + b x)} + \frac{1}{4 b^4} \\
 & (a + b x) \left(-7 a + b x + (6 a - 2 b x) \text{Log}\left[\frac{a}{b} + x\right] - 2 (a - b x) \text{Log}\left[\frac{a}{b} + x\right]^2\right) - \\
 & \frac{2 a (c + d x) \left(2 - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{b^3 d} + \frac{1}{4 b^2 d^2} \\
 & (c + d x) \left(-7 c + d x + (6 c - 2 d x) \text{Log}\left[\frac{c}{d} + x\right] - 2 (c - d x) \text{Log}\left[\frac{c}{d} + x\right]^2\right) + \\
 & \frac{1}{2 b^4} \left(-4 a b x + b^2 x^2 + \frac{2 a^3}{a + b x} + 6 a^2 \text{Log}[a + b x] \right) \\
 & \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2 - \left( a^3 \left( -b (c + d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + \right. \right. \\
 & \left. \left. 2 d (a + b x) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 d (a + b x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left( b^4 (b c - a d) (a + b x) + 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \right. \\
 & \left( -\frac{2 a \left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} + \frac{3 a^2 \text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} + \frac{a^3 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} + \right. \\
 & \left. \frac{2 a \left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} + \frac{-\frac{1}{2} b \left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a+b x]}{b^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{a+b x}{b}\right]}{b^2} + \right. \\
 & \left. \left( a^3 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right) \right) \right) / \right. \\
 & \left. \left( b^4 (b c - a d) (a + b x) \right) - \frac{-\frac{1}{2} d \left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c+d x]}{d^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c+d x}{d}\right]}{b^2} - \right. \\
 & \left. \frac{3 a^2 \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] \right)}{b^4} \right) - 2 \left( -\frac{1}{b^4 d} \right. \\
 & \left. 2 a \left( a d + 2 b d x - b d x \text{Log}\left[\frac{c}{d} + x\right] - b c \text{Log}[c + d x] + \text{Log}\left[\frac{a}{b} + x\right] \left( -d (a + b x) + d (a + b x) \right. \right. \right. \\
 & \left. \left. \left. \text{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + (b c - a d) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) + \right. \\
 & \frac{1}{4 b^4 d^2} \left( -2 a b c d - 3 b^2 c d x - 3 a b d^2 x + b^2 d^2 x^2 + 2 a b d^2 x \text{Log}\left[\frac{c}{d} + x\right] - \right. \\
 & \left. b^2 d^2 x^2 \text{Log}\left[\frac{c}{d} + x\right] + a^2 d^2 \text{Log}[a + b x] + b^2 c^2 \text{Log}[c + d x] + 2 a b c d \text{Log}[c + d x] + \right. \\
 & \left. \text{Log}\left[\frac{a}{b} + x\right] \left( b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \text{Log}\left[\frac{c}{d} + x\right] + (-2 b^2 c^2 + 2 a^2 d^2) \right. \right. \\
 & \left. \left. \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + (-2 b^2 c^2 + 2 a^2 d^2) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) - \\
 & \left( a^3 \left( d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \right. \right. \right. \\
 & \left. \left. \left. \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right) \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \right. \\
 & \left. \left. \left. d (a + b x) \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - 2 d (a + b x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) / \\
 & \left( 2 b^4 (b c - a d) (a + b x) + \frac{1}{2 b^4} 3 a^2 \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \left( \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) - \right. \right. \\
 & \left. \left. 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) + \\
 & \frac{1}{b^4} 3 a^2 \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - \right. \\
 & \left. \left. 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{g^2} 3 B^2 c d^2 i^3 n^2 \left( -\frac{2 a \operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^3} + \frac{(a+b x)\left(2-2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3} - \right. \\
 & \frac{a^2\left(2+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^3(a+b x)} + \frac{(c+d x)\left(2-2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{b^2 d} + \frac{1}{b^3} \\
 & \left. \left(b x - \frac{a^2}{a+b x} - 2 a \operatorname{Log}[a+b x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)^2 + \right. \\
 & \left. \left(a^2\left(-b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+ \right. \right. \right. \\
 & \left. \left. 2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right) / \left(b^3(b c-a d)(a+b x)\right) + \\
 & 2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)\left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^2} - \right. \\
 & \frac{a \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{b^3} - \frac{a^2\left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{b^3(a+b x)} - \frac{\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{b^2} - \\
 & \left. \left(a^2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right) / \right. \\
 & \left. \left(b^3(b c-a d)(a+b x)\right)+\frac{2 a\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)}{b^3} \right) - \\
 & 2\left(\frac{1}{b^3 d}\left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right]-b c \operatorname{Log}[c+d x]+\operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \\
 & \left. \left(-d(a+b x)+d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right]+(b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)+(b c-a d) \right. \\
 & \left. \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)+\left(a^2\left(d(a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2+2\left((-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+ \right. \right. \right. \\
 & \left. \left. d(a+b x)\left(\operatorname{Log}[a+b x]-\operatorname{Log}[c+d x]\right)\right)\right)-2 \operatorname{Log}\left[\frac{a}{b}+x\right]\left((b c-a d) \operatorname{Log}\left[\frac{c}{d}+x\right]+ \right. \\
 & \left. \left. d(a+b x) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)-2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right) / \right. \\
 & \left. \left(2 b^3(b c-a d)(a+b x)\right)-\frac{1}{b^3} a\left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2\left(\operatorname{Log}\left[\frac{c}{d}+x\right]-\operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)- \right. \right. \\
 & \left. \left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right)\right) - \\
 & \frac{1}{b^3} 2 a\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]- \right. \\
 & \left. \left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right)\right) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{g^2} 3 B^2 c^2 d i^3 n^2 \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^3}{3 b^2} + \frac{a \left(2 + 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{b^2 (a + b x)} + \frac{1}{b^2} \right. \\
 & \left. \left( \frac{a}{a + b x} + \text{Log}[a + b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2 - \right. \\
 & \left. \left( a \left( -b (c + d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a + b x) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right. \right. \right. \\
 & \left. \left. \left. 2 d (a + b x) \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) / (b^2 (b c - a d) (a + b x)) + \\
 & 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^2} + \frac{a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^2 (a + b x)} + \right. \\
 & \left. \left( a \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) \right) / \\
 & \left. \left( b^2 (b c - a d) (a + b x) \right) - \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^2} \right) - \\
 & 2 \left( - \left( \left( a \left( d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \right. \right. \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. (\text{Log}[a + b x] - \text{Log}[c + d x]) \right) \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left. d (a + b x) \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - 2 d (a + b x) \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) \right) \right) / \\
 & \left. \left( 2 b^2 (b c - a d) (a + b x) \right) \right) + \frac{1}{2 b^2} \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \left( \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) - \right. \\
 & \left. 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] + 2 \text{PolyLog}\left[3, \frac{d (a + b x)}{-b c + a d}\right] \right) \right) + \\
 & \frac{1}{b^2} \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - \right. \\
 & \left. 2 \text{PolyLog}\left[3, \frac{b (c + d x)}{b c - a d}\right] \right) \right)
 \end{aligned}$$

**Problem 184: Result more than twice size of optimal antiderivative.**

$$\int \frac{(c i + d i x)^3 \left( A + B \text{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \right)^2}{(a g + b g x)^3} dx$$

Optimal (type 4, 644 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{4 B^2 d (b c - a d) i^3 n^2 (c + d x)}{b^3 g^3 (a + b x)} - \frac{B^2 (b c - a d) i^3 n^2 (c + d x)^2}{4 b^2 g^3 (a + b x)^2} - \\
 & \frac{4 B d (b c - a d) i^3 n (c + d x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g^3 (a + b x)} - \\
 & \frac{B (b c - a d) i^3 n (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^2 g^3 (a + b x)^2} + \frac{d^3 i^3 (a + b x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^4 g^3} - \\
 & \frac{2 d (b c - a d) i^3 (c + d x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^3 g^3 (a + b x)} - \frac{(b c - a d) i^3 (c + d x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 b^2 g^3 (a + b x)^2} + \\
 & \frac{2 B d^2 (b c - a d) i^3 n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{-b c - a d}{b (c+d x)} \right]}{b^4 g^3} - \\
 & \frac{3 d^2 (b c - a d) i^3 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \operatorname{Log}\left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g^3} + \\
 & \frac{2 B^2 d^2 (b c - a d) i^3 n^2 \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{b^4 g^3} + \\
 & \frac{6 B d^2 (b c - a d) i^3 n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{PolyLog}\left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g^3} + \\
 & \frac{6 B^2 d^2 (b c - a d) i^3 n^2 \operatorname{PolyLog}\left[ 3, \frac{b (c+d x)}{d (a+b x)} \right]}{b^4 g^3}
 \end{aligned}$$

Result (type 4, 6613 leaves):

$$\begin{aligned}
 & \frac{d^3 i^3 x \left( A + B \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{b^3 g^3} + \frac{1}{b^4 g^3} \\
 & 3 d^2 (b c - a d) i^3 \operatorname{Log}[a + b x] \left( A + B \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 - \\
 & \frac{1}{b^4 g^3 (a + b x)} 3 \left( A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3 + \right. \\
 & \quad 2 A b^2 B c^2 d i^3 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - 4 a A b B c d^2 i^3 \\
 & \quad \left. \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) + 2 a^2 A B d^3 i^3 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right) + \\
 & \quad b^2 B^2 c^2 d i^3 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 - 2 a b B^2 c d^2 i^3 \\
 & \quad \left. \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 + a^2 B^2 d^3 i^3 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) + \\
 & \frac{1}{2 b^4 g^3 (a + b x)^2} \left( -A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3 - \right. \\
 & \quad \left. 2 A b^3 B c^3 i^3 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 6 a A b^2 B c^2 d i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) - \\
 & 6 a^2 A b B c d^2 i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + 2 a^3 A B d^3 i^3 \\
 & \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) - b^3 B^2 c^3 i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\
 & 3 a b^2 B^2 c^2 d i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - 3 a^2 b B^2 c d^2 i^3 \\
 & \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + a^3 B^2 d^3 i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 \Big) - \\
 & \left( B^2 c^3 i^3 n^2 \left( b^2 c^2 - 8 a b c d + 7 a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 d^2 (a+b x)^2 \text{Log}[a+b x] + \right. \right. \\
 & \quad \left. \left. 2 (b c - a d) (b c - 3 a d - 2 b d x) \text{Log} \left[ \frac{a+b x}{c+d x} \right] + 2 b (c+d x) (b c - 2 a d - b d x) \text{Log} \left[ \frac{a+b x}{c+d x} \right]^2 + \right. \right. \\
 & \quad \left. \left. 6 a^2 d^2 \text{Log}[c+d x] + 12 a b d^2 x \text{Log}[c+d x] + 6 b^2 d^2 x^2 \text{Log}[c+d x] \right) \right) / \\
 & \left( 4 b (b c - a d)^2 g^3 (a+b x)^2 \right) + \frac{1}{g^3} 2 B c^3 i^3 n \left( A+B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( - \frac{\left( \frac{a}{b} + x \right) \left( 2 \text{Log} \left[ \frac{a}{b} + x \right] + 4 \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{8 (a+b x)^3 \text{Log} \left[ \frac{a}{b} + x \right]} - \frac{1}{2 b} \right. \\
 & \left. \left( \frac{b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^3 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} - \left( \frac{b^2 \left( \frac{c}{d} + x \right)^2}{\left( -a + \frac{b c}{d} \right)^4 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)^2} + \frac{2 b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^3 \left( 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right)} \right) \text{Log} \left[ \frac{c}{d} + x \right] - \right. \\
 & \left. \frac{\text{Log} \left[ 1 - \frac{b \left( \frac{c}{d} + x \right)}{-a + \frac{b c}{d}} \right]}{\left( -a + \frac{b c}{d} \right)^2} \right) - \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{-a}{c+d x} + \frac{b x}{c+d x} \right]}{2 b (a+b x)^2} \right) + \\
 & \frac{1}{g^3} 6 B c^2 d i^3 n \left( A+B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( - \frac{1 + \text{Log} \left[ \frac{a}{b} + x \right]}{b^2 (a+b x)} + \frac{a \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] \right)}{4 b^2 (a+b x)^2} - \right. \\
 & \quad \frac{(-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + d (a+b x) \left( \text{Log}[a+b x] - \text{Log}[c+d x] \right)}{b^2 (b c - a d) (a+b x)} - \\
 & \quad \left. \frac{a \left( \text{Log} \left[ \frac{c}{d} + x \right] + \frac{d (a+b x) (b c - a d + d (a+b x) \text{Log}[a+b x] - d (a+b x) \text{Log}[c+d x])}{(b c - a d)^2} \right)}{2 b^2 (a+b x)^2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{(a+2bx) \left( -\log\left[\frac{a}{b}+x\right] + \log\left[\frac{c}{d}+x\right] + \log\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)}{2b^2(a+bx)^2} \right) + \\
 & \frac{1}{g^3} 2Bd^3i^3n \left( A+B \left( \log\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] - n \log\left[ \frac{a+bx}{c+dx} \right] \right) \right) \left( \frac{\left( \frac{a}{b}+x \right) \left( -1 + \log\left[ \frac{a}{b}+x \right] \right)}{b^3} - \right. \\
 & \frac{3a \log\left[ \frac{a}{b}+x \right]^2}{2b^4} - \frac{3a^2 \left( 1 + \log\left[ \frac{a}{b}+x \right] \right)}{b^4(a+bx)} + \frac{a^3 \left( 1 + 2 \log\left[ \frac{a}{b}+x \right] \right)}{4b^4(a+bx)^2} - \frac{\left( \frac{c}{d}+x \right) \left( -1 + \log\left[ \frac{c}{d}+x \right] \right)}{b^3} - \\
 & \left. \left( 3a^2 \left( (-bc+ad) \log\left[ \frac{c}{d}+x \right] + d(a+bx) \left( \log[a+bx] - \log[c+dx] \right) \right) \right) / \right. \\
 & \left. \left( b^4(bc-ad)(a+bx) \right) - \frac{a^3 \left( \log\left[ \frac{c}{d}+x \right] + \frac{d(a+bx)(bc-ad+d(a+bx)\log[a+bx]-d(a+bx)\log[c+dx])}{(bc-ad)^2} \right)}{2b^4(a+bx)^2} - \right. \\
 & \frac{1}{2b^4} \left( -2bx + \frac{a^2(5a+6bx)}{(a+bx)^2} + 6a \log[a+bx] \right) \left( -\log\left[ \frac{a}{b}+x \right] + \log\left[ \frac{c}{d}+x \right] + \right. \\
 & \left. \log\left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right) + \frac{3a \left( \log\left[ \frac{c}{d}+x \right] \log\left[ \frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog}\left[ 2, \frac{b(c+dx)}{bc-ad} \right] \right)}{b^4} \left. \right) + \\
 & \frac{1}{g^3} 6Bc d^2 i^3 n \left( A+B \left( \log\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] - n \log\left[ \frac{a+bx}{c+dx} \right] \right) \right) \\
 & \left( \frac{\log\left[ \frac{a}{b}+x \right]^2}{2b^3} + \frac{2a \left( 1 + \log\left[ \frac{a}{b}+x \right] \right)}{b^3(a+bx)} - \frac{a^2 \left( 1 + 2 \log\left[ \frac{a}{b}+x \right] \right)}{4b^3(a+bx)^2} + \right. \\
 & \left. \left( 2a \left( (-bc+ad) \log\left[ \frac{c}{d}+x \right] + d(a+bx) \left( \log[a+bx] - \log[c+dx] \right) \right) \right) / \right. \\
 & \left. \left( b^3(bc-ad)(a+bx) \right) + \frac{a^2 \left( \log\left[ \frac{c}{d}+x \right] + \frac{d(a+bx)(bc-ad+d(a+bx)\log[a+bx]-d(a+bx)\log[c+dx])}{(bc-ad)^2} \right)}{2b^3(a+bx)^2} + \right. \\
 & \frac{1}{2b^3} \left( \frac{a(3a+4bx)}{(a+bx)^2} + 2 \log[a+bx] \right) \left( -\log\left[ \frac{a}{b}+x \right] + \log\left[ \frac{c}{d}+x \right] + \log\left[ \frac{a}{c+dx} + \frac{bx}{c+dx} \right] \right) - \\
 & \left. \frac{\log\left[ \frac{c}{d}+x \right] \log\left[ \frac{d(a+bx)}{-bc+ad} \right] + \text{PolyLog}\left[ 2, \frac{b(c+dx)}{bc-ad} \right]}{b^3} \right) + \\
 & \frac{1}{g^3} 3B^2c^2d i^3 n^2 \left( -\frac{2+2 \log\left[ \frac{a}{b}+x \right] + \log\left[ \frac{a}{b}+x \right]^2}{b^2(a+bx)} + \frac{a \left( 1 + 2 \log\left[ \frac{a}{b}+x \right] + 2 \log\left[ \frac{a}{b}+x \right]^2 \right)}{4b^2(a+bx)^2} + \right. \\
 & 2 \left( -\frac{1 + \log\left[ \frac{a}{b}+x \right]}{b^2(a+bx)} + \frac{a \left( 1 + 2 \log\left[ \frac{a}{b}+x \right] \right)}{4b^2(a+bx)^2} - \left( (-bc+ad) \log\left[ \frac{c}{d}+x \right] + \right. \right. \\
 & \left. \left. d(a+bx) \left( \log[a+bx] - \log[c+dx] \right) \right) \right) / \left( b^2(bc-ad)(a+bx) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left. \frac{a \left( \text{Log} \left[ \frac{c}{d} + x \right] + \frac{d (a+b x) (b c - a d + d (a+b x) \text{Log} [a+b x] - d (a+b x) \text{Log} [c+d x])}{(b c - a d)^2} \right)}{2 b^2 (a+b x)^2} \right) \\
 & \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right) - \\
 & \frac{(a+2 b x) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right)^2}{2 b^2 (a+b x)^2} - \\
 & 2 \left( \left( d (a+b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 + 2 \left( (-b c + a d) \text{Log} \left[ \frac{c}{d} + x \right] + d (a+b x) (\text{Log} [a+b x] - \text{Log} [c + \right. \right. \right. \\
 & \left. \left. \left. d x) \right) \right) - 2 \text{Log} \left[ \frac{a}{b} + x \right] \left( (b c - a d) \text{Log} \left[ \frac{c}{d} + x \right] + d (a+b x) \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) \right) - \\
 & \left. 2 d (a+b x) \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) / (2 b^2 (b c - a d) (a+b x)) + \\
 & \left( a \left( -d (-b c + a d) (a+b x) + (b c - a d)^2 \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] \right) \text{Log} \left[ \frac{c}{d} + x \right] + d^2 (a+b x)^2 \right. \right. \\
 & \left. \left. \text{Log} [a+b x] - d^2 (a+b x)^2 \text{Log} [c+d x] + d (a+b x) \left( d (a+b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 + \right. \right. \right. \\
 & \left. \left. \left. 2 (b c - a d) \left( 1 + \text{Log} \left[ \frac{a}{b} + x \right] \right) - 2 d (a+b x) \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) + \right. \right. \right. \\
 & \left. \left. \left. \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) \right) / (4 b^2 (b c - a d)^2 (a+b x)^2) \right) + \\
 & \left( -b (c+d x) \text{Log} \left[ \frac{c}{d} + x \right]^2 + 2 d (a+b x) \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + \right. \\
 & \left. 2 d (a+b x) \text{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) / (b^2 (b c - a d) (a+b x)) + \\
 & \left( a \left( b (c+d x) (-2 a d + b (c-d x)) \text{Log} \left[ \frac{c}{d} + x \right]^2 - 2 d^2 (a+b x)^2 \text{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] + \right. \right. \\
 & \left. \left. 2 d (a+b x) \text{Log} \left[ \frac{c}{d} + x \right] \left( b (c+d x) + d (a+b x) \text{Log} \left[ \frac{d (a+b x)}{-b c + a d} \right] \right) \right) + \right. \\
 & \left. \left. 2 d^2 (a+b x)^2 \text{PolyLog} \left[ 2, \frac{b (c+d x)}{b c - a d} \right] \right) \right) / (2 b^2 (b c - a d)^2 (a+b x)^2) \right) + \\
 & \frac{1}{g^3} B^2 d^3 i^3 n^2 \left( -\frac{a \text{Log} \left[ \frac{a}{b} + x \right]^3}{b^4} + \frac{(a+b x) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^4} - \right. \\
 & \frac{3 a^2 \left( 2 + 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b^4 (a+b x)} + \frac{a^3 \left( 1 + 2 \text{Log} \left[ \frac{a}{b} + x \right] + 2 \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{4 b^4 (a+b x)^2} + \\
 & \left. \frac{(c+d x) \left( 2 - 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{b^3 d} - \frac{1}{2 b^4} \left( -2 b x + \frac{a^2 (5 a + 6 b x)}{(a+b x)^2} + 6 a \text{Log} [a+b x] \right) \right)
 \end{aligned}$$



$$\begin{aligned}
 & \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2 + \\
 & \left( 3 a^2 \left( -b(c+dx) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \right. \\
 & \quad \left. \left. 2d(a+bx) \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / (b^4(bc-ad)(a+bx)) + \\
 & \left( a^3 \left( b(c+dx)(-2ad+b(c-dx)) \text{Log}\left[\frac{c}{d} + x\right]^2 - 2d^2(a+bx)^2 \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \right. \right. \\
 & \quad \left. \left. 2d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] \left( b(c+dx) + d(a+bx) \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) + \right. \right. \\
 & \quad \left. \left. 2d^2(a+bx)^2 \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / \\
 & \left( 2b^4(bc-ad)^2(a+bx)^2 \right) + 2 \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) \\
 & \left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^3} - \frac{3a \text{Log}\left[\frac{a}{b} + x\right]^2}{2b^4} - \frac{3a^2 \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^4(a+bx)} + \right. \\
 & \quad \left. \frac{a^3 \left(1 + 2 \text{Log}\left[\frac{a}{b} + x\right]\right)}{4b^4(a+bx)^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{b^3} - \right. \\
 & \quad \left. \left( 3 a^2 \left( (-bc+ad) \text{Log}\left[\frac{c}{d} + x\right] + d(a+bx) \left( \text{Log}[a+bx] - \text{Log}[c+dx] \right) \right) \right) / (b^4(bc-ad)) \right. \\
 & \quad \left. (a+bx) - \frac{a^3 \left( \text{Log}\left[\frac{c}{d} + x\right] + \frac{d(a+bx)(bc-ad+d(a+bx) \text{Log}[a+bx]-d(a+bx) \text{Log}[c+dx])}{(bc-ad)^2} \right)}{2b^4(a+bx)^2} + \right. \\
 & \quad \left. \frac{3a \left( \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right)}{b^4} \right) - \\
 & 2 \left( \frac{1}{b^4 d} \left( ad + 2bdx - bdx \text{Log}\left[\frac{c}{d} + x\right] - bc \text{Log}[c+dx] + \text{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
 & \quad \left. \left( -d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d} + x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + (bc-ad) \right. \\
 & \quad \left. \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) + \left( 3 a^2 \left( d(a+bx) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-bc+ad) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \right. \\
 & \quad \left. \left. d(a+bx) \left( \text{Log}[a+bx] - \text{Log}[c+dx] \right) \right) - 2 \text{Log}\left[\frac{a}{b} + x\right] \left( (bc-ad) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \quad \left. \left. d(a+bx) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - 2d(a+bx) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / \\
 & \left( 2b^4(bc-ad)(a+bx) \right) + \left( a^3 \left( -d(-bc+ad)(a+bx) + (bc-ad)^2 \right. \right. \\
 & \quad \left. \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right) \text{Log}\left[\frac{c}{d} + x\right] + d^2(a+bx)^2 \text{Log}[a+bx] - d^2(a+bx)^2 \text{Log}[c+dx] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & d (a+b x) \left( d (a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 2 (b c-a d) \left( 1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) - \right. \\
 & \quad \left. 2 d (a+b x) \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \Big/ \\
 & \left( 4 b^4 (b c-a d)^2 (a+b x)^2 \right) - \frac{1}{2 b^4} 3 a \left( \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - \right. \\
 & \quad \left. 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) - \\
 & \frac{1}{b^4} 3 a \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - \right. \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \Big) + \\
 & \frac{1}{g^3} 3 B^2 c d^2 i^3 n^2 \left( \frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^3}{3 b^3} + \frac{2 a \left( 2 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \right)}{b^3 (a+b x)} - \right. \\
 & \quad \left. \frac{a^2 \left( 1 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \right)}{4 b^3 (a+b x)^2} + \frac{1}{2 b^3} \right. \\
 & \quad \left. \left( \frac{a(3 a+4 b x)}{(a+b x)^2} + 2 \operatorname{Log}[a+b x] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right)^2 - \right. \\
 & \quad \left. \left( 2 a \left( -b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \right. \right. \\
 & \quad \left. \left. 2 d(a+b x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \Big/ (b^3 (b c-a d) (a+b x)) - \\
 & \left( a^2 \left( b(c+d x) (-2 a d+b(c-d x)) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 d^2 (a+b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \left( b(c+d x) + d(a+b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) + \right. \right. \\
 & \quad \left. \left. 2 d^2 (a+b x)^2 \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \Big/ \\
 & \left( 2 b^3 (b c-a d)^2 (a+b x)^2 \right) + 2 \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) \\
 & \left( \frac{\operatorname{Log}\left[\frac{a}{b}+x\right]^2}{2 b^3} + \frac{2 a \left( 1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right)}{b^3 (a+b x)} - \frac{a^2 \left( 1 + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \right)}{4 b^3 (a+b x)^2} + \right. \\
 & \quad \left. \left( 2 a \left( (-b c+a d) \operatorname{Log}\left[\frac{c}{d}+x\right] + d(a+b x) \left( \operatorname{Log}[a+b x] - \operatorname{Log}[c+d x] \right) \right) \right) \right) \Big/ (b^3 (b c-a d) \\
 & \quad (a+b x)) + \frac{a^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{d(a+b x)(b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x])}{(b c-a d)^2} \right)}{2 b^3 (a+b x)^2} -
 \end{aligned}$$



$$\begin{aligned} & - \frac{2 B^2 d^2 i^3 n^2 (c+d x)}{b^3 g^4 (a+b x)} - \frac{B^2 d i^3 n^2 (c+d x)^2}{4 b^2 g^4 (a+b x)^2} - \\ & \frac{2 B^2 i^3 n^2 (c+d x)^3}{27 b g^4 (a+b x)^3} - \frac{2 B d^2 i^3 n (c+d x) \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{b^3 g^4 (a+b x)} - \\ & \frac{B d i^3 n (c+d x)^2 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 b^2 g^4 (a+b x)^2} - \frac{2 B i^3 n (c+d x)^3 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{9 b g^4 (a+b x)^3} - \\ & \frac{d^2 i^3 (c+d x) \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{b^3 g^4 (a+b x)} - \frac{d i^3 (c+d x)^2 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 b^2 g^4 (a+b x)^2} - \\ & \frac{i^3 (c+d x)^3 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{3 b g^4 (a+b x)^3} - \frac{d^3 i^3 \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \log\left[ 1 - \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^4} + \\ & \frac{2 B d^3 i^3 n \left( A+B \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog}\left[ 2, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^4} + \frac{2 B^2 d^3 i^3 n^2 \text{PolyLog}\left[ 3, \frac{b(c+d x)}{d(a+b x)} \right]}{b^4 g^4} \end{aligned}$$

Result (type 4, 8160 leaves):

$$\begin{aligned} & \frac{d^3 i^3 \log[a+b x] \left( A+B \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2}{b^4 g^4} + \frac{1}{b^4 g^4 (a+b x)} \\ & 3 \left( -A^2 b c d^2 i^3 + a A^2 d^3 i^3 - 2 A b B c d^2 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + 2 a A B d^3 i^3 \right. \\ & \quad \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) - b B^2 c d^2 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\ & \quad \left. a B^2 d^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) - \frac{1}{2 b^4 g^4 (a+b x)^2} \\ & 3 \left( A^2 b^2 c^2 d i^3 - 2 a A^2 b c d^2 i^3 + a^2 A^2 d^3 i^3 + 2 A b^2 B c^2 d i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) - \right. \\ & \quad 4 a A b B c d^2 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + \\ & \quad 2 a^2 A B d^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + \\ & \quad \left. b^2 B^2 c^2 d i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right)^2 - 2 a b B^2 c d^2 i^3 \right. \\ & \quad \left. \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right)^2 + a^2 B^2 d^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) + \\ & \frac{1}{3 b^4 g^4 (a+b x)^3} \left( -A^2 b^3 c^3 i^3 + 3 a A^2 b^2 c^2 d i^3 - 3 a^2 A^2 b c d^2 i^3 + a^3 A^2 d^3 i^3 - \right. \\ & \quad 2 A b^3 B c^3 i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) + \\ & \quad \left. 6 a A b^2 B c^2 d i^3 \left( \log\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - n \log\left[ \frac{a+b x}{c+d x} \right] \right) - \right. \end{aligned}$$

$$\begin{aligned}
 & 6 a^2 A b B c d^2 i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + 2 a^3 A B d^3 i^3 \\
 & \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) - b^3 B^2 c^3 i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\
 & 3 a b^2 B^2 c^2 d i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - 3 a^2 b B^2 c d^2 i^3 \\
 & \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + a^3 B^2 d^3 i^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\
 & \frac{1}{54 b (b c - a d)^3 g^4 (a+b x)^3} B^2 c^3 i^3 n^2 \left( -4 (b c - a d)^3 + 15 d (b c - a d)^2 (a+b x) + \right. \\
 & 66 d^2 (-b c + a d) (a+b x)^2 - 66 d^3 (a+b x)^3 \text{Log}[a+b x] - \\
 & 6 (b c - a d) \left( 2 (b c - a d)^2 + 3 d (-b c + a d) (a+b x) + 6 d^2 (a+b x)^2 \right) \text{Log} \left[ \frac{a+b x}{c+d x} \right] - \\
 & 18 b \left( 3 a^2 d^2 (c+d x) + 3 a b d (-c^2 + d^2 x^2) + b^2 (c^3 + d^3 x^3) \right) \text{Log} \left[ \frac{a+b x}{c+d x} \right]^2 + \\
 & \left. 66 d^3 (a+b x)^3 \text{Log}[c+d x] \right) + \\
 & \frac{1}{g^4} 2 B c^3 i^3 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( - \frac{\left( \frac{a}{b} + x \right) \left( 3 \text{Log} \left[ \frac{a}{b} + x \right] + 9 \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{27 (a+b x)^4 \text{Log} \left[ \frac{a}{b} + x \right]} - \frac{1}{6 b} \right. \\
 & \left( - \frac{b^2 \left( \frac{c}{d} + x \right)^2}{\left( -a + \frac{b c}{d} \right)^5 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right)^2} - \frac{4 b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^4 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right)} + \right. \\
 & \left. \left( \frac{2 b^3 \left( \frac{c}{d} + x \right)^3}{\left( -a + \frac{b c}{d} \right)^6 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right)^3} + \frac{6 b^2 \left( \frac{c}{d} + x \right)^2}{\left( -a + \frac{b c}{d} \right)^5 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right)^2} + \frac{6 b \left( \frac{c}{d} + x \right)}{\left( -a + \frac{b c}{d} \right)^4 \left( 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right)} \right) \text{Log} \left[ \frac{c}{d} + x \right] + \\
 & \left. \frac{2 \text{Log} \left[ 1 - \frac{b \left( \frac{c+x}{d} \right)}{-a + \frac{b c}{d}} \right]}{\left( -a + \frac{b c}{d} \right)^3} \right) - \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right]}{3 b (a+b x)^3} \right) + \\
 & \frac{1}{g^4} 6 B c^2 d i^3 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right)
 \end{aligned}$$

$$\left( \begin{aligned} & - \frac{1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]}{4 b^2 (a + b x)^2} + \frac{a \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^2 (a + b x)^3} + \\ & \frac{a \left( - \frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{d \left( \frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \operatorname{Log}[a + b x] - 2 d^2 \operatorname{Log}[c + d x] \right)}{(b c - a d)^3} \right)}{6 b^2} + \\ & \frac{\operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2}}{2 b^2 (a + b x)^2} - \\ & \frac{(a + 3 b x) \left( - \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)}{6 b^2 (a + b x)^3} \end{aligned} \right) +$$

$$\frac{1}{g^4} 6 B c d^2 i^3 n \left( A + B \left( \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] \right) \right)$$

$$\left( \begin{aligned} & - \frac{1 + \operatorname{Log}\left[\frac{a}{b} + x\right]}{b^3 (a + b x)} + \frac{a \left(1 + 2 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{2 b^3 (a + b x)^2} - \frac{a^2 \left(1 + 3 \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^3 (a + b x)^3} - \\ & \frac{(-b c + a d) \operatorname{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left( \operatorname{Log}[a + b x] - \operatorname{Log}[c + d x] \right)}{b^3 (b c - a d) (a + b x)} - \\ & \frac{a^2 \left( - \frac{2 \operatorname{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{d \left( \frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \operatorname{Log}[a + b x] - 2 d^2 \operatorname{Log}[c + d x] \right)}{(b c - a d)^3} \right)}{6 b^3} - \\ & \frac{a \left( \operatorname{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \operatorname{Log}[a + b x] - d (a + b x) \operatorname{Log}[c + d x])}{(b c - a d)^2} \right)}{b^3 (a + b x)^2} - \frac{1}{3 b^3 (a + b x)^3} \\ & \frac{(a^2 + 3 a b x + 3 b^2 x^2) \left( - \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)}{3 b^3 (a + b x)^3} \end{aligned} \right) +$$

$$\frac{1}{g^4} 2 B d^3 i^3 n \left( A + B \left( \operatorname{Log}\left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a + b x}{c + d x} \right] \right) \right)$$

$$\begin{aligned}
 & \left( \frac{\text{Log}\left[\frac{a}{b} + x\right]^2}{2 b^4} + \frac{3 a \left(1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{b^4 (a + b x)} - \frac{3 a^2 \left(1 + 2 \text{Log}\left[\frac{a}{b} + x\right]\right)}{4 b^4 (a + b x)^2} + \frac{a^3 \left(1 + 3 \text{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^4 (a + b x)^3} + \right. \\
 & \left. \left( 3 a \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right) \right) \right) / \right. \\
 & \left. a^3 \left( -\frac{2 \text{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{d \left( \frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \text{Log}[a + b x] - 2 d^2 \text{Log}[c + d x] \right)}{(b c - a d)^3} \right) \right. \\
 & \left. (b^4 (b c - a d) (a + b x)) + \frac{3 a^2 \left( \text{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \text{Log}[a + b x] - d (a + b x) \text{Log}[c + d x])}{(b c - a d)^2} \right)}{2 b^4 (a + b x)^2} + \frac{1}{6 b^4} \right. \\
 & \left. \left( \frac{a \left( 11 a^2 + 27 a b x + 18 b^2 x^2 \right)}{(a + b x)^3} + 6 \text{Log}[a + b x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \left. \left. \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) - \frac{\text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right]}{b^4} \right) + \\
 & \frac{1}{g^4} 3 B^2 c d^2 i^3 n^2 \left( -\frac{2 + 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2}{b^3 (a + b x)} + \frac{a \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] + 2 \text{Log}\left[\frac{a}{b} + x\right]^2 \right)}{2 b^3 (a + b x)^2} - \right. \\
 & \left. \frac{a^2 \left( 2 + 6 \text{Log}\left[\frac{a}{b} + x\right] + 9 \text{Log}\left[\frac{a}{b} + x\right]^2 \right)}{27 b^3 (a + b x)^3} + \right. \\
 & \left. 2 \left( -\frac{1 + \text{Log}\left[\frac{a}{b} + x\right]}{b^3 (a + b x)} + \frac{a \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right]\right)}{2 b^3 (a + b x)^2} - \frac{a^2 \left( 1 + 3 \text{Log}\left[\frac{a}{b} + x\right]\right)}{9 b^3 (a + b x)^3} - \right. \right. \\
 & \left. \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a + b x) \left( \text{Log}[a + b x] - \text{Log}[c + d x] \right) \right) / \right. \\
 & \left. (b^3 (b c - a d) (a + b x)) - \frac{1}{6 b^3} a^2 \left( -\frac{2 \text{Log}\left[\frac{c}{d} + x\right]}{(a + b x)^3} + \frac{1}{(b c - a d)^3} \right. \right. \\
 & \left. \left. d \left( \frac{(b c - a d) (-b c + 3 a d + 2 b d x)}{(a + b x)^2} + 2 d^2 \text{Log}[a + b x] - 2 d^2 \text{Log}[c + d x] \right) \right) \right) - \\
 & \left. \frac{a \left( \text{Log}\left[\frac{c}{d} + x\right] + \frac{d (a + b x) (b c - a d + d (a + b x) \text{Log}[a + b x] - d (a + b x) \text{Log}[c + d x])}{(b c - a d)^2} \right)}{b^3 (a + b x)^2} \right) \\
 & \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) - \frac{1}{3 b^3 (a + b x)^3}
 \end{aligned}$$

$$\begin{aligned}
 & (a^2 + 3 a b x + 3 b^2 x^2) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right)^2 - \\
 & 2 \left( \left( d (a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \left( (-b c + a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a+b x) (\text{Log}[a+b x] - \text{Log}[c+d x]) \right) \right) \right. \\
 & \quad \left. - 2 \text{Log}\left[\frac{a}{b} + x\right] \left( (b c - a d) \text{Log}\left[\frac{c}{d} + x\right] + d (a+b x) \text{Log}\left[\frac{b (c+d x)}{b c - a d}\right] \right) \right) - \\
 & \quad 2 d (a+b x) \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \Big/ (2 b^3 (b c - a d) (a+b x)) + \\
 & \left( a \left( -d (-b c + a d) (a+b x) + (b c - a d)^2 \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \quad d^2 (a+b x)^2 \text{Log}[a+b x] - d^2 (a+b x)^2 \text{Log}[c+d x] + \\
 & \quad d (a+b x) \left( d (a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 (b c - a d) \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - \right. \\
 & \quad \left. \left. 2 d (a+b x) \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \right) \right) \right) \Big/ \\
 & \quad \left( 2 b^3 (b c - a d)^2 (a+b x)^2 \right) + \frac{1}{36 b^3 (b c - a d)^3 (a+b x)^3} a^2 \left( -2 d (b c - a d)^2 (a+b x) + \right. \\
 & \quad 4 d^2 (b c - a d) (a+b x)^2 - 4 (b c - a d)^3 \left( 1 + 3 \text{Log}\left[\frac{a}{b} + x\right] \right) \text{Log}\left[\frac{c}{d} + x\right] + 4 d^3 (a+b x)^3 \\
 & \quad \text{Log}[a+b x] - 4 d^3 (a+b x)^3 \text{Log}[c+d x] + 3 d (a+b x) \left( 2 d^2 (a+b x)^2 \text{Log}\left[\frac{a}{b} + x\right]^2 + 4 \right. \\
 & \quad \left. d (b c - a d) (a+b x) \left( 1 + \text{Log}\left[\frac{a}{b} + x\right] \right) - (b c - a d)^2 \left( 1 + 2 \text{Log}\left[\frac{a}{b} + x\right] \right) - 4 \right. \\
 & \quad \left. \left. d^2 (a+b x)^2 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \right) \right) \right) \Big/ + \\
 & \left( -b (c+d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2 d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] + \right. \\
 & \quad \left. 2 d (a+b x) \text{PolyLog}\left[2, \frac{b (c+d x)}{b c - a d}\right] \right) \Big/ (b^3 (b c - a d) (a+b x)) + \\
 & \left( a \left( b (c+d x) (-2 a d + b (c-d x)) \text{Log}\left[\frac{c}{d} + x\right]^2 - 2 d^2 (a+b x)^2 \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] + \right. \right. \\
 & \quad 2 d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] \left( b (c+d x) + d (a+b x) \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] \right) + \\
 & \quad \left. \left. 2 d^2 (a+b x)^2 \text{PolyLog}\left[2, \frac{b (c+d x)}{b c - a d}\right] \right) \right) \Big/ (b^3 (b c - a d)^2 (a+b x)^2) + \\
 & \left( a^2 \left( -b (3 a^2 d^2 (c+d x) + 3 a b d (-c^2 + d^2 x^2) + b^2 (c^3 + d^3 x^3)) \text{Log}\left[\frac{c}{d} + x\right]^2 - \right. \right. \\
 & \quad d^2 (a+b x)^2 \left( b (c+d x) + 3 d (a+b x) \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] \right) + d (a+b x) \text{Log}\left[\frac{c}{d} + x\right] \\
 & \quad \left. \left( -b (c+d x) (-4 a d + b (c-3 d x)) + 2 d^2 (a+b x)^2 \text{Log}\left[\frac{d (a+b x)}{-b c + a d}\right] \right) \right) +
 \end{aligned}$$



$$\begin{aligned}
 & \left. 2 d^3 (a+b x)^3 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(3 b^3 (b c-a d)^3 (a+b x)^3\right) + \\
 & \frac{1}{g^4} 3 B^2 c^2 d i^3 n^2 \left( -\frac{1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]+2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2}{4 b^2 (a+b x)^2} + \frac{a\left(2+6 \operatorname{Log}\left[\frac{a}{b}+x\right]+9 \operatorname{Log}\left[\frac{a}{b}+x\right]^2\right)}{27 b^2 (a+b x)^3} + \right. \\
 & 2 \left( -\frac{1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]}{4 b^2 (a+b x)^2} + \frac{a\left(1+3 \operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{9 b^2 (a+b x)^3} + \frac{1}{6 b^2} a \left( -\frac{2 \operatorname{Log}\left[\frac{c}{d}+x\right]}{(a+b x)^3} + \frac{1}{(b c-a d)^3} \right. \right. \\
 & \left. \left. d \left( \frac{(b c-a d)(-b c+3 a d+2 b d x)}{(a+b x)^2} + 2 d^2 \operatorname{Log}[a+b x]-2 d^2 \operatorname{Log}[c+d x] \right) \right) + \right. \\
 & \left. \frac{\operatorname{Log}\left[\frac{c}{d}+x\right] + \frac{d(a+b x)(b c-a d+d(a+b x) \operatorname{Log}[a+b x]-d(a+b x) \operatorname{Log}[c+d x])}{(b c-a d)^2}}{2 b^2 (a+b x)^2} \right) \\
 & \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) - \\
 & \frac{(a+3 b x)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]\right)^2}{6 b^2 (a+b x)^3} - \\
 & 2 \left( \left( \left( -d(-b c+a d)(a+b x) + (b c-a d)^2 \left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right) \operatorname{Log}\left[\frac{c}{d}+x\right] + d^2(a+b x)^2 \right. \right. \right. \\
 & \left. \left. \operatorname{Log}[a+b x] - d^2(a+b x)^2 \operatorname{Log}[c+d x] + d(a+b x) \left( d(a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \right. \right. \right. \\
 & \left. \left. \left. 2(b c-a d) \left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right) - 2 d(a+b x) \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) / \left(4 b^2 (b c-a d)^2 (a+b x)^2\right) \right) - \\
 & \frac{1}{36 b^2 (b c-a d)^3 (a+b x)^3} a \left( -2 d(b c-a d)^2 (a+b x) + 4 d^2 (b c-a d)(a+b x)^2 - \right. \\
 & 4(b c-a d)^3 \left(1+3 \operatorname{Log}\left[\frac{a}{b}+x\right]\right) \operatorname{Log}\left[\frac{c}{d}+x\right] + 4 d^3 (a+b x)^3 \operatorname{Log}[a+b x] - \\
 & 4 d^3 (a+b x)^3 \operatorname{Log}[c+d x] + 3 d(a+b x) \left( 2 d^2 (a+b x)^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + 4 d \right. \\
 & (b c-a d)(a+b x) \left(1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right) - (b c-a d)^2 \left(1+2 \operatorname{Log}\left[\frac{a}{b}+x\right]\right) - 4 d^2 \\
 & \left. (a+b x)^2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) \right) - \\
 & \left( b(c+d x)(-2 a d+b(c-d x)) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 d^2(a+b x)^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \\
 & \left. 2 d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] \left( b(c+d x) + d(a+b x) \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) \right) +
 \end{aligned}$$

$$\begin{aligned}
 & 2 d^2 (a+b x)^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] / \left(2 b^2(b c-a d)^2(a+b x)^2\right) - \\
 & \left(a\left(-b\left(3 a^2 d^2(c+d x)+3 a b d\left(-c^2+d^2 x^2\right)+b^2\left(c^3+d^3 x^3\right)\right) \text{Log}\left[\frac{c}{d}+x\right]^2 - \right. \right. \\
 & \quad \left. d^2(a+b x)^2\left(b(c+d x)+3 d(a+b x) \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+d(a+b x) \text{Log}\left[\frac{c}{d}+x\right] \right. \\
 & \quad \left.\left(-b(c+d x)\left(-4 a d+b(c-3 d x)\right)+2 d^2(a+b x)^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)\right]+ \\
 & \quad \left. 2 d^3(a+b x)^3 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(3 b^2(b c-a d)^3(a+b x)^3\right)+ \\
 & \frac{1}{g^4} B^2 d^3 i^3 n^2\left(\frac{\text{Log}\left[\frac{a}{b}+x\right]^3}{3 b^4}+\frac{3 a\left(2+2 \text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{a}{b}+x\right]^2\right)}{b^4(a+b x)}-\right. \\
 & \quad \left.\frac{3 a^2\left(1+2 \text{Log}\left[\frac{a}{b}+x\right]+2 \text{Log}\left[\frac{a}{b}+x\right]^2\right)}{4 b^4(a+b x)^2}+\right. \\
 & \quad \left.\frac{a^3\left(2+6 \text{Log}\left[\frac{a}{b}+x\right]+9 \text{Log}\left[\frac{a}{b}+x\right]^2\right)}{27 b^4(a+b x)^3}+\frac{1}{6 b^4}\right. \\
 & \quad \left.\left(\frac{a\left(11 a^2+27 a b x+18 b^2 x^2\right)}{(a+b x)^3}+6 \text{Log}[a+b x]\right)\right. \\
 & \quad \left.\left(-\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]+\text{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)^2-\right. \\
 & \quad \left.3 a\left(-b(c+d x) \text{Log}\left[\frac{c}{d}+x\right]^2+2 d(a+b x) \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+\right. \\
 & \quad \left.2 d(a+b x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(b^4(b c-a d)(a+b x)\right)- \\
 & \left(3 a^2\left(b(c+d x)\left(-2 a d+b(c-d x)\right) \text{Log}\left[\frac{c}{d}+x\right]^2-2 d^2(a+b x)^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+\right. \\
 & \quad \left.2 d(a+b x) \text{Log}\left[\frac{c}{d}+x\right]\left(b(c+d x)+d(a+b x) \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+\right. \\
 & \quad \left.2 d^2(a+b x)^2 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(2 b^4(b c-a d)^2(a+b x)^2\right)- \\
 & \left(a^3\left(-b\left(3 a^2 d^2(c+d x)+3 a b d\left(-c^2+d^2 x^2\right)+b^2\left(c^3+d^3 x^3\right)\right) \text{Log}\left[\frac{c}{d}+x\right]^2 - \right. \right. \\
 & \quad \left. d^2(a+b x)^2\left(b(c+d x)+3 d(a+b x) \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)+d(a+b x) \text{Log}\left[\frac{c}{d}+x\right] \right. \\
 & \quad \left.\left(-b(c+d x)\left(-4 a d+b(c-3 d x)\right)+2 d^2(a+b x)^2 \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)\right)+
 \end{aligned}$$

$$\begin{aligned}
 & \left. 2 d^3 (a+b x)^3 \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(3 b^4 (b c-a d)^3 (a+b x)^3\right) + \\
 & 2 \left(-\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]+\text{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right) \\
 & \left(\frac{\text{Log}\left[\frac{a}{b}+x\right]^2}{2 b^4}+\frac{3 a\left(1+\text{Log}\left[\frac{a}{b}+x\right]\right)}{b^4(a+b x)}-\frac{3 a^2\left(1+2 \text{Log}\left[\frac{a}{b}+x\right]\right)}{4 b^4(a+b x)^2}+\frac{a^3\left(1+3 \text{Log}\left[\frac{a}{b}+x\right]\right)}{9 b^4(a+b x)^3}+\right. \\
 & \left.\left(3 a\left((-b c+a d) \text{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\left(\text{Log}[a+b x]-\text{Log}[c+d x]\right)\right)\right) / \right. \\
 & \left.\left(b^4(b c-a d)(a+b x)\right)+\frac{1}{6 b^4} a^3\left(-\frac{2 \text{Log}\left[\frac{c}{d}+x\right]}{(a+b x)^3}+\frac{1}{(b c-a d)^3}\right.\right. \\
 & \left.\left.d\left(\frac{(b c-a d)(-b c+3 a d+2 b d x)}{(a+b x)^2}+2 d^2 \text{Log}[a+b x]-2 d^2 \text{Log}[c+d x]\right)\right) + \right. \\
 & \left.\frac{1}{2 b^4(a+b x)^2} 3 a^2\left(\text{Log}\left[\frac{c}{d}+x\right]+\frac{1}{(b c-a d)^2} d(a+b x)(b c-a d+d(a+b x) \text{Log}[a+b x]-\right.\right. \right. \\
 & \left.\left.\left.d(a+b x) \text{Log}[c+d x]\right)\right)-\frac{\text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]}{b^4}\right) - \\
 & 2 \left(-\left(\left(3 a\left(d(a+b x) \text{Log}\left[\frac{a}{b}+x\right]^2+2\left((-b c+a d) \text{Log}\left[\frac{c}{d}+x\right]+d(a+b x)\right.\right.\right.\right.\right. \right. \\
 & \left.\left.\left.\left.\left(\text{Log}[a+b x]-\text{Log}[c+d x]\right)\right)\right)-2 \text{Log}\left[\frac{a}{b}+x\right]\left((b c-a d) \text{Log}\left[\frac{c}{d}+x\right]+d(a+b x) \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)\right.\right.\right. \\
 & \left.\left.\left.\left.\left.-2 d(a+b x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right)\right) / \right. \\
 & \left.\left(2 b^4(b c-a d)(a+b x)\right)\right)-\left(3 a^2\left(-d(-b c+a d)(a+b x)+(b c-a d)^2\right.\right. \\
 & \left.\left.\left(1+2 \text{Log}\left[\frac{a}{b}+x\right]\right) \text{Log}\left[\frac{c}{d}+x\right]+d^2(a+b x)^2 \text{Log}[a+b x]-d^2(a+b x)^2 \text{Log}[c+d x]+\right.\right. \\
 & \left.\left.d(a+b x)\left(d(a+b x) \text{Log}\left[\frac{a}{b}+x\right]^2+2(b c-a d)\left(1+\text{Log}\left[\frac{a}{b}+x\right]\right)-\right.\right. \\
 & \left.\left.\left.2 d(a+b x)\left(\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right)\right)\right) / \right. \\
 & \left.\left(4 b^4(b c-a d)^2(a+b x)^2\right)-\frac{1}{36 b^4(b c-a d)^3(a+b x)^3} a^3\left(-2 d(b c-a d)^2(a+b x)+\right.\right. \\
 & \left.\left.4 d^2(b c-a d)(a+b x)^2-4(b c-a d)^3\left(1+3 \text{Log}\left[\frac{a}{b}+x\right]\right) \text{Log}\left[\frac{c}{d}+x\right]+4 d^3(a+b x)^3\right.\right. \\
 & \left.\left.\text{Log}[a+b x]-4 d^3(a+b x)^3 \text{Log}[c+d x]+3 d(a+b x)\left(2 d^2(a+b x)^2 \text{Log}\left[\frac{a}{b}+x\right]^2+4\right.\right.\right. \\
 & \left.\left.\left.d(b c-a d)(a+b x)\left(1+\text{Log}\left[\frac{a}{b}+x\right]\right)-(b c-a d)^2\left(1+2 \text{Log}\left[\frac{a}{b}+x\right]\right)-4 d^2\right.\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & (a + b x)^2 \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right) + \frac{1}{2 b^4} \\
 & \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \left( \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] \right) - 2 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] + \right. \\
 & \quad \left. 2 \text{PolyLog} \left[ 3, \frac{d (a + b x)}{-b c + a d} \right] \right) + \frac{1}{b^4} \\
 & \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + 2 \text{Log} \left[ \frac{c}{d} + x \right] \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] - \right. \\
 & \quad \left. 2 \text{PolyLog} \left[ 3, \frac{b (c + d x)}{b c - a d} \right] \right)
 \end{aligned}$$

**Problem 186: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 768 leaves, 25 steps):

$$\begin{aligned}
 & \frac{b B^2 (b c - a d)^2 g^3 n^2 x}{3 d^3 i} + \frac{7 B (b c - a d)^2 g^3 n (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 d^3 i} - \\
 & \frac{b^2 B (b c - a d) g^3 n (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{3 d^4 i} + \\
 & \frac{3 (b c - a d)^2 g^3 (a + b x) \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{d^3 i} - \\
 & \frac{3 b^2 (b c - a d) g^3 (c + d x)^2 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 d^4 i} + \frac{b^3 g^3 (c + d x)^3 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{3 d^4 i} + \\
 & \frac{6 B (b c - a d)^3 g^3 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ \frac{b c - a d}{b (c + d x)} \right]}{d^4 i} + \\
 & \frac{(b c - a d)^3 g^3 \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \log \left[ \frac{b c - a d}{b (c + d x)} \right]}{d^4 i} + \frac{B^2 (b c - a d)^3 g^3 n^2 \log \left[ \frac{a+b x}{c+d x} \right]}{3 d^4 i} - \\
 & \frac{2 B^2 (b c - a d)^3 g^3 n^2 \log [c + d x]}{d^4 i} - \frac{7 B (b c - a d)^3 g^3 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \log \left[ 1 - \frac{b (c + d x)}{d (a + b x)} \right]}{3 d^4 i} + \\
 & \frac{6 B^2 (b c - a d)^3 g^3 n^2 \text{PolyLog} \left[ 2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^4 i} + \\
 & \frac{2 B (b c - a d)^3 g^3 n \left( A + B \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog} \left[ 2, \frac{d (a + b x)}{b (c + d x)} \right]}{d^4 i} + \\
 & \frac{7 B^2 (b c - a d)^3 g^3 n^2 \text{PolyLog} \left[ 2, \frac{b (c + d x)}{d (a + b x)} \right]}{3 d^4 i} - \frac{2 B^2 (b c - a d)^3 g^3 n^2 \text{PolyLog} \left[ 3, \frac{d (a + b x)}{b (c + d x)} \right]}{d^4 i}
 \end{aligned}$$

Result (type 4, 4914 leaves):

$$\begin{aligned}
 & \frac{1}{12 d^4 i} g^3 \left( 12 b d (b^2 c^2 - 3 a b c d + 3 a^2 d^2) x \left( A + B \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - B n \log \left[ \frac{a + b x}{c + d x} \right] \right)^2 - \right. \\
 & 6 b^2 d^2 (b c - 3 a d) x^2 \left( A + B \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - B n \log \left[ \frac{a + b x}{c + d x} \right] \right)^2 + \\
 & 4 b^3 d^3 x^3 \left( A + B \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - B n \log \left[ \frac{a + b x}{c + d x} \right] \right)^2 - \\
 & 12 (b c - a d)^3 \left( A + B \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - B n \log \left[ \frac{a + b x}{c + d x} \right] \right)^2 \log [c + d x] + \\
 & 36 a B d n \left( A + B \log \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - B n \log \left[ \frac{a + b x}{c + d x} \right] \right) \\
 & \left( -2 b^2 c^2 + 2 a b c d - b^2 c d x + a b d^2 x + 2 b^2 c^2 \log \left[ \frac{c}{d} + x \right] - b^2 c^2 \log \left[ \frac{c}{d} + x \right]^2 - \right. \\
 & a^2 d^2 \log [a + b x] - 2 b^2 c d x \log \left[ \frac{a + b x}{c + d x} \right] + b^2 d^2 x^2 \log \left[ \frac{a + b x}{c + d x} \right] + b^2 c^2 \log [c + d x] + \\
 & \left. 2 b^2 c^2 \log \left[ \frac{c}{d} + x \right] \log [c + d x] + 2 b^2 c^2 \log \left[ \frac{a + b x}{c + d x} \right] \log [c + d x] - 2 b c \log \left[ \frac{a}{b} + x \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( a d + b c \operatorname{Log}[c+d x] - b c \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + 2 b^2 c^2 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \\
 4 B n & \left( A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \left( 6 b^3 c^3 - 6 a b^2 c^2 d + 5 b^3 c^2 d x - \right. \\
 & 3 a b^2 c d^2 x - 2 a^2 b d^3 x - b^3 c d^2 x^2 + a b^2 d^3 x^2 - 6 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] + 3 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + \\
 & 3 a^2 b c d^2 \operatorname{Log}[a+b x] + 2 a^3 d^3 \operatorname{Log}[a+b x] + 6 b^3 c^2 d x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] - \\
 & 3 b^3 c d^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 2 b^3 d^3 x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] - 5 b^3 c^3 \operatorname{Log}[c+d x] - \\
 & 6 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x] - 6 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x] + 6 b^2 c^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \\
 & \left. \left( a d + b c \operatorname{Log}[c+d x] - b c \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - 6 b^3 c^3 \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) - \\
 12 a^3 B d^3 n & \left( A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + 2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \operatorname{Log}[c+d x] - \right. \\
 & \left. 2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) - \\
 36 a^2 B d^2 n & \left( A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left( -2 d(a+b x) \left(-1 + \operatorname{Log}\left[\frac{a}{b}+x\right]\right) + 2 b(c+d x) \left(-1 + \operatorname{Log}\left[\frac{c}{d}+x\right]\right) - b c \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + \right. \\
 & 2 b \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) (d x - c \operatorname{Log}[c+d x]) + \\
 & \left. 2 b c \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) + \\
 4 a^3 B^2 d^3 n^2 & \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^3 + 3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) \right) + \\
 & 3 \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 \operatorname{Log}[c+d x] + 3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 6 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 3 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) + 6 \operatorname{Log}\left[\frac{c}{d}+x\right] \\
 & \left. \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] - 6 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) + \\
 B^2 n^2 & \left( 45 b^3 c^3 - 20 a b^2 c^2 d + 21 a^2 b c d^2 + 4 b^3 c^2 d x - 8 a b^2 c d^2 x + 4 a^2 b d^3 x - \right. \\
 & \left. 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] + 44 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] - 18 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 12 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right]^2+6 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right]^2+4 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2-18 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 24 a b^2 c^2 d \operatorname{Log}\left[\frac{c}{d}+x\right]+24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right]-12 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right]- \\
 & 8 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right]-2 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2+8 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^3+ \\
 & 10 a^2 b c d^2 \operatorname{Log}[a+b x]-12 a^3 d^3 \operatorname{Log}[a+b x]-12 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]- \\
 & 8 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[a+b x]+12 a^2 b c d^2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]+ \\
 & 8 a^3 d^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[a+b x]-12 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+24 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]- \\
 & 24 a b^2 c^2 d \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+20 b^3 c^2 d x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-12 a b^2 c d^2 x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]- \\
 & 8 a^2 b d^3 x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-4 b^3 c d^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+4 a b^2 d^3 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \\
 & 24 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]-24 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \\
 & 12 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+12 a^2 b c d^2 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \\
 & 8 a^3 d^3 \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+12 b^3 c^2 d x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2- \\
 & 6 b^3 c d^2 x^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+4 b^3 d^3 x^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+18 b^3 c^3 \operatorname{Log}[c+d x]+ \\
 & 16 a b^2 c^2 d \operatorname{Log}[c+d x]+8 a^2 b c d^2 \operatorname{Log}[c+d x]+20 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}[c+d x]- \\
 & 12 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}[c+d x]-20 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]+ \\
 & 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}[c+d x]-12 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \operatorname{Log}[c+d x]- \\
 & 20 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x]+24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x]- \\
 & 24 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x]-12 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 \operatorname{Log}[c+d x]- \\
 & 44 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+24 a b^2 c^2 d \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \\
 & 12 a^2 b c d^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+8 a^3 d^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \\
 & 12 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]-24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
 & 24 b^3 c^3 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\
 & 4\left(11 b^3 c^3-6 a b^2 c^2 d-3 a^2 b c d^2-2 a^3 d^3+6 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right]+6 b^3 c^3 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \\
 & \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-24 b^3 c^3 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]+
 \end{aligned}$$

$$\begin{aligned}
 & 24 b^3 c^3 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + 24 b^3 c^3 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + \\
 & 12 a^2 B^2 d^2 n^2 \left( 3 d (a+bx) \left( 2 - 2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{a}{b}+x\right]^2 \right) - bc \text{Log}\left[\frac{c}{d}+x\right]^3 + \right. \\
 & 3 b (c+dx) \left( 2 - 2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2 \right) + \\
 & 3 b \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 (dx - c \text{Log}[c+dx]) - \\
 & 6 \left( ad + 2 b dx - b dx \text{Log}\left[\frac{c}{d}+x\right] - bc \text{Log}[c+dx] + \right. \\
 & \quad \text{Log}\left[\frac{a}{b}+x\right] \left( -d(a+bx) + d(a+bx) \text{Log}\left[\frac{c}{d}+x\right] + (bc-ad) \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + \\
 & \quad (bc-ad) \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \left. \right) + 3 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \\
 & \left( -2 d (a+bx) \left( -1 + \text{Log}\left[\frac{a}{b}+x\right] \right) + 2 b (c+dx) \left( -1 + \text{Log}\left[\frac{c}{d}+x\right] \right) - bc \text{Log}\left[\frac{c}{d}+x\right]^2 + \right. \\
 & \quad \left. 2 bc \left( \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) - \\
 & 3 bc \left( \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \right. \\
 & \quad \left. 2 \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] \right) + 3 bc \left( \text{Log}\left[\frac{c}{d}+x\right]^2 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - \right. \\
 & \quad \left. 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right) \left. \right) - \\
 & 3 a B^2 d n^2 \left( 12 b c d (a+bx) \left( 2 - 2 \text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{a}{b}+x\right]^2 \right) + \right. \\
 & 3 d^2 (a+bx) \left( 7 a - bx + (-6 a + 2 b x) \text{Log}\left[\frac{a}{b}+x\right] + 2 (a - b x) \text{Log}\left[\frac{a}{b}+x\right]^2 \right) - \\
 & 4 b^2 c^2 \text{Log}\left[\frac{c}{d}+x\right]^3 + 12 b^2 c (c+dx) \left( 2 - 2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2 \right) + \\
 & 3 b^2 (c+dx) \left( 7 c - dx + (-6 c + 2 d x) \text{Log}\left[\frac{c}{d}+x\right] + 2 (c - d x) \text{Log}\left[\frac{c}{d}+x\right]^2 \right) - \\
 & 6 b^2 \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a+bx}{c+dx}\right] \right)^2 (dx (-2 c + dx) + 2 c^2 \text{Log}[c+dx]) + \\
 & 6 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{c}{d}+x\right] - \text{Log}\left[\frac{a+bx}{c+dx}\right] \right) \\
 & \left( -4 b c d (a+bx) \left( -1 + \text{Log}\left[\frac{a}{b}+x\right] \right) + 4 b^2 c (c+dx) \left( -1 + \text{Log}\left[\frac{c}{d}+x\right] \right) - \right. \\
 & \quad \left. 2 b^2 c^2 \text{Log}\left[\frac{c}{d}+x\right]^2 + d^2 \left( b x (2 a - b x) + 2 b^2 x^2 \text{Log}\left[\frac{a}{b}+x\right] - 2 a^2 \text{Log}[a+bx] \right) \right) + \\
 & \quad \left. b^2 \left( d x (-2 c + dx) - 2 d^2 x^2 \text{Log}\left[\frac{c}{d}+x\right] + 2 c^2 \text{Log}[c+dx] \right) \right) +
 \end{aligned}$$



$$\begin{aligned}
 & 4 b^2 c^2 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) - \\
 & 12 b^2 c^2 \left( \text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - \right. \\
 & \left. 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \right) - 6 \left( 2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - \right. \\
 & \left. 2 a b d^2 x \text{Log}\left[\frac{c}{d} + x\right] + b^2 d^2 x^2 \text{Log}\left[\frac{c}{d} + x\right] - a^2 d^2 \text{Log}[a+b x] - b^2 c^2 \text{Log}[c+d x] - 2 a b c \right. \\
 & \left. d \text{Log}[c+d x] - \text{Log}\left[\frac{a}{b} + x\right] \left( b d (2 a c + b x (2 c - d x)) - 2 d^2 (a^2 - b^2 x^2) \text{Log}\left[\frac{c}{d} + x\right] + \right. \right. \\
 & \left. \left. (-2 b^2 c^2 + 2 a^2 d^2) \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + 2 (b^2 c^2 - a^2 d^2) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + \right. \\
 & \left. 4 b c \left( a d + 2 b d x - b d x \text{Log}\left[\frac{c}{d} + x\right] - b c \text{Log}[c+d x] + \text{Log}\left[\frac{a}{b} + x\right] \right. \right. \\
 & \left. \left. \left( -d(a+b x) + d(a+b x) \text{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + (b c - a d) \right. \right. \\
 & \left. \left. \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) - 2 b^2 c^2 \left( \text{Log}\left[\frac{c}{d} + x\right]^2 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] \right) - \right. \\
 & \left. \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \right) \right)
 \end{aligned}$$

**Problem 187: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^2 \left( A + B \text{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 573 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{B (b c - a d) g^2 n (a + b x) \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{d^2 i} - \frac{2 (b c - a d) g^2 (a + b x) \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{d^2 i} + \\
 & \frac{b^2 g^2 (c + d x)^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 d^3 i} - \frac{4 B (b c - a d)^2 g^2 n \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log} \left[ \frac{b c - a d}{b (c+d x)} \right]}{d^3 i} - \\
 & \frac{(b c - a d)^2 g^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \text{Log} \left[ \frac{b c - a d}{b (c+d x)} \right]}{d^3 i} + \frac{B^2 (b c - a d)^2 g^2 n^2 \text{Log} [c + d x]}{d^3 i} + \\
 & \frac{B (b c - a d)^2 g^2 n \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{Log} \left[ 1 - \frac{b (c+d x)}{d (a+b x)} \right]}{d^3 i} - \\
 & \frac{4 B^2 (b c - a d)^2 g^2 n^2 \text{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^3 i} - \\
 & \frac{2 B (b c - a d)^2 g^2 n \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \text{PolyLog} \left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^3 i} - \\
 & \frac{B^2 (b c - a d)^2 g^2 n^2 \text{PolyLog} \left[ 2, \frac{b (c+d x)}{d (a+b x)} \right]}{d^3 i} + \frac{2 B^2 (b c - a d)^2 g^2 n^2 \text{PolyLog} \left[ 3, \frac{d (a+b x)}{b (c+d x)} \right]}{d^3 i}
 \end{aligned}$$

Result (type 4, 2797 leaves):

$$\begin{aligned}
 & \frac{1}{12 d^3 i} g^2 \left( -12 b d (b c - 2 a d) x \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \right. \\
 & 6 b^2 d^2 x^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\
 & 12 (b c - a d)^2 \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 \text{Log} [c + d x] + \\
 & 12 B n \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \left( -2 b^2 c^2 + 2 a b c d - b^2 c d x + a b d^2 x + 2 b^2 c^2 \text{Log} \left[ \frac{c}{d} + x \right] - b^2 c^2 \text{Log} \left[ \frac{c}{d} + x \right]^2 - \right. \\
 & a^2 d^2 \text{Log} [a + b x] - 2 b^2 c d x \text{Log} \left[ \frac{a+b x}{c+d x} \right] + b^2 d^2 x^2 \text{Log} \left[ \frac{a+b x}{c+d x} \right] + b^2 c^2 \text{Log} [c + d x] + \\
 & 2 b^2 c^2 \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} [c + d x] + 2 b^2 c^2 \text{Log} \left[ \frac{a+b x}{c+d x} \right] \text{Log} [c + d x] - 2 b c \text{Log} \left[ \frac{a}{b} + x \right] \\
 & \left. \left( a d + b c \text{Log} [c + d x] - b c \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] \right) + 2 b^2 c^2 \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) - \\
 & 12 a^2 B d^2 n \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{c}{d} + x \right] - \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \text{Log} [c + d x] - \right. \\
 & \left. 2 \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c - a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c + a d} \right] \right) \right) - \\
 & 24 a B d n \left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -2 d (a+b x) \left( -1 + \log\left[\frac{a}{b} + x\right] \right) + 2 b (c+d x) \left( -1 + \log\left[\frac{c}{d} + x\right] \right) - b c \log\left[\frac{c}{d} + x\right]^2 + \right. \\
 & 2 b \left( \log\left[\frac{a}{b} + x\right] - \log\left[\frac{c}{d} + x\right] - \log\left[\frac{a+b x}{c+d x}\right] \right) (d x - c \log[c+d x]) + \\
 & \left. 2 b c \left( \log\left[\frac{a}{b} + x\right] \log\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) + \\
 & 4 a^2 B^2 d^2 n^2 \left( \log\left[\frac{c}{d} + x\right]^3 + 3 \log\left[\frac{c}{d} + x\right]^2 \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{d(a+b x)}{-b c + a d}\right] \right) \right) + \\
 & 3 \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{a+b x}{c+d x}\right] \right)^2 \log[c+d x] + 3 \log\left[\frac{a}{b} + x\right]^2 \log\left[\frac{b(c+d x)}{b c - a d}\right] + \\
 & 6 \log\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + 3 \left( \log\left[\frac{a}{b} + x\right] - \log\left[\frac{c}{d} + x\right] - \log\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left( \log\left[\frac{c}{d} + x\right]^2 - 2 \left( \log\left[\frac{a}{b} + x\right] \log\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) + 6 \log\left[\frac{c}{d} + x\right] \\
 & \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] - 6 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] - 6 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) + \\
 & 8 a B^2 d n^2 \left( 3 d (a+b x) \left( 2 - 2 \log\left[\frac{a}{b} + x\right] + \log\left[\frac{a}{b} + x\right]^2 \right) - b c \log\left[\frac{c}{d} + x\right]^3 + 3 b (c+d x) \right. \\
 & \left( 2 - 2 \log\left[\frac{c}{d} + x\right] + \log\left[\frac{c}{d} + x\right]^2 \right) + 3 b \left( -\log\left[\frac{a}{b} + x\right] + \log\left[\frac{c}{d} + x\right] + \log\left[\frac{a+b x}{c+d x}\right] \right)^2 \\
 & \left. (d x - c \log[c+d x]) - 6 \left( a d + 2 b d x - b d x \log\left[\frac{c}{d} + x\right] - b c \log[c+d x] + \right. \right. \\
 & \left. \left. \log\left[\frac{a}{b} + x\right] \left( -d (a+b x) + d (a+b x) \log\left[\frac{c}{d} + x\right] + (b c - a d) \log\left[\frac{b(c+d x)}{b c - a d}\right] \right) + \right. \right. \\
 & \left. \left. (b c - a d) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) + 3 \left( \log\left[\frac{a}{b} + x\right] - \log\left[\frac{c}{d} + x\right] - \log\left[\frac{a+b x}{c+d x}\right] \right) \right. \\
 & \left( -2 d (a+b x) \left( -1 + \log\left[\frac{a}{b} + x\right] \right) + 2 b (c+d x) \left( -1 + \log\left[\frac{c}{d} + x\right] \right) - b c \log\left[\frac{c}{d} + x\right]^2 + \right. \\
 & \left. 2 b c \left( \log\left[\frac{a}{b} + x\right] \log\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) - \\
 & 3 b c \left( \log\left[\frac{a}{b} + x\right]^2 \log\left[\frac{b(c+d x)}{b c - a d}\right] + 2 \log\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - \right. \\
 & \left. 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \right) + 3 b c \left( \log\left[\frac{c}{d} + x\right]^2 \left( \log\left[\frac{a}{b} + x\right] - \log\left[\frac{d(a+b x)}{-b c + a d}\right] \right) - \right. \\
 & \left. 2 \log\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \right) - \\
 & B^2 n^2 \left( 12 b c d (a+b x) \left( 2 - 2 \log\left[\frac{a}{b} + x\right] + \log\left[\frac{a}{b} + x\right]^2 \right) + 3 d^2 (a+b x) \right. \\
 & \left( 7 a - b x + (-6 a + 2 b x) \log\left[\frac{a}{b} + x\right] + 2 (a - b x) \log\left[\frac{a}{b} + x\right]^2 \right) - \\
 & \left. 4 b^2 c^2 \log\left[\frac{c}{d} + x\right]^3 + 12 b^2 c (c+d x) \left( 2 - 2 \log\left[\frac{c}{d} + x\right] + \log\left[\frac{c}{d} + x\right]^2 \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3 b^2 (c+d x) \left( 7 c-d x + (-6 c+2 d x) \operatorname{Log}\left[\frac{c}{d}+x\right] + 2(c-d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \right) - \\
 & 6 b^2 \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 (d x(-2 c+d x) + 2 c^2 \operatorname{Log}[c+d x]) + \\
 & 6 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{c}{d}+x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left( -4 b c d(a+b x) \left( -1 + \operatorname{Log}\left[\frac{a}{b}+x\right] \right) + 4 b^2 c(c+d x) \left( -1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - \right. \\
 & \quad \left. 2 b^2 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2 + d^2 \left( b x(2 a-b x) + 2 b^2 x^2 \operatorname{Log}\left[\frac{a}{b}+x\right] - 2 a^2 \operatorname{Log}[a+b x] \right) + \right. \\
 & \quad \left. b^2 \left( d x(-2 c+d x) - 2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 c^2 \operatorname{Log}[c+d x] \right) + \right. \\
 & \quad \left. 4 b^2 c^2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) - \\
 & 12 b^2 c^2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \right. \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) - 6 \left( 2 a b c d + 3 b^2 c d x + 3 a b d^2 x - b^2 d^2 x^2 - \right. \\
 & \quad \left. 2 a b d^2 x \operatorname{Log}\left[\frac{c}{d}+x\right] + b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right] - a^2 d^2 \operatorname{Log}[a+b x] - b^2 c^2 \operatorname{Log}[c+d x] - 2 a b c \right. \\
 & \quad \left. d \operatorname{Log}[c+d x] - \operatorname{Log}\left[\frac{a}{b}+x\right] \left( b d(2 a c+b x(2 c-d x)) - 2 d^2(a^2-b^2 x^2) \operatorname{Log}\left[\frac{c}{d}+x\right] + \right. \right. \\
 & \quad \left. \left. (-2 b^2 c^2 + 2 a^2 d^2) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + 2(b^2 c^2 - a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \right. \\
 & \quad \left. 4 b c \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d}+x\right] - b c \operatorname{Log}[c+d x] + \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \\
 & \quad \left. \left. \left( -d(a+b x) + d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right] + (b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) + (b c-a d) \right. \right. \\
 & \quad \left. \left. \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) - 2 b^2 c^2 \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 \left( \operatorname{Log}\left[\frac{a}{b}+x\right] - \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) - \right. \\
 & \quad \left. \left. 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right)
 \end{aligned}$$

**Problem 188: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 303 leaves, 9 steps):

$$\begin{aligned}
 & \frac{g (a+b x) \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{d i} + \frac{2 B (b c-a d) g n \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{Log}\left[ \frac{b c-a d}{b (c+d x)} \right]}{d^2 i} + \\
 & \frac{(b c-a d) g \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \operatorname{Log}\left[ \frac{b c-a d}{b (c+d x)} \right]}{d^2 i} + \frac{2 B^2 (b c-a d) g n^2 \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^2 i} + \\
 & \frac{2 B (b c-a d) g n \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^2 i} - \\
 & \frac{2 B^2 (b c-a d) g n^2 \operatorname{PolyLog}\left[ 3, \frac{d (a+b x)}{b (c+d x)} \right]}{d^2 i}
 \end{aligned}$$

Result (type 4, 1367 leaves):

$$\begin{aligned}
 & \frac{1}{3 d^2 i} g \left( 3 b d x \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 - \right. \\
 & \quad 3 (b c-a d) \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 \operatorname{Log}[c+d x] - \\
 & \quad 3 a B d n \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left( \operatorname{Log}\left[ \frac{c}{d} + x \right]^2 + 2 \left( \operatorname{Log}\left[ \frac{a}{b} + x \right] - \operatorname{Log}\left[ \frac{c}{d} + x \right] - \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \operatorname{Log}[c+d x] - \right. \\
 & \quad \left. 2 \left( \operatorname{Log}\left[ \frac{a}{b} + x \right] \operatorname{Log}\left[ \frac{b (c+d x)}{b c-a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right) \right) - \\
 & \quad 3 B n \left( A+B \operatorname{Log}\left[ e\left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left( -2 d (a+b x) \left( -1 + \operatorname{Log}\left[ \frac{a}{b} + x \right] \right) + 2 b (c+d x) \left( -1 + \operatorname{Log}\left[ \frac{c}{d} + x \right] \right) - b c \operatorname{Log}\left[ \frac{c}{d} + x \right]^2 + \right. \\
 & \quad 2 b \left( \operatorname{Log}\left[ \frac{a}{b} + x \right] - \operatorname{Log}\left[ \frac{c}{d} + x \right] - \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) (d x - c \operatorname{Log}[c+d x]) + \\
 & \quad \left. 2 b c \left( \operatorname{Log}\left[ \frac{a}{b} + x \right] \operatorname{Log}\left[ \frac{b (c+d x)}{b c-a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right) \right) + \\
 & \quad a B^2 d n^2 \left( \operatorname{Log}\left[ \frac{c}{d} + x \right]^3 + 3 \operatorname{Log}\left[ \frac{c}{d} + x \right]^2 \left( -\operatorname{Log}\left[ \frac{a}{b} + x \right] + \operatorname{Log}\left[ \frac{d (a+b x)}{-b c+a d} \right] \right) + \right. \\
 & \quad 3 \left( -\operatorname{Log}\left[ \frac{a}{b} + x \right] + \operatorname{Log}\left[ \frac{c}{d} + x \right] + \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 \operatorname{Log}[c+d x] + 3 \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 \operatorname{Log}\left[ \frac{b (c+d x)}{b c-a d} \right] + \\
 & \quad 6 \operatorname{Log}\left[ \frac{a}{b} + x \right] \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{-b c+a d} \right] + 3 \left( \operatorname{Log}\left[ \frac{a}{b} + x \right] - \operatorname{Log}\left[ \frac{c}{d} + x \right] - \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left( \operatorname{Log}\left[ \frac{c}{d} + x \right]^2 - 2 \left( \operatorname{Log}\left[ \frac{a}{b} + x \right] \operatorname{Log}\left[ \frac{b (c+d x)}{b c-a d} \right] + \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right) \right) + 6 \operatorname{Log}\left[ \frac{c}{d} + x \right] \\
 & \quad \operatorname{PolyLog}\left[ 2, \frac{b (c+d x)}{b c-a d} \right] - 6 \operatorname{PolyLog}\left[ 3, \frac{d (a+b x)}{-b c+a d} \right] - 6 \operatorname{PolyLog}\left[ 3, \frac{b (c+d x)}{b c-a d} \right] \right) + \\
 & \quad B^2 n^2 \left( 3 d (a+b x) \left( 2 - 2 \operatorname{Log}\left[ \frac{a}{b} + x \right] + \operatorname{Log}\left[ \frac{a}{b} + x \right]^2 \right) - b c \operatorname{Log}\left[ \frac{c}{d} + x \right]^3 + 3 b (c+d x) \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right) + 3 b \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 \\
 & (d x - c \operatorname{Log}[c+d x]) - 6 \left( a d + 2 b d x - b d x \operatorname{Log}\left[\frac{c}{d} + x\right] - b c \operatorname{Log}[c+d x] + \right. \\
 & \left. \operatorname{Log}\left[\frac{a}{b} + x\right] \left( -d(a+b x) + d(a+b x) \operatorname{Log}\left[\frac{c}{d} + x\right] + (b c - a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] \right) + \right. \\
 & \left. (b c - a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) + 3 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{c}{d} + x\right] - \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \right) \\
 & \left( -2 d(a+b x) \left( -1 + \operatorname{Log}\left[\frac{a}{b} + x\right] \right) + 2 b(c+d x) \left( -1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b c \operatorname{Log}\left[\frac{c}{d} + x\right]^2 + \right. \\
 & \left. 2 b c \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] \right) \right) - \\
 & 3 b c \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - \right. \\
 & \left. 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right] \right) + 3 b c \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \left( \operatorname{Log}\left[\frac{a}{b} + x\right] - \operatorname{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] \right) - \right. \\
 & \left. 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right] \right) \Big)
 \end{aligned}$$

**Problem 189: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{c i + d i x} dx$$

Optimal (type 4, 137 leaves, 4 steps):

$$\frac{\left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \operatorname{Log}\left[ \frac{b c - a d}{b(c+d x)} \right]}{d i} - \frac{2 B n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{PolyLog}\left[ 2, \frac{d(a+b x)}{b(c+d x)} \right]}{d i} + \frac{2 B^2 n^2 \operatorname{PolyLog}\left[ 3, \frac{d(a+b x)}{b(c+d x)} \right]}{d i}$$

Result (type 4, 537 leaves):

$$\begin{aligned}
 & \frac{1}{3 d i} \left( 3 \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 \operatorname{Log} [c+d x] - \right. \\
 & \quad 3 B n \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - B n \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left( \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 + 2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \operatorname{Log} [c+d x] - \right. \\
 & \quad \left. 2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right) \right) + \\
 & B^2 n^2 \left( \operatorname{Log} \left[ \frac{c}{d} + x \right]^3 + 3 \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{d(a+b x)}{-b c + a d} \right] \right) + \right. \\
 & \quad 3 \left( -\operatorname{Log} \left[ \frac{a}{b} + x \right] + \operatorname{Log} \left[ \frac{c}{d} + x \right] + \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 \operatorname{Log} [c+d x] + 3 \operatorname{Log} \left[ \frac{a}{b} + x \right]^2 \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] + \\
 & \quad 6 \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] + 3 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] - \operatorname{Log} \left[ \frac{c}{d} + x \right] - \operatorname{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \\
 & \quad \left( \operatorname{Log} \left[ \frac{c}{d} + x \right]^2 - 2 \left( \operatorname{Log} \left[ \frac{a}{b} + x \right] \operatorname{Log} \left[ \frac{b(c+d x)}{b c - a d} \right] + \operatorname{PolyLog} \left[ 2, \frac{d(a+b x)}{-b c + a d} \right] \right) \right) + 6 \operatorname{Log} \left[ \frac{c}{d} + x \right] \\
 & \quad \left. \operatorname{PolyLog} \left[ 2, \frac{b(c+d x)}{b c - a d} \right] - 6 \operatorname{PolyLog} \left[ 3, \frac{d(a+b x)}{-b c + a d} \right] - 6 \operatorname{PolyLog} \left[ 3, \frac{b(c+d x)}{b c - a d} \right] \right)
 \end{aligned}$$

**Problem 191: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(a g + b g x)^2 (c i + d i x)} dx$$

Optimal (type 3, 199 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{2 b B^2 n^2 (c+d x)}{(b c - a d)^2 g^2 i (a+b x)} - \frac{2 b B n (c+d x) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{(b c - a d)^2 g^2 i (a+b x)} - \\
 & \frac{b (c+d x) \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(b c - a d)^2 g^2 i (a+b x)} - \frac{d \left( A + B \operatorname{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^3}{3 B (b c - a d)^2 g^2 i n}
 \end{aligned}$$

Result (type 3, 793 leaves):

$$\begin{aligned}
 & - \frac{B^2 d n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^3}{3(b c-a d)^2 g^2 i} + \frac{2 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \left(A+B n+B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)}{(-b c+a d) g^2 i(a+b x)} + \\
 & \left(\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2\left(-a A B d n-b B^2 c n^2-A b B d n x-b B^2 d n^2 x-a B^2 d n\right.\right. \\
 & \quad \left.\left.\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)-b B^2 d n x\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)\right) / \\
 & \left((-b c+a d)^2 g^2 i(a+b x)\right)+\left(-A^2-2 A B n-2 B^2 n^2-2 A B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)-\right. \\
 & \quad \left.2 B^2 n\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)-B^2\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) / \\
 & \left((b c-a d) g^2 i(a+b x)\right)-\frac{1}{(b c-a d)^2 g^2 i} d \operatorname{Log}[a+b x] \\
 & \left(A^2+2 A B n+2 B^2 n^2+2 A B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+\right. \\
 & \quad \left.2 B^2 n\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+B^2\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right)+ \\
 & \frac{1}{(b c-a d)^2 g^2 i} d\left(A^2+2 A B n+2 B^2 n^2+2 A B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+2 B^2 n\right. \\
 & \quad \left.\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+B^2\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) \operatorname{Log}[c+d x]
 \end{aligned}$$

**Problem 192: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(a g+b g x)^3(c i+d i x)} d x$$

Optimal (type 3, 369 leaves, 9 steps):

$$\begin{aligned}
 & \frac{4 b B^2 d n^2(c+d x)}{(b c-a d)^3 g^3 i(a+b x)}-\frac{b^2 B^2 n^2(c+d x)^2}{4(b c-a d)^3 g^3 i(a+b x)^2}+\frac{4 b B d n(c+d x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c-a d)^3 g^3 i(a+b x)}- \\
 & \frac{b^2 B n(c+d x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2(b c-a d)^3 g^3 i(a+b x)^2}+\frac{2 b d(c+d x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^3 g^3 i(a+b x)}- \\
 & \frac{b^2(c+d x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2(b c-a d)^3 g^3 i(a+b x)^2}+\frac{d^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{3 B(b c-a d)^3 g^3 i n}
 \end{aligned}$$

Result (type 3, 975 leaves):



$$\frac{1}{12 (b c - a d)^3 g^3 i (a + b x)^2} \left( 4 B^2 d^2 n^2 (a + b x)^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^3 + 6 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 \right. \\ \left. \left( 2 a^2 A d^2 - b^2 B c^2 n + 4 a b B c d n + 4 a A b d^2 x + 2 b^2 B c d n x + 4 a b B d^2 n x + 2 A b^2 d^2 x^2 + \right. \right. \\ \left. \left. 3 b^2 B d^2 n x^2 + 2 B d^2 (a + b x)^2 \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] - 2 B d^2 n (a + b x)^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) - \right. \\ \left. 6 B (b c - a d) n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \left( 2 A b c - 6 a A d + b B c n - 7 a B d n - 4 A b d x - 6 b B d n x + \right. \right. \\ \left. \left. 2 B (-3 a d + b (c - 2 d x)) \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + 2 B n (-b c + 3 a d + 2 b d x) \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) - \right. \\ \left. 3 (b c - a d)^2 \left( 2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 - 2 B n (2 A + B n) \text{Log} \left[ \frac{a + b x}{c + d x} \right] + \right. \right. \\ \left. \left. 2 B^2 n^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 + 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \left( 2 A + B n - 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) + 6 d (b c - a d) \right. \\ \left. (a + b x) \left( 2 A^2 + 6 A B n + 7 B^2 n^2 + 2 B^2 \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 - 2 B n (2 A + 3 B n) \text{Log} \left[ \frac{a + b x}{c + d x} \right] + \right. \right. \\ \left. \left. 2 B^2 n^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 + 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \left( 2 A + 3 B n - 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) + 6 d^2 (a + b x)^2 \right. \\ \left. \text{Log} [a + b x] \left( 2 A^2 + 6 A B n + 7 B^2 n^2 + 2 B^2 \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 - 2 B n (2 A + 3 B n) \text{Log} \left[ \frac{a + b x}{c + d x} \right] + \right. \right. \\ \left. \left. 2 B^2 n^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 + 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \left( 2 A + 3 B n - 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) - \right. \\ \left. 6 d^2 (a + b x)^2 \left( 2 A^2 + 6 A B n + 7 B^2 n^2 + 2 B^2 \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 - 2 B n (2 A + 3 B n) \text{Log} \left[ \frac{a + b x}{c + d x} \right] + \right. \right. \\ \left. \left. 2 B^2 n^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 + 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \left( 2 A + 3 B n - 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) \text{Log} [c + d x] \right)$$

**Problem 193: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left( A + B \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(a g + b g x)^4 (c i + d i x)} dx$$

Optimal (type 3, 543 leaves, 11 steps):

$$\begin{aligned}
 & - \frac{6 b B^2 d^2 n^2 (c+d x)}{(b c-a d)^4 g^4 i (a+b x)} + \frac{3 b^2 B^2 d n^2 (c+d x)^2}{4 (b c-a d)^4 g^4 i (a+b x)^2} - \\
 & \frac{2 b^3 B^2 n^2 (c+d x)^3}{27 (b c-a d)^4 g^4 i (a+b x)^3} - \frac{6 b B d^2 n (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c-a d)^4 g^4 i (a+b x)} + \\
 & \frac{3 b^2 B d n (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 (b c-a d)^4 g^4 i (a+b x)^2} - \frac{2 b^3 B n (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{9 (b c-a d)^4 g^4 i (a+b x)^3} - \\
 & \frac{3 b d^2 (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^4 g^4 i (a+b x)} + \frac{3 b^2 d (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 (b c-a d)^4 g^4 i (a+b x)^2} - \\
 & \frac{b^3 (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{3 (b c-a d)^4 g^4 i (a+b x)^3} - \frac{d^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{3 B (b c-a d)^4 g^4 i n}
 \end{aligned}$$

Result(type 3, 1295 leaves):

$$\begin{aligned}
 & \frac{1}{108 (b c - a d)^4 g^4 i (a + b x)^3} \\
 & \left( 36 B^2 d^3 n^2 (a + b x)^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^3 + 18 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 \left( 6 a^3 A d^3 + 2 b^3 B c^3 n - 9 a b^2 B c^2 d n + \right. \right. \\
 & \quad 18 a^2 b B c d^2 n + 18 a^2 A b d^3 x - 3 b^3 B c^2 d n x + 18 a b^2 B c d^2 n x + 18 a^2 b B d^3 n x + \\
 & \quad \left. 18 a A b^2 d^3 x^2 + 6 b^3 B c d^2 n x^2 + 27 a b^2 B d^3 n x^2 + 6 A b^3 d^3 x^3 + 11 b^3 B d^3 n x^3 + \right. \\
 & \quad \left. 6 B d^3 (a + b x)^3 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 B d^3 n (a + b x)^3 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) - 3 d (b c - a d)^2 (a + b x) \\
 & \quad \left( 18 A^2 + 30 A B n + 19 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 B n (6 A + 5 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 6 A + 5 B n - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
 & 6 d^2 (b c - a d) (a + b x)^2 \left( 18 A^2 + 66 A B n + 85 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - \right. \\
 & \quad 6 B n (6 A + 11 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 18 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \\
 & \quad \left. 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 6 A + 11 B n - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 6 d^3 (a + b x)^3 \operatorname{Log}[a + b x] \\
 & \quad \left( 18 A^2 + 66 A B n + 85 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 B n (6 A + 11 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 6 A + 11 B n - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
 & 4 (b c - a d)^3 \left( 9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 B n (3 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 9 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 3 A + B n - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 6 B (b c - a d) n \\
 & \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left( 3 d (-b c + a d) (a + b x) \left( 6 A + 5 B n + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \left. 6 d^2 (a + b x)^2 \left( 6 A + 11 B n + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \left. 4 (b c - a d)^2 \left( 3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - 6 d^3 (a + b x)^3 \\
 & \quad \left( 18 A^2 + 66 A B n + 85 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 6 B n (6 A + 11 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 6 A + 11 B n - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \operatorname{Log}[c + d x] \Big)
 \end{aligned}$$

**Problem 194: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left( A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{(c i + d i x)^2} dx$$

Optimal (type 4, 770 leaves, 18 steps):

$$\begin{aligned} & \frac{2 A B (b c - a d)^2 g^3 n (a + b x)}{d^3 i^2 (c + d x)} - \frac{2 B^2 (b c - a d)^2 g^3 n^2 (a + b x)}{d^3 i^2 (c + d x)} + \\ & \frac{2 B^2 (b c - a d)^2 g^3 n (a + b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d^3 i^2 (c + d x)} - \frac{b B (b c - a d) g^3 n (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{d^3 i^2} - \\ & \frac{3 b (b c - a d) g^3 (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{d^3 i^2} - \frac{(b c - a d)^2 g^3 (a + b x) \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{d^3 i^2 (c + d x)} + \\ & \frac{b^3 g^3 (c + d x)^2 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 d^4 i^2} - \frac{6 b B (b c - a d)^2 g^3 n \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right]}{d^4 i^2} - \\ & \frac{3 b (b c - a d)^2 g^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \operatorname{Log}\left[\frac{b c - a d}{b (c + d x)}\right]}{d^4 i^2} + \frac{b B^2 (b c - a d)^2 g^3 n^2 \operatorname{Log}[c + d x]}{d^4 i^2} + \\ & \frac{b B (b c - a d)^2 g^3 n \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{Log}\left[1 - \frac{b (c + d x)}{d (a + b x)}\right]}{d^4 i^2} - \\ & \frac{6 b B^2 (b c - a d)^2 g^3 n^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i^2} - \\ & \frac{6 b B (b c - a d)^2 g^3 n \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i^2} - \\ & \frac{b B^2 (b c - a d)^2 g^3 n^2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{d (a + b x)}\right]}{d^4 i^2} + \frac{6 b B^2 (b c - a d)^2 g^3 n^2 \operatorname{PolyLog}\left[3, \frac{d (a + b x)}{b (c + d x)}\right]}{d^4 i^2} \end{aligned}$$

Result (type 4, 5396 leaves):

$$\begin{aligned} & \frac{a^3 B^2 g^3 n^2 (a + b x) \left(2 - 2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2\right)}{(b c - a d) i^2 (c + d x)} - \\ & \frac{b^2 (2 b c - 3 a d) g^3 x \left(A + B \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)^2}{d^3 i^2} + \\ & \frac{b^3 g^3 x^2 \left(A + B \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)^2}{2 d^2 i^2} + \\ & \frac{1}{d^4 i^2 (c + d x)} \left( A^2 b^3 c^3 g^3 - 3 a A^2 b^2 c^2 d g^3 + 3 a^2 A^2 b c d^2 g^3 - a^3 A^2 d^3 g^3 + 2 A b^3 B c^3 g^3 \right. \\ & \quad \left. \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - 6 a A b^2 B c^2 d g^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \right) + \\ & \quad 6 a^2 A b B c d^2 g^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - 2 a^3 A B d^3 g^3 \\ & \quad \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + b^3 B^2 c^3 g^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 - \\ & \quad \left. 3 a b^2 B^2 c^2 d g^3 \left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + 3 a^2 b B^2 c d^2 g^3 \right) \end{aligned}$$

$$\begin{aligned}
 & \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 - a^3 B^2 d^3 g^3 \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right)^2 + \\
 & \frac{1}{d^4 i^2} 3 b (b c - a d)^2 g^3 \left( A + B \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right)^2 \text{Log}[c+d x] + \\
 & \frac{1}{i^2} 2 a^3 B g^3 n \left( A + B \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) \\
 & \left( \frac{\left(\frac{c}{d} + x\right) \left(\text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{(c+d x)^2 \text{Log}\left[\frac{c}{d} + x\right]} + \frac{\frac{d\left(\frac{a}{b} + x\right) \text{Log}\left[\frac{a}{b} + x\right]}{\left(-c + \frac{a d}{b}\right)^2 \left(1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right)} + \frac{\text{Log}\left[1 - \frac{d\left(\frac{a}{b} + x\right)}{-c + \frac{a d}{b}}\right]}{-c + \frac{a d}{b}}}{d} - \right. \\
 & \left. \frac{-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]}{d(c+d x)} \right) + \\
 & \frac{1}{i^2} 2 b^3 B g^3 n \left( A + B \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right) \\
 & \left( -\frac{2 c\left(\frac{a}{b} + x\right)\left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{d^3} + \frac{2 c\left(\frac{c}{d} + x\right)\left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3} - \frac{3 c^2 \text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^4} - \right. \\
 & \frac{c^3\left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^4(c+d x)} + \frac{-\frac{1}{2} b\left(-\frac{a x}{b^2} + \frac{x^2}{2 b} + \frac{a^2 \text{Log}[a+b x]}{b^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{a+b x}{b}\right]}{d^2} - \\
 & \frac{c^3\left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d(c+d x)} - \frac{b \text{Log}[a+b x]}{d(-b c+a d)} + \frac{b \text{Log}[c+d x]}{d(-b c+a d)}\right)}{d^3} - \frac{-\frac{1}{2} d\left(-\frac{c x}{d^2} + \frac{x^2}{2 d} + \frac{c^2 \text{Log}[c+d x]}{d^3}\right) + \frac{1}{2} x^2 \text{Log}\left[\frac{c+d x}{d}\right]}{d^2} + \\
 & \frac{1}{2 d^4} \left( -4 c d x + d^2 x^2 + \frac{2 c^3}{c+d x} + 6 c^2 \text{Log}[c+d x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \right. \\
 & \left. \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) + \frac{3 c^2 \left( \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right)}{d^4} \left. \right) + \\
 & \frac{1}{i^2} 6 a b^2 B g^3 n \left( A + B \left( \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) \right)
 \end{aligned}$$

$$\left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \text{Log}\left[\frac{a}{b} + x\right]\right)}{d^2} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2} + \frac{c \text{Log}\left[\frac{c}{d} + x\right]^2}{d^3} + \right.$$

$$\frac{c^2 \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^3 (c + d x)} + \frac{c^2 \left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \text{Log}[a + b x]}{d (-b c + a d)} + \frac{b \text{Log}[c + d x]}{d (-b c + a d)}\right)}{d^2} + \frac{1}{d^3}$$

$$\left( d x - \frac{c^2}{c + d x} - 2 c \text{Log}[c + d x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) -$$

$$\left. \frac{2 c \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]\right)}{d^3} \right) +$$

$$\frac{1}{i^2} 6 a^2 b B g^3 n \left( A + B \left( \text{Log}\left[e \left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right)$$

$$\left( -\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} - \frac{c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2 (c + d x)} - \frac{c \left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \text{Log}[a + b x]}{d (-b c + a d)} + \frac{b \text{Log}[c + d x]}{d (-b c + a d)}\right)}{d} + \frac{1}{d^2} \right.$$

$$\left. \left( \frac{c}{c + d x} + \text{Log}[c + d x] \right) \left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) + \right.$$

$$\left. \frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right]}{d^2} \right) +$$

$$\frac{1}{i^2} b^3 B^2 g^3 n^2 \left( -\frac{2 c (a + b x) \left(2 - 2 \text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{a}{b} + x\right]^2\right)}{b d^3} + \frac{1}{4 b^2 d^2} \right.$$

$$(a + b x) \left( -7 a + b x + (6 a - 2 b x) \text{Log}\left[\frac{a}{b} + x\right] - 2 (a - b x) \text{Log}\left[\frac{a}{b} + x\right]^2 \right) + \frac{c^2 \text{Log}\left[\frac{c}{d} + x\right]^3}{d^4} -$$

$$\frac{2 c (c + d x) \left(2 - 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^4} + \frac{c^3 \left(2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^4 (c + d x)} +$$

$$\frac{1}{4 d^4} (c + d x) \left( -7 c + d x + (6 c - 2 d x) \text{Log}\left[\frac{c}{d} + x\right] - 2 (c - d x) \text{Log}\left[\frac{c}{d} + x\right]^2 \right) +$$

$$\frac{1}{2 d^4} \left( -4 c d x + d^2 x^2 + \frac{2 c^3}{c + d x} + 6 c^2 \text{Log}[c + d x] \right)$$

$$\left( -\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2 - \left( c^3 \left( -d (a + b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + \right.$$

$$\begin{aligned}
 & \left. 2 b (c+d x) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+2 b(c+d x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right) / \\
 & \left(d^4(-b c+a d)(c+d x)+2\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)\right. \\
 & \left(-\frac{2 c\left(\frac{a}{b}+x\right)\left(-1+\operatorname{Log}\left[\frac{a}{b}+x\right]\right)}{d^3}+\frac{2 c\left(\frac{c}{d}+x\right)\left(-1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^3}-\frac{3 c^2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{2 d^4}-\right. \\
 & \left.\frac{c^3\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{d^4(c+d x)}+\frac{-\frac{1}{2} b\left(-\frac{a x}{b^2}+\frac{x^2}{2 b}+\frac{a^2 \operatorname{Log}[a+b x]}{b^3}\right)+\frac{1}{2} x^2 \operatorname{Log}\left[\frac{a+b x}{b}\right]}{d^2}-\right. \\
 & \left.\frac{c^3\left(-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)}-\frac{b \operatorname{Log}[a+b x]}{d(-b c+a d)}+\frac{b \operatorname{Log}[c+d x]}{d(-b c+a d)}\right)}{d^3}-\frac{-\frac{1}{2} d\left(-\frac{c x}{d^2}+\frac{x^2}{2 d}+\frac{c^2 \operatorname{Log}[c+d x]}{d^3}\right)+\frac{1}{2} x^2 \operatorname{Log}\left[\frac{c+d x}{d}\right]}{d^2}+\right. \\
 & \left.\frac{3 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{d^4}\right)+\frac{1}{d^4} \\
 & 3 c^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-\right. \\
 & \left.2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right)-2\left(-\frac{1}{b d^4}\right. \\
 & \left.2 c\left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right]-b c \operatorname{Log}[c+d x]+\operatorname{Log}\left[\frac{a}{b}+x\right]\left(-d(a+b x)+d(a+b x)\right.\right.\right. \\
 & \left.\left.\left.\operatorname{Log}\left[\frac{c}{d}+x\right]+(b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)\right)+(b c-a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)+ \\
 & \frac{1}{4 b^2 d^4}\left(-2 a b c d-3 b^2 c d x-3 a b d^2 x+b^2 d^2 x^2+2 a b d^2 x \operatorname{Log}\left[\frac{c}{d}+x\right]-\right. \\
 & \left.b^2 d^2 x^2 \operatorname{Log}\left[\frac{c}{d}+x\right]+a^2 d^2 \operatorname{Log}[a+b x]+b^2 c^2 \operatorname{Log}[c+d x]+2 a b c d \operatorname{Log}[c+d x]+ \right. \\
 & \left.\operatorname{Log}\left[\frac{a}{b}+x\right]\left(b d(2 a c+b x(2 c-d x))-2 d^2\left(a^2-b^2 x^2\right) \operatorname{Log}\left[\frac{c}{d}+x\right]+(-2 b^2 c^2+2 a^2 d^2)\right.\right. \\
 & \left.\left.\operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)+(-2 b^2 c^2+2 a^2 d^2) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)- \\
 & \left(c^3\left(2(b c-a d) \operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+b(c+d x)\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2-\right.\right.\right. \\
 & \left.\left.\left.2 \operatorname{Log}[a+b x]-2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}[c+d x]\right)\right)-\right. \\
 & \left.2 b(c+d x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right) / \left(2 d^4(-b c+a d)(c+d x)\right)+
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{2 d^4} 3 c^2 \left( \text{Log} \left[ \frac{c}{d} + x \right]^2 \left( \text{Log} \left[ \frac{a}{b} + x \right] - \text{Log} \left[ \frac{d (a+b x)}{-b c+a d} \right] \right) - 2 \text{Log} \left[ \frac{c}{d} + x \right] \right. \\
 & \quad \left. \text{PolyLog} \left[ 2, \frac{b (c+d x)}{b c-a d} \right] + 2 \text{PolyLog} \left[ 3, \frac{b (c+d x)}{b c-a d} \right] \right) \Bigg) + \\
 & \frac{1}{i^2} 3 a b^2 B^2 g^3 n^2 \left( \frac{(a+b x) \left( 2 - 2 \text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{a}{b} + x \right]^2 \right)}{b d^2} - \frac{2 c \text{Log} \left[ \frac{c}{d} + x \right]^3}{3 d^3} + \right. \\
 & \quad \frac{(c+d x) \left( 2 - 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{d^3} - \frac{c^2 \left( 2 + 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{d^3 (c+d x)} + \frac{1}{d^3} \\
 & \quad \left( d x - \frac{c^2}{c+d x} - 2 c \text{Log} [c+d x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right)^2 + \\
 & \quad \left( c^2 \left( -d (a+b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 + 2 b (c+d x) \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] + \right. \right. \\
 & \quad \left. \left. 2 b (c+d x) \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right) \right) / \\
 & \quad \left( d^3 (-b c+a d) (c+d x) \right) + 2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right) \\
 & \quad \left( \frac{\left( \frac{a}{b} + x \right) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{d^2} - \frac{\left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^2} + \frac{c \text{Log} \left[ \frac{c}{d} + x \right]^2}{d^3} + \right. \\
 & \quad \frac{c^2 \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^3 (c+d x)} + \frac{c^2 \left( -\frac{\text{Log} \left[ \frac{a}{b} + x \right]}{d (c+d x)} - \frac{b \text{Log} [a+b x]}{d (-b c+a d)} + \frac{b \text{Log} [c+d x]}{d (-b c+a d)} \right)}{d^2} - \\
 & \quad \left. \frac{2 c \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right)}{d^3} \right) - \frac{1}{d^3} \\
 & 2 c \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \text{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] + 2 \text{Log} \left[ \frac{a}{b} + x \right] \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c+a d} \right] - \right. \\
 & 2 \text{PolyLog} \left[ 3, \frac{d (a+b x)}{-b c+a d} \right] \Bigg) - 2 \left( \frac{1}{b d^3} \left( a d + 2 b d x - b d x \text{Log} \left[ \frac{c}{d} + x \right] - b c \text{Log} [c+d x] + \right. \right. \\
 & \quad \left. \left. \text{Log} \left[ \frac{a}{b} + x \right] \left( -d (a+b x) + d (a+b x) \text{Log} \left[ \frac{c}{d} + x \right] + (b c-a d) \text{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] \right) \right) + \\
 & \quad \left. (b c-a d) \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right) + \left( c^2 \left( 2 (b c-a d) \text{Log} \left[ \frac{a}{b} + x \right] \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right) + \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & b (c+d x) \left( \text{Log}\left[\frac{c}{d}+x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \\
 & \quad \left. 2 \text{Log}[c+d x] \right) - 2 b (c+d x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \Bigg) / \\
 & \left( 2 d^3 (-b c+a d) (c+d x) - \frac{1}{d^3} c \left( \text{Log}\left[\frac{c}{d}+x\right]^2 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) - \right. \right. \\
 & \quad \left. \left. 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \Bigg) + \\
 & \frac{1}{i^2} 3 a^2 b B^2 g^3 n^2 \left( \frac{\text{Log}\left[\frac{c}{d}+x\right]^3}{3 d^2} + \frac{c \left( 2 + 2 \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{c}{d}+x\right]^2 \right)}{d^2 (c+d x)} + \frac{1}{d^2} \right. \\
 & \quad \left( \frac{c}{c+d x} + \text{Log}[c+d x] \right) \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right)^2 - \\
 & \quad \left( c \left( -d(a+b x) \text{Log}\left[\frac{a}{b}+x\right]^2 + 2 b(c+d x) \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \right. \right. \\
 & \quad \left. \left. 2 b(c+d x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] \right) \right) / \left( d^2 (-b c+a d) (c+d x) \right) + \\
 & 2 \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) \left( -\frac{\text{Log}\left[\frac{c}{d}+x\right]^2}{2 d^2} - \frac{c \left( 1 + \text{Log}\left[\frac{c}{d}+x\right] \right)}{d^2 (c+d x)} - \right. \\
 & \quad \left. \frac{c \left( -\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)} - \frac{b \text{Log}[a+b x]}{d(-b c+a d)} + \frac{b \text{Log}[c+d x]}{d(-b c+a d)} \right)}{d} + \frac{\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^2} \right) \Bigg) + \\
 & \frac{1}{d^2} \left( \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \right. \\
 & \quad \left. 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) - 2 \left( -\left( \left( c \left( 2 (b c-a d) \text{Log}\left[\frac{a}{b}+x\right] \left( 1 + \text{Log}\left[\frac{c}{d}+x\right] \right) + b(c+d x) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left( \text{Log}\left[\frac{c}{d}+x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \text{Log}[c+d x] \right) + 2 \text{Log}[c+d x] \right) \right) - 2 \\
 & \quad \left. b(c+d x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \Bigg) / \left( 2 d^2 (-b c+a d) (c+d x) \right) + \frac{1}{2 d^2} \\
 & \left( \text{Log}\left[\frac{c}{d}+x\right]^2 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + \right.
 \end{aligned}$$



$$\begin{aligned}
 & c d g^2 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - a^2 B^2 d^2 g^2 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - \\
 & \frac{2 b (b c - a d) g^2 \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 \text{Log} [c+d x]}{d^3 i^2} + \frac{1}{i^2} \\
 & 2 a^2 B g^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( \frac{\left( \frac{c}{d} + x \right) \left( \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{(c+d x)^2 \text{Log} \left[ \frac{c}{d} + x \right]} + \frac{\frac{d \left( \frac{a}{b} + x \right) \text{Log} \left[ \frac{a}{b} + x \right]}{\left( -c + \frac{a d}{b} \right)^2 \left( 1 - \frac{d \left( \frac{a}{b} + x \right)}{-c + \frac{a d}{b}} \right)} + \frac{\text{Log} \left[ 1 - \frac{d \left( \frac{a}{b} + x \right)}{-c + \frac{a d}{b}} \right]}{-c + \frac{a d}{b}}}{d} - \right. \\
 & \left. \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right]}{d (c+d x)} \right) + \\
 & \frac{1}{i^2} 2 b^2 B g^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( \frac{\left( \frac{a}{b} + x \right) \left( -1 + \text{Log} \left[ \frac{a}{b} + x \right] \right)}{d^2} - \frac{\left( \frac{c}{d} + x \right) \left( -1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^2} + \frac{c \text{Log} \left[ \frac{c}{d} + x \right]^2}{d^3} + \right. \\
 & \frac{c^2 \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^3 (c+d x)} + \frac{c^2 \left( -\frac{\text{Log} \left[ \frac{a}{b} + x \right]}{d (c+d x)} - \frac{b \text{Log} [a+b x]}{d (-b c+a d)} + \frac{b \text{Log} [c+d x]}{d (-b c+a d)} \right)}{d^2} + \frac{1}{d^3} \\
 & \left( d x - \frac{c^2}{c+d x} - 2 c \text{Log} [c+d x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right) - \\
 & \left. \frac{2 c \left( \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c+d x)}{b c-a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a+b x)}{-b c+a d} \right] \right)}{d^3} \right) + \\
 & \frac{1}{i^2} 4 a b B g^2 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( -\frac{\text{Log}\left[\frac{c}{d}+x\right]^2}{2 d^2}-\frac{c\left(1+\text{Log}\left[\frac{c}{d}+x\right]\right)}{d^2(c+d x)}-\frac{c\left(-\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)}-\frac{b \text{Log}[a+b x]}{d(-b c+a d)}+\frac{b \text{Log}[c+d x]}{d(-b c+a d)}\right)}{d}+\frac{1}{d^2}\right. \\
 & \left.\left(\frac{c}{c+d x}+\text{Log}[c+d x]\right)\left(-\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]+\text{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)+\right. \\
 & \left.\frac{\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^2}\right)+ \\
 & \frac{1}{i^2} b^2 B^2 g^2 n^2 \left( \frac{(a+b x)\left(2-2 \text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{a}{b}+x\right]^2\right)}{b d^2}-\frac{2 c \text{Log}\left[\frac{c}{d}+x\right]^3}{3 d^3}+\right. \\
 & \left.\frac{(c+d x)\left(2-2 \text{Log}\left[\frac{c}{d}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]^2\right)}{d^3}-\frac{c^2\left(2+2 \text{Log}\left[\frac{c}{d}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]^2\right)}{d^3(c+d x)}+\frac{1}{d^3}\right. \\
 & \left.\left(d x-\frac{c^2}{c+d x}-2 c \text{Log}[c+d x]\right)\left(-\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]+\text{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)^2+\right. \\
 & \left.\left(c^2\left(-d(a+b x) \text{Log}\left[\frac{a}{b}+x\right]^2+2 b(c+d x) \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+2 b(c+d x)\right.\right.\right. \\
 & \left.\left.\left.\text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right) / \left(d^3(-b c+a d)(c+d x)+2\left(-\text{Log}\left[\frac{a}{b}+x\right]+\text{Log}\left[\frac{c}{d}+x\right]+\right.\right. \\
 & \left.\left.\text{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)\right)\left(\frac{\left(\frac{a}{b}+x\right)\left(-1+\text{Log}\left[\frac{a}{b}+x\right]\right)}{d^2}-\frac{\left(\frac{c}{d}+x\right)\left(-1+\text{Log}\left[\frac{c}{d}+x\right]\right)}{d^2}+\right. \\
 & \left.\frac{c \text{Log}\left[\frac{c}{d}+x\right]^2}{d^3}+\frac{c^2\left(1+\text{Log}\left[\frac{c}{d}+x\right]\right)}{d^3(c+d x)}+\frac{c^2\left(-\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)}-\frac{b \text{Log}[a+b x]}{d(-b c+a d)}+\frac{b \text{Log}[c+d x]}{d(-b c+a d)}\right)}{d^2}-\right. \\
 & \left.\frac{2 c\left(\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+\text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)}{d^3}\right)-\frac{1}{d^3} \\
 & 2 c\left(\text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-\right. \\
 & \left.2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]\right)-2\left(\frac{1}{b d^3}\left(a d+2 b d x-b d x \text{Log}\left[\frac{c}{d}+x\right]-b c \text{Log}[c+d x]+ \right.\right. \\
 & \left.\left.\text{Log}\left[\frac{a}{b}+x\right]\left(-d(a+b x)+d(a+b x) \text{Log}\left[\frac{c}{d}+x\right]+(b c-a d) \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)\right)+
 \end{aligned}$$

$$\begin{aligned}
 & (b c - a d) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] + \left(c^2 \left(2(b c - a d) \text{Log}\left[\frac{a}{b} + x\right] \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right) + \right. \right. \\
 & \quad b(c+d x) \left(\text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + \right. \\
 & \quad \quad \left. \left. 2 \text{Log}[c+d x]\right) - 2 b(c+d x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]\right) \Bigg) / \\
 & \left(2 d^3(-b c + a d)(c+d x) - \frac{1}{d^3} c \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right]\right) - \right. \right. \\
 & \quad \left. \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c - a d}\right]\right)\right) \Bigg) + \\
 & \frac{1}{i^2} 2 a b B^2 g^2 n^2 \left( \frac{\text{Log}\left[\frac{c}{d} + x\right]^3}{3 d^2} + \frac{c \left(2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right)}{d^2(c+d x)} + \frac{1}{d^2} \right. \\
 & \quad \left. \left(\frac{c}{c+d x} + \text{Log}[c+d x]\right) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]\right)^2 - \right. \\
 & \quad \left. \left(c \left(-d(a+b x) \text{Log}\left[\frac{a}{b} + x\right]^2 + 2 b(c+d x) \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \right. \right. \right. \\
 & \quad \quad \left. \left. 2 b(c+d x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]\right)\right) \Bigg) / \left(d^2(-b c + a d)(c+d x)\right) + \\
 & 2 \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right]\right) \left(-\frac{\text{Log}\left[\frac{c}{d} + x\right]^2}{2 d^2} - \frac{c \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right)}{d^2(c+d x)} - \right. \\
 & \quad \left. \frac{c \left(-\frac{\text{Log}\left[\frac{a}{b} + x\right]}{d(c+d x)} - \frac{b \text{Log}[a+b x]}{d(-b c + a d)} + \frac{b \text{Log}[c+d x]}{d(-b c + a d)}\right)}{d} + \frac{\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right]}{d^2}\right) \Bigg) + \\
 & \frac{1}{d^2} \left(\text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c - a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c + a d}\right] - \right. \\
 & \quad \left. 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c + a d}\right]\right) - 2 \left(-\left(\left(c \left(2(b c - a d) \text{Log}\left[\frac{a}{b} + x\right] \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right) + b(c+d x) \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left(\text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c + a d}\right] + 2 \text{Log}[c+d x]\right) - 2 \right. \right. \\
 & \quad \quad \left. \left. b(c+d x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c - a d}\right]\right)\right) \Bigg) / \left(2 d^2(-b c + a d)(c+d x)\right) + \frac{1}{2 d^2}
 \end{aligned}$$

$$\left( \text{Log}\left[\frac{c}{d} + x\right]^2 \left( \text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \right) - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] + \right. \\ \left. 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] \right)$$

**Problem 196: Result more than twice size of optimal antiderivative.**

$$\int \frac{(ag + bgx) \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2}{(ci + dix)^2} dx$$

Optimal (type 4, 282 leaves, 9 steps):

$$\frac{2ABgn(a+bx)}{d^2(c+dx)} - \frac{2B^2gn^2(a+bx)}{d^2(c+dx)} + \frac{2B^2gn(a+bx) \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right]}{d^2(c+dx)} - \\ \frac{g(a+bx) \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2}{d^2(c+dx)} - \frac{bg \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2 \text{Log}\left[ \frac{bc-ad}{b(c+dx)} \right]}{d^2i^2} - \\ \frac{2bBgn \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right) \text{PolyLog}\left[ 2, \frac{d(a+bx)}{b(c+dx)} \right]}{d^2i^2} + \frac{2bB^2gn^2 \text{PolyLog}\left[ 3, \frac{d(a+bx)}{b(c+dx)} \right]}{d^2i^2}$$

Result (type 4, 1305 leaves):

$$\frac{1}{i^2} g \left( \frac{(bc-ad) \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] - Bn \text{Log}\left[ \frac{a+bx}{c+dx} \right] \right)^2}{d^2(c+dx)} + \right. \\ \frac{aB^2n^2(a+bx) \left( 2 - 2 \text{Log}\left[ \frac{a+bx}{c+dx} \right] + \text{Log}\left[ \frac{a+bx}{c+dx} \right]^2 \right)}{(bc-ad)(c+dx)} + \\ \frac{b \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] - Bn \text{Log}\left[ \frac{a+bx}{c+dx} \right] \right)^2 \text{Log}[c+dx]}{d^2} + \\ \left( 2aBn \left( -A - B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] + Bn \text{Log}\left[ \frac{a+bx}{c+dx} \right] \right) \left( bc-ad + b(c+dx) \text{Log}\left[ \frac{a}{b} + x \right] + \right. \right. \\ \left. \left. (-bc+ad) \text{Log}\left[ \frac{a+bx}{c+dx} \right] - bc \text{Log}\left[ \frac{b(c+dx)}{bc-ad} \right] - bdx \text{Log}\left[ \frac{b(c+dx)}{bc-ad} \right] \right) \right) / \\ (d(-bc+ad)(c+dx)) + \frac{1}{d^2} bBn \left( A + B \text{Log}\left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] - Bn \text{Log}\left[ \frac{a+bx}{c+dx} \right] \right) \\ \left( -\text{Log}\left[ \frac{c}{d} + x \right]^2 + 2 \text{Log}\left[ \frac{c}{d} + x \right] \text{Log}[c+dx] + \right. \\ \left. 2 \left( -\frac{c}{c+dx} + \frac{bc \text{Log}[a+bx]}{-bc+ad} + \frac{bc \text{Log}[c+dx]}{bc-ad} - \text{Log}\left[ \frac{a}{b} + x \right] \text{Log}[c+dx] + \right. \right.$$

$$\begin{aligned}
 & \text{Log}\left[\frac{a+b x}{c+d x}\right] \left(\frac{c}{c+d x} + \text{Log}[c+d x]\right) + \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \\
 & 2 \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + \frac{1}{3 d^2 (b c-a d) (c+d x)} \\
 & b B^2 n^2 \left( (b c-a d) (c+d x) \text{Log}\left[\frac{c}{d} + x\right]^3 + 3 c (b c-a d) \left(2 + 2 \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{c}{d} + x\right]^2\right) + \right. \\
 & 3 (b c-a d) \left(-\text{Log}\left[\frac{a}{b} + x\right] + \text{Log}\left[\frac{c}{d} + x\right] + \text{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 (c+(c+d x) \text{Log}[c+d x]) + \\
 & 3 c \text{Log}\left[\frac{a}{b} + x\right] \left(-d(a+b x) \text{Log}\left[\frac{a}{b} + x\right] + 2 b(c+d x) \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right) + \\
 & 6 b c(c+d x) \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] + 3 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{c}{d} + x\right] - \text{Log}\left[\frac{a+b x}{c+d x}\right]\right) \\
 & \left( (b c-a d) (c+d x) \text{Log}\left[\frac{c}{d} + x\right]^2 + 2 c (b c-a d) \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right) + \right. \\
 & 2 c \left( (-b c+a d) \text{Log}\left[\frac{a}{b} + x\right] + b(c+d x) \left(\text{Log}[a+b x] - \text{Log}[c+d x]\right) \right) - 2 (b c-a d) \\
 & (c+d x) \left(\text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right) \left. \right) + 3 (b c-a d) \\
 & (c+d x) \left(\text{Log}\left[\frac{a}{b} + x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \right. \\
 & 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \left. \right) - 3 \left(c \left(2 (b c-a d) \text{Log}\left[\frac{a}{b} + x\right] \left(1 + \text{Log}\left[\frac{c}{d} + x\right]\right) + \right. \right. \\
 & b(c+d x) \left(\text{Log}\left[\frac{c}{d} + x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d} + x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \right. \\
 & \left. \left. 2 \text{Log}[c+d x]\right) - 2 b(c+d x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) + \\
 & (b c-a d) (c+d x) \left(\text{Log}\left[\frac{c}{d} + x\right]^2 \left(\text{Log}\left[\frac{a}{b} + x\right] - \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right) - \right. \\
 & \left. \left. 2 \text{Log}\left[\frac{c}{d} + x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \left. \right) \left. \right) \left. \right) \left. \right)
 \end{aligned}$$

**Problem 197: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(c i + d i x)^2} dx$$

Optimal (type 3, 163 leaves, 4 steps):

$$-\frac{2 A B n (a+b x)}{(b c-a d) i^2 (c+d x)}+\frac{2 B^2 n^2 (a+b x)}{(b c-a d) i^2 (c+d x)}-\frac{2 B^2 n (a+b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c-a d) i^2 (c+d x)}+\frac{(a+b x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d) i^2 (c+d x)}$$

Result (type 3, 391 leaves):

$$\frac{1}{d(-b c+a d) i^2 (c+d x)}\left(A^2 b c-a A^2 d-2 A b B c n+2 a A B d n+2 b B^2 c n^2-2 a B^2 d n^2+B^2(b c-a d) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-b B^2 c n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2-b B^2 d n^2 x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+2 b B n(c+d x) \operatorname{Log}[a+b x]\left(-A+B n-B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]+B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+2 A b B c n \operatorname{Log}[c+d x]-2 b B^2 c n^2 \operatorname{Log}[c+d x]+2 A b B d n x \operatorname{Log}[c+d x]-2 b B^2 d n^2 x \operatorname{Log}[c+d x]-2 b B^2 c n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x]-2 b B^2 d n^2 x \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \operatorname{Log}[c+d x]+2 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left((b c-a d)(A-B n)+b B n(c+d x) \operatorname{Log}[c+d x]\right)\right)$$

### Problem 198: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(a g+b g x)(c i+d i x)^2} d x$$

Optimal (type 3, 231 leaves, 7 steps):

$$\frac{2 A B d n(a+b x)}{(b c-a d)^2 g i^2 (c+d x)}-\frac{2 B^2 d n^2(a+b x)}{(b c-a d)^2 g i^2 (c+d x)}+\frac{2 B^2 d n(a+b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c-a d)^2 g i^2 (c+d x)}-\frac{d(a+b x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^2 g i^2 (c+d x)}+\frac{b\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{3 B(b c-a d)^2 g i^2 n}$$

Result (type 3, 789 leaves):



$$\begin{aligned}
 & \frac{b B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^3}{3(b c-a d)^2 g i^2} - \frac{2 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \left(-A+B n-B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)}{(b c-a d) g i^2(c+d x)} + \\
 & \left(\operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2\left(A b B c n-a B^2 d n^2+A b B d n x-b B^2 d n^2 x+b B^2 c n\right.\right. \\
 & \quad \left.\left.\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+b B^2 d n x\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)\right) / \\
 & \left((b c-a d)^2 g i^2(c+d x)\right)+\left(A^2-2 A B n+2 B^2 n^2+2 A B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)-\right. \\
 & \quad \left.2 B^2 n\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+B^2\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) / \\
 & \left((b c-a d) g i^2(c+d x)\right)+\frac{1}{(b c-a d)^2 g i^2} b \operatorname{Log}[a+b x] \\
 & \left(A^2-2 A B n+2 B^2 n^2+2 A B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)-\right. \\
 & \quad \left.2 B^2 n\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+B^2\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right)- \\
 & \frac{1}{(b c-a d)^2 g i^2} b\left(A^2-2 A B n+2 B^2 n^2+2 A B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)-2 B^2 n\right. \\
 & \quad \left.\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+B^2\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) \operatorname{Log}[c+d x]
 \end{aligned}$$

### Problem 199: Result more than twice size of optimal antiderivative.

$$\int \frac{\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(a g+b g x)^2(c i+d i x)^2} d x$$

Optimal (type 3, 392 leaves, 10 steps):

$$\begin{aligned}
 & -\frac{2 A B d^2 n(a+b x)}{(b c-a d)^3 g^2 i^2(c+d x)} + \frac{2 B^2 d^2 n^2(a+b x)}{(b c-a d)^3 g^2 i^2(c+d x)} - \\
 & \frac{2 b^2 B^2 n^2(c+d x)}{(b c-a d)^3 g^2 i^2(a+b x)} - \frac{2 B^2 d^2 n(a+b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c-a d)^3 g^2 i^2(c+d x)} - \\
 & \frac{2 b^2 B n(c+d x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c-a d)^3 g^2 i^2(a+b x)} + \frac{d^2(a+b x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^3 g^2 i^2(c+d x)} - \\
 & \frac{b^2(c+d x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^3 g^2 i^2(a+b x)} - \frac{2 b d\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{3 B(b c-a d)^3 g^2 i^2 n}
 \end{aligned}$$

Result (type 3, 870 leaves):

$$\begin{aligned}
 & \frac{1}{3 (b c - a d)^3 g^2 i^2 (a + b x) (c + d x)} \\
 & \left( 2 b B^2 d n^2 (a + b x) (c + d x) \text{Log}\left[\frac{a + b x}{c + d x}\right]^3 + 3 B n \text{Log}\left[\frac{a + b x}{c + d x}\right]^2 \left( 2 a A b c d + b^2 B c^2 n - \right. \right. \\
 & \quad \left. \left. a^2 B d^2 n + 2 A b^2 c d x + 2 a A b d^2 x + 2 b^2 B c d n x - 2 a b B d^2 n x + 2 A b^2 d^2 x^2 + \right. \right. \\
 & \quad \left. \left. 2 b B d (a + b x) (c + d x) \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 b B d n (a + b x) (c + d x) \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \left. 6 B (b c - a d) n \text{Log}\left[\frac{a + b x}{c + d x}\right] \left( A b c + a A d + b B c n - a B d n + 2 A b d x + \right. \right. \\
 & \quad \left. \left. B (a d + b (c + 2 d x)) \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n (b c + a d + 2 b d x) \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \left. 6 b d (a + b x) (c + d x) \text{Log}[a + b x] \left( A^2 + 2 B^2 n^2 + 2 A B \left( \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \right. \\
 & \quad \left. \left. B^2 \left( \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 \right) + \right. \\
 & \quad \left. 3 b (b c - a d) (c + d x) \left( A^2 + 2 A B n + 2 B^2 n^2 + B^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (A + B n) \text{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \right. \\
 & \quad \left. \left. B^2 n^2 \text{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( A + B n - B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 3 d (b c - a d) \right. \\
 & \quad \left. (a + b x) \left( A^2 - 2 A B n + 2 B^2 n^2 + B^2 \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-A + B n) \text{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \right. \\
 & \quad \left. \left. B^2 n^2 \text{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -A + B n + B n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - \right. \\
 & \quad \left. 6 b d (a + b x) (c + d x) \left( A^2 + 2 B^2 n^2 + 2 A B \left( \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \right. \\
 & \quad \left. \left. B^2 \left( \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \text{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 \right) \text{Log}[c + d x] \right)
 \end{aligned}$$

**Problem 200: Result more than twice size of optimal antiderivative.**

$$\int \frac{\left( A + B \text{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \right)^2}{(a g + b g x)^3 (c i + d i x)^2} dx$$

Optimal (type 3, 560 leaves, 12 steps):

$$\begin{aligned}
 & \frac{2 A B d^3 n (a+b x)}{(b c-a d)^4 g^3 i^2 (c+d x)} - \frac{2 B^2 d^3 n^2 (a+b x)}{(b c-a d)^4 g^3 i^2 (c+d x)} + \frac{6 b^2 B^2 d n^2 (c+d x)}{(b c-a d)^4 g^3 i^2 (a+b x)} - \\
 & \frac{b^3 B^2 n^2 (c+d x)^2}{4 (b c-a d)^4 g^3 i^2 (a+b x)^2} + \frac{2 B^2 d^3 n (a+b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c-a d)^4 g^3 i^2 (c+d x)} + \\
 & \frac{6 b^2 B d n (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c-a d)^4 g^3 i^2 (a+b x)} - \frac{b^3 B n (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 (b c-a d)^4 g^3 i^2 (a+b x)^2} - \\
 & \frac{d^3 (a+b x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^4 g^3 i^2 (c+d x)} + \frac{3 b^2 d (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^4 g^3 i^2 (a+b x)} - \\
 & \frac{b^3 (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 (b c-a d)^4 g^3 i^2 (a+b x)^2} + \frac{b d^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{B (b c-a d)^4 g^3 i^2 n}
 \end{aligned}$$

Result (type 3, 1340 leaves):

$$\begin{aligned}
 & \frac{1}{4 (b c - a d)^4 g^3 i^2 (a + b x)^2 (c + d x)} \\
 & \left( 4 b B^2 d^2 n^2 (a + b x)^2 (c + d x) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^3 + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 \right. \\
 & \quad \left( 6 a^2 A b c d^2 - b^3 B c^3 n + 6 a b^2 B c^2 d n - 2 a^3 B d^3 n + 12 a A b^2 c d^2 x + 6 a^2 A b d^3 x + \right. \\
 & \quad \quad 3 b^3 B c^2 d n x + 12 a b^2 B c d^2 n x - 6 a^2 b B d^3 n x + 6 A b^3 c d^2 x^2 + 12 a A b^2 d^3 x^2 + \\
 & \quad \quad 9 b^3 B c d^2 n x^2 + 6 A b^3 d^3 x^3 + 3 b^3 B d^3 n x^3 + 6 b B d^2 (a + b x)^2 (c + d x) \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
 & \quad \quad \left. 6 b B d^2 n (a + b x)^2 (c + d x) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + 2 b d (b c - a d) (a + b x) (c + d x) \\
 & \quad \left( 4 A^2 + 10 A B n + 11 B^2 n^2 + 4 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (4 A + 5 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \quad \left. 4 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 4 A + 5 B n - 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - b (b c - a d)^2 \\
 & \quad (c + d x) \left( 2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
 & \quad 6 b d^2 (a + b x)^2 (c + d x) \operatorname{Log}[a + b x] \left( 2 A^2 + 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - \right. \\
 & \quad \quad \left. 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \\
 & \quad \quad \left. 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 2 B (b c - a d) n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \\
 & \quad \left( 2 b d (a + b x) (c + d x) \left( 4 A + 5 B n + 4 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) - \right. \\
 & \quad \quad \left. b (b c - a d) (c + d x) \left( 2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \quad \left. 4 d^2 (a + b x)^2 \left( A - B n + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 4 d^2 (b c - a d) \\
 & \quad (a + b x)^2 \left( A^2 - 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \quad \left. B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -A + B n + B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - 6 b d^2 (a + b x)^2 \\
 & \quad (c + d x) \left( 2 A^2 + 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \operatorname{Log}[c + d x] \Big)
 \end{aligned}$$

**Problem 201: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right])^2}{(a g + b g x)^4 (c i + d i x)^2} dx$$

Optimal (type 3, 729 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{2 A B d^4 n (a+b x)}{(b c-a d)^5 g^4 i^2 (c+d x)} + \frac{2 B^2 d^4 n^2 (a+b x)}{(b c-a d)^5 g^4 i^2 (c+d x)} - \frac{12 b^2 B^2 d^2 n^2 (c+d x)}{(b c-a d)^5 g^4 i^2 (a+b x)} + \\
 & \frac{b^3 B^2 d n^2 (c+d x)^2}{(b c-a d)^5 g^4 i^2 (a+b x)^2} - \frac{2 b^4 B^2 n^2 (c+d x)^3}{27 (b c-a d)^5 g^4 i^2 (a+b x)^3} - \frac{2 B^2 d^4 n (a+b x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c-a d)^5 g^4 i^2 (c+d x)} - \\
 & \frac{12 b^2 B d^2 n (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c-a d)^5 g^4 i^2 (a+b x)} + \frac{2 b^3 B d n (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c-a d)^5 g^4 i^2 (a+b x)^2} - \\
 & \frac{2 b^4 B n (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{9 (b c-a d)^5 g^4 i^2 (a+b x)^3} + \frac{d^4 (a+b x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^5 g^4 i^2 (c+d x)} - \\
 & \frac{6 b^2 d^2 (c+d x) \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^5 g^4 i^2 (a+b x)} + \frac{2 b^3 d (c+d x)^2 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c-a d)^5 g^4 i^2 (a+b x)^2} - \\
 & \frac{b^4 (c+d x)^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{3 (b c-a d)^5 g^4 i^2 (a+b x)^3} - \frac{4 b d^3 \left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{3 B (b c-a d)^5 g^4 i^2 n}
 \end{aligned}$$

Result (type 3, 1695 leaves):

$$\begin{aligned}
 & - \frac{1}{27 (b c-a d)^5 g^4 i^2 (a+b x)^3 (c+d x)} \\
 & \left(36 b B^2 d^3 n^2 (a+b x)^3 (c+d x) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^3 + 9 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 \right. \\
 & \left. \left(12 a^3 A b c d^3 + b^4 B c^4 n - 6 a b^3 B c^3 d n + 18 a^2 b^2 B c^2 d^2 n - 3 a^4 B d^4 n + 36 a^2 A b^2 c d^3 x + \right. \right. \\
 & \left. \left. 12 a^3 A b d^4 x - 2 b^4 B c^3 d n x + 18 a b^3 B c^2 d^2 n x + 36 a^2 b^2 B c d^3 n x - 12 a^3 b B d^4 n x + \right. \right. \\
 & \left. \left. 36 a A b^3 c d^3 x^2 + 36 a^2 A b^2 d^4 x^2 + 6 b^4 B c^2 d^2 n x^2 + 54 a b^3 B c d^3 n x^2 + 12 A b^4 c d^3 x^3 + \right. \right. \\
 & \left. \left. 36 a A b^3 d^4 x^3 + 22 b^4 B c d^3 n x^3 + 18 a b^3 B d^4 n x^3 + 12 A b^4 d^4 x^4 + 10 b^4 B d^4 n x^4 + \right. \right. \\
 & \left. \left. 12 b B d^3 (a+b x)^3 (c+d x) \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 12 b B d^3 n (a+b x)^3 (c+d x) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right. \\
 & \left. 3 b d^2 (b c-a d) (a+b x)^2 (c+d x) \left(27 A^2 + 78 A B n + 92 B^2 n^2 + 27 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 - \right. \\
 & \left. 6 B n (9 A + 13 B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 27 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \right. \\
 & \left. \left(9 A + 13 B n - 9 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + 6 b d^3 (a+b x)^3 (c+d x) \operatorname{Log}[a+b x] \right. \\
 & \left. \left(18 A^2 + 30 A B n + 55 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 - 6 B n (6 A + 5 B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\
 & \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \left(6 A + 5 B n - 6 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right. \\
 & \left. b (b c-a d)^3 (c+d x) \left(9 A^2 + 6 A B n + 2 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 - 6 B n (3 A + B n) \right. \\
 & \left. \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 9 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \left(3 A + B n - 3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right. \\
 & \left. 3 b d (b c-a d)^2 (a+b x) (c+d x) \left(9 A^2 + 12 A B n + 7 B^2 n^2 + 9 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 B n (3 A + 2 B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 9 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + \\
 & 6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \left(3 A + 2 B n - 3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + 6 B (b c - a d) n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \\
 & \left(3 b d^2 (a+b x)^2 (c+d x) \left(9 A + 13 B n + 9 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 9 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right. \\
 & \left. b (b c - a d)^2 (c+d x) \left(3 A + B n + 3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) - \right. \\
 & \left. 3 b d (b c - a d) (a+b x) (c+d x) \left(3 A + 2 B n + 3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - 3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right. \\
 & \left. 9 d^3 (a+b x)^3 \left(A - B n + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right) + 27 d^3 (b c - a d) \\
 & (a+b x)^3 \left(A^2 - 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2 B n (-A + B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\
 & \left. B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \left(-A + B n + B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right) - 6 b d^3 (a+b x)^3 \\
 & (c+d x) \left(18 A^2 + 30 A B n + 55 B^2 n^2 + 18 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 - 6 B n (6 A + 5 B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\
 & \left. 18 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2 + 6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] \left(6 A + 5 B n - 6 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right) \operatorname{Log}[c+d x]
 \end{aligned}$$

**Problem 202: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^3 \left(A + B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(c i + d i x)^3} dx$$

Optimal (type 4, 676 leaves, 14 steps):

$$\begin{aligned}
 & \frac{B^2 (b c - a d) g^3 n^2 (a + b x)^2}{4 d^2 i^3 (c + d x)^2} - \frac{4 A b B (b c - a d) g^3 n (a + b x)}{d^3 i^3 (c + d x)} + \\
 & \frac{4 b B^2 (b c - a d) g^3 n^2 (a + b x)}{d^3 i^3 (c + d x)} - \frac{4 b B^2 (b c - a d) g^3 n (a + b x) \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{d^3 i^3 (c + d x)} - \\
 & \frac{B (b c - a d) g^3 n (a + b x)^2 \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 d^2 i^3 (c + d x)^2} + \frac{b^2 g^3 (a + b x) \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{d^3 i^3} + \\
 & \frac{(b c - a d) g^3 (a + b x)^2 \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 d^2 i^3 (c + d x)^2} + \frac{2 b (b c - a d) g^3 (a + b x) \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{d^3 i^3 (c + d x)} + \\
 & \frac{2 b^2 B (b c - a d) g^3 n \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \text{Log}\left[\frac{-b c - a d}{b (c + d x)}\right]}{d^4 i^3} + \\
 & \frac{3 b^2 (b c - a d) g^3 \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2 \text{Log}\left[\frac{b c - a d}{b (c + d x)}\right]}{d^4 i^3} + \\
 & \frac{2 b^2 B^2 (b c - a d) g^3 n^2 \text{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{d^4 i^3} + \\
 & \frac{6 b^2 B (b c - a d) g^3 n \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right) \text{PolyLog}\left[2, \frac{d (a+b x)}{b (c+d x)}\right]}{d^4 i^3} - \\
 & \frac{6 b^2 B^2 (b c - a d) g^3 n^2 \text{PolyLog}\left[3, \frac{d (a+b x)}{b (c+d x)}\right]}{d^4 i^3}
 \end{aligned}$$

Result (type 4, 6600 leaves):

$$\begin{aligned}
 & \frac{b^3 g^3 x \left(A + B \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)^2}{d^3 i^3} - \frac{1}{d^4 i^3 (c + d x)} \\
 & 3 \left(A^2 b^3 c^2 g^3 - 2 a A^2 b^2 c d g^3 + a^2 A^2 b d^2 g^3 + 2 A b^3 B c^2 g^3 \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right) - \right. \\
 & \quad 4 a A b^2 B c d g^3 \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \\
 & \quad 2 a^2 A b B d^2 g^3 \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \\
 & \quad b^3 B^2 c^2 g^3 \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 - 2 a b^2 B^2 c d g^3 \\
 & \quad \left.\left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2 + a^2 b B^2 d^2 g^3 \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right)^2\right) + \\
 & \frac{1}{2 d^4 i^3 (c + d x)^2} \left(A^2 b^3 c^3 g^3 - 3 a A^2 b^2 c^2 d g^3 + 3 a^2 A^2 b c d^2 g^3 - a^3 A^2 d^3 g^3 + \right. \\
 & \quad 2 A b^3 B c^3 g^3 \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right) - \\
 & \quad \left. 6 a A b^2 B c^2 d g^3 \left(\text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] - n \text{Log}\left[\frac{a+b x}{c+d x}\right]\right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 a^2 A b B c d^2 g^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) - \\
 & 2 a^3 A B d^3 g^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) + \\
 & b^3 B^2 c^3 g^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - \\
 & 3 a b^2 B^2 c^2 d g^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 + \\
 & 3 a^2 b B^2 c d^2 g^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - \\
 & a^3 B^2 d^3 g^3 \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right)^2 - \frac{1}{d^4 i^3} \\
 & 3 b^2 (b c - a d) g^3 \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 \text{Log} [c+d x] + \\
 & \left( a^3 B^2 g^3 n^2 \left( -7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c+d x)^2 \text{Log} [a+b x] + \right. \right. \\
 & \quad \left. \left. 2 (b c - a d) (3 b c - a d + 2 b d x) \text{Log} \left[ \frac{a+b x}{c+d x} \right] - 2 d (a+b x) (-2 b c + a d - b d x) \right. \right. \\
 & \quad \left. \left. \text{Log} \left[ \frac{a+b x}{c+d x} \right]^2 + 6 b^2 c^2 \text{Log} [c+d x] + 12 b^2 c d x \text{Log} [c+d x] + 6 b^2 d^2 x^2 \text{Log} [c+d x] \right) \right) / \\
 & \left( 4 d (b c - a d)^2 i^3 (c+d x)^2 + \frac{1}{i^3} 2 a^3 B g^3 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \right) \\
 & \left( \frac{\left( \frac{c}{d} + x \right) \left( 2 \text{Log} \left[ \frac{c}{d} + x \right] + 4 \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{8 (c+d x)^3 \text{Log} \left[ \frac{c}{d} + x \right]} + \frac{1}{2 d} \right. \\
 & \left. \left( \frac{d \left( \frac{a}{b} + x \right)}{\left( -c + \frac{a d}{b} \right)^3 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)} - \left( \frac{d^2 \left( \frac{a}{b} + x \right)^2}{\left( -c + \frac{a d}{b} \right)^4 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)^2} + \frac{2 d \left( \frac{a}{b} + x \right)}{\left( -c + \frac{a d}{b} \right)^3 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)} \right) \text{Log} \left[ \frac{a}{b} + x \right] - \right. \\
 & \left. \frac{\text{Log} \left[ 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right]}{\left( -c + \frac{a d}{b} \right)^2} \right) - \frac{-\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{-a}{c+d x} + \frac{b x}{c+d x} \right]}{2 d (c+d x)^2} \right) + \\
 & \frac{1}{i^3} 6 a^2 b B g^3 n \left( A + B \left( \text{Log} \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \text{Log} \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( \frac{1 + \text{Log} \left[ \frac{c}{d} + x \right]}{d^2 (c+d x)} - \frac{c \left( 1 + 2 \text{Log} \left[ \frac{c}{d} + x \right] \right)}{4 d^2 (c+d x)^2} + \frac{-\frac{\text{Log} \left[ \frac{a+x}{b} \right]}{d (c+d x)} - \frac{b \text{Log} [a+b x]}{d (-b c+a d)} + \frac{b \text{Log} [c+d x]}{d (-b c+a d)}}{d} - \right. \\
 & \left. \frac{c \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \frac{b (c+d x) (b c - a d + b (c+d x) \text{Log} [a+b x] - b (c+d x) \text{Log} [c+d x])}{(b c - a d)^2} \right)}{2 d^2 (c+d x)^2} \right) -
 \end{aligned}$$



$$\begin{aligned}
 & \left. \frac{(c+2dx) \left( -\log\left[\frac{a}{b}+x\right] + \log\left[\frac{c}{d}+x\right] + \log\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)}{2d^2(c+dx)^2} \right) + \\
 & \frac{1}{i^3} 2b^3 B g^3 n \left( A+B \left( \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \log\left[\frac{a+bx}{c+dx}\right] \right) \right) \\
 & \left( \frac{\left(\frac{a}{b}+x\right) \left(-1 + \log\left[\frac{a}{b}+x\right]\right)}{d^3} - \frac{\left(\frac{c}{d}+x\right) \left(-1 + \log\left[\frac{c}{d}+x\right]\right)}{d^3} + \frac{3c \log\left[\frac{c}{d}+x\right]^2}{2d^4} + \right. \\
 & \frac{3c^2 \left(1 + \log\left[\frac{c}{d}+x\right]\right)}{d^4(c+dx)} - \frac{c^3 \left(1 + 2 \log\left[\frac{c}{d}+x\right]\right)}{4d^4(c+dx)^2} + \frac{3c^2 \left(-\frac{\log\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \log[a+bx]}{d(-bc+ad)} + \frac{b \log[c+dx]}{d(-bc+ad)}\right)}{d^3} - \\
 & \frac{c^3 \left(-\log\left[\frac{a}{b}+x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\log[a+bx]-b(c+dx)\log[c+dx])}{(bc-ad)^2}\right)}{2d^4(c+dx)^2} - \frac{1}{2d^4} \\
 & \left. \left(-2dx + \frac{c^2(5c+6dx)}{(c+dx)^2} + 6c \log[c+dx]\right) \left(-\log\left[\frac{a}{b}+x\right] + \log\left[\frac{c}{d}+x\right] + \right. \right. \\
 & \left. \left. \log\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) - \frac{3c \left(\log\left[\frac{a}{b}+x\right] \log\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]\right)}{d^4} \right) + \\
 & \frac{1}{i^3} 6ab^2 B g^3 n \left( A+B \left( \log\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] - n \log\left[\frac{a+bx}{c+dx}\right] \right) \right) \left( -\frac{\log\left[\frac{c}{d}+x\right]^2}{2d^3} - \right. \\
 & \frac{2c \left(1 + \log\left[\frac{c}{d}+x\right]\right)}{d^3(c+dx)} + \frac{c^2 \left(1 + 2 \log\left[\frac{c}{d}+x\right]\right)}{4d^3(c+dx)^2} - \frac{2c \left(-\frac{\log\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \log[a+bx]}{d(-bc+ad)} + \frac{b \log[c+dx]}{d(-bc+ad)}\right)}{d^2} + \\
 & \frac{c^2 \left(-\log\left[\frac{a}{b}+x\right] + \frac{b(c+dx)(bc-ad+b(c+dx)\log[a+bx]-b(c+dx)\log[c+dx])}{(bc-ad)^2}\right)}{2d^3(c+dx)^2} + \frac{1}{2d^3} \\
 & \left. \left(\frac{c(3c+4dx)}{(c+dx)^2} + 2 \log[c+dx]\right) \left(-\log\left[\frac{a}{b}+x\right] + \log\left[\frac{c}{d}+x\right] + \log\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) + \right. \\
 & \left. \frac{\log\left[\frac{a}{b}+x\right] \log\left[\frac{b(c+dx)}{bc-ad}\right] + \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} \right) +
 \end{aligned}$$

$$\frac{1}{i^3} 3 a^2 b B^2 g^3 n^2 \left( -\frac{2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{d^2 (c + d x)} + \frac{c \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2\right)}{4 d^2 (c + d x)^2} + \right.$$

$$2 \left( \frac{1 + \operatorname{Log}\left[\frac{c}{d} + x\right]}{d^2 (c + d x)} - \frac{c \left(1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{4 d^2 (c + d x)^2} + \frac{-\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c + d x)} - \frac{b \operatorname{Log}[a + b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c + d x]}{d (-b c + a d)}}{d} - \frac{1}{2 d^2 (c + d x)^2} \right.$$

$$c \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(b c - a d)^2} b (c + d x) (b c - a d + b (c + d x) \operatorname{Log}[a + b x]) - \right.$$

$$\left. \left. b (c + d x) \operatorname{Log}[c + d x] \right) \right) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right) -$$

$$\frac{(c + 2 d x) \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c + d x} + \frac{b x}{c + d x}\right] \right)^2}{2 d^2 (c + d x)^2} + \left( -d (a + b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + \right.$$

$$2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \Big) /$$

$$(d^2 (-b c + a d) (c + d x)) + \left( c \left( d (a + b x) (a d - b (2 c + d x)) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - \right.$$

$$2 b^2 (c + d x)^2 \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] + 2 b (c + d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \right.$$

$$\left. \left. \left( d (a + b x) + b (c + d x) \operatorname{Log}\left[\frac{b (c + d x)}{b c - a d}\right] \right) + 2 b^2 (c + d x)^2 \operatorname{PolyLog}\left[2, \frac{d (a + b x)}{-b c + a d}\right] \right) \Big) /$$

$$(2 d^2 (b c - a d)^2 (c + d x)^2) - 2 \left( \left( 2 (b c - a d) \operatorname{Log}\left[\frac{a}{b} + x\right] \left( 1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) + b (c + d x) \right.$$

$$\left. \left( \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - 2 \operatorname{Log}[a + b x] - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}[c + d x] \right) - \right.$$

$$2 b (c + d x) \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \Big) / (2 d^2 (-b c + a d) (c + d x)) +$$

$$\left( c \left( -b (b c - a d) (c + d x) + (b c - a d)^2 \operatorname{Log}\left[\frac{a}{b} + x\right] \left( 1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - b^2 (c + d x)^2 \right.$$

$$\operatorname{Log}[a + b x] + b^2 (c + d x)^2 \operatorname{Log}[c + d x] + b (c + d x) \left( b (c + d x) \operatorname{Log}\left[\frac{c}{d} + x\right]^2 - \right.$$

$$2 (b c - a d) \left( 1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right) - 2 b (c + d x) \left( \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + \right.$$

$$\left. \left. \left. \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] \right) \right) \right) \Big) / (4 d^2 (b c - a d)^2 (c + d x)^2) \Big) \Big) +$$

$$\begin{aligned}
 & \frac{1}{i^3} b^3 B^2 g^3 n^2 \left( \frac{(a+b x) \left( 2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \right)}{b d^3} - \frac{c \operatorname{Log}\left[\frac{c}{d} + x\right]^3}{d^4} + \right. \\
 & \frac{(c+d x) \left( 2 - 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^4} - \frac{3 c^2 \left( 2 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{d^4 (c+d x)} + \\
 & \frac{c^3 \left( 1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right]^2 \right)}{4 d^4 (c+d x)^2} - \frac{1}{2 d^4} \left( -2 d x + \frac{c^2 (5 c + 6 d x)}{(c+d x)^2} + 6 c \operatorname{Log}[c+d x] \right) \\
 & \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right)^2 + \\
 & \left( 3 c^2 \left( -d (a+b x) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 + 2 b (c+d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c+d x)}{b c - a d}\right] + \right. \right. \\
 & \left. \left. 2 b (c+d x) \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \right) \right) / \left( d^4 (-b c + a d) (c+d x) \right) + \\
 & \left( c^3 \left( d (a+b x) (a d - b (2 c + d x)) \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 b^2 (c+d x)^2 \operatorname{Log}\left[\frac{b (c+d x)}{b c - a d}\right] + \right. \right. \\
 & \left. \left. 2 b (c+d x) \operatorname{Log}\left[\frac{a}{b} + x\right] \left( d (a+b x) + b (c+d x) \operatorname{Log}\left[\frac{b (c+d x)}{b c - a d}\right] \right) + \right. \right. \\
 & \left. \left. 2 b^2 (c+d x)^2 \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \right) \right) / \\
 & \left( 2 d^4 (b c - a d)^2 (c+d x)^2 \right) + 2 \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \operatorname{Log}\left[\frac{c}{d} + x\right] + \operatorname{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) \\
 & \left( \frac{\left(\frac{a}{b} + x\right) \left(-1 + \operatorname{Log}\left[\frac{a}{b} + x\right]\right)}{d^3} - \frac{\left(\frac{c}{d} + x\right) \left(-1 + \operatorname{Log}\left[\frac{c}{d} + x\right]\right)}{d^3} + \frac{3 c \operatorname{Log}\left[\frac{c}{d} + x\right]^2}{2 d^4} + \right. \\
 & \frac{3 c^2 \left( 1 + \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{d^4 (c+d x)} - \frac{c^3 \left( 1 + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \right)}{4 d^4 (c+d x)^2} + \frac{3 c^2 \left( -\frac{\operatorname{Log}\left[\frac{a}{b} + x\right]}{d (c+d x)} - \frac{b \operatorname{Log}[a+b x]}{d (-b c + a d)} + \frac{b \operatorname{Log}[c+d x]}{d (-b c + a d)} \right)}{d^3} - \\
 & \frac{1}{2 d^4 (c+d x)^2} c^3 \left( -\operatorname{Log}\left[\frac{a}{b} + x\right] + \frac{1}{(b c - a d)^2} b (c+d x) (b c - a d + b (c+d x) \operatorname{Log}[a+b x] - \right. \\
 & \left. b (c+d x) \operatorname{Log}[c+d x] \right) - \frac{3 c \left( \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (c+d x)}{b c - a d}\right] + \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] \right)}{d^4} \left. \right) - \\
 & \frac{1}{d^4} 3 c \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 \operatorname{Log}\left[\frac{b (c+d x)}{b c - a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{PolyLog}\left[2, \frac{d (a+b x)}{-b c + a d}\right] - \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]-2\left(\frac{1}{b d^4}\left(a d+2 b d x-b d x \operatorname{Log}\left[\frac{c}{d}+x\right]-b c \operatorname{Log}[c+d x]+ \right.\right. \\
 & \left.\left.\operatorname{Log}\left[\frac{a}{b}+x\right]\left(-d(a+b x)+d(a+b x) \operatorname{Log}\left[\frac{c}{d}+x\right]+(b c-a d) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)\right)+ \\
 & (b c-a d) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+\left(3 c^2\left(2(b c-a d) \operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+ \right.\right. \\
 & \left.\left.b(c+d x)\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2-2 \operatorname{Log}[a+b x]-2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}[c+ \right.\right.\right. \\
 & \left.\left.\left.d x\right)\right)-2 b(c+d x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\left.\right) / \left(2 d^4(-b c+a d)(c+d x)\right)+ \\
 & \left(c^3\left(-b(b c-a d)(c+d x)+(b c-a d)^2 \operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right]\right)- \right.\right. \\
 & \left.\left.b^2(c+d x)^2 \operatorname{Log}[a+b x]+b^2(c+d x)^2 \operatorname{Log}[c+d x]+ \right.\right. \\
 & \left.\left.b(c+d x)\left(b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2(b c-a d)\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)- \right.\right.\right. \\
 & \left.\left.\left.2 b(c+d x)\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right)\right)\right) / \\
 & \left(4 d^4(b c-a d)^2(c+d x)^2\right)-\frac{1}{2 d^4} 3 c\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)- \right. \\
 & \left.\left.2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right)\right)\left.\right) + \\
 & \frac{1}{i^3} 3 a b^2 B^2 g^3 n^2\left(\frac{\operatorname{Log}\left[\frac{c}{d}+x\right]^3}{3 d^3}+\frac{2 c\left(2+2 \operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{d^3(c+d x)}-\right. \\
 & \left.\frac{c^2\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right]+2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{4 d^3(c+d x)^2}+\frac{1}{2 d^3}\right. \\
 & \left.\left(\frac{c(3 c+4 d x)}{(c+d x)^2}+2 \operatorname{Log}[c+d x]\right)\left(-\operatorname{Log}\left[\frac{a}{b}+x\right]+\operatorname{Log}\left[\frac{c}{d}+x\right]+\operatorname{Log}\left[\frac{a}{c+d x}+\frac{b x}{c+d x}\right]\right)^2- \right. \\
 & \left(2 c\left(-d(a+b x) \operatorname{Log}\left[\frac{a}{b}+x\right]^2+2 b(c+d x) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \right.\right. \\
 & \left.\left.2 b(c+d x) \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right)\right) / \left(d^3(-b c+a d)(c+d x)\right)- \\
 & \left(c^2\left(d(a+b x)(a d-b(2 c+d x)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2-2 b^2(c+d x)^2 \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]+ \right.\right. \\
 & \left.\left.2 b(c+d x) \operatorname{Log}\left[\frac{a}{b}+x\right]\left(d(a+b x)+b(c+d x) \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right]\right)\right)\right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left. 2 b^2 (c+d x)^2 \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]\right) / \\
 & \left( 2 d^3 (b c-a d)^2 (c+d x)^2 \right) + 2 \left( -\text{Log}\left[\frac{a}{b}+x\right] + \text{Log}\left[\frac{c}{d}+x\right] + \text{Log}\left[\frac{a}{c+d x} + \frac{b x}{c+d x}\right] \right) \\
 & \left( -\frac{\text{Log}\left[\frac{c}{d}+x\right]^2}{2 d^3} - \frac{2 c \left(1 + \text{Log}\left[\frac{c}{d}+x\right]\right)}{d^3 (c+d x)} + \frac{c^2 \left(1 + 2 \text{Log}\left[\frac{c}{d}+x\right]\right)}{4 d^3 (c+d x)^2} - \right. \\
 & \left. \frac{2 c \left( -\frac{\text{Log}\left[\frac{a}{b}+x\right]}{d(c+d x)} - \frac{b \text{Log}[a+b x]}{d(-b c+a d)} + \frac{b \text{Log}[c+d x]}{d(-b c+a d)} \right)}{d^2} + \frac{1}{2 d^3 (c+d x)^2} c^2 \left( -\text{Log}\left[\frac{a}{b}+x\right] + \frac{1}{(b c-a d)^2} \right. \right. \\
 & \left. \left. b(c+d x) (b c-a d + b(c+d x) \text{Log}[a+b x] - b(c+d x) \text{Log}[c+d x]) \right) \right) + \\
 & \left. \frac{\text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]}{d^3} \right) + \frac{1}{d^3} \left( \text{Log}\left[\frac{a}{b}+x\right]^2 \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right] + \right. \\
 & \left. 2 \text{Log}\left[\frac{a}{b}+x\right] \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - 2 \text{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] \right) - \\
 & 2 \left( -\left( \left( c \left( 2(b c-a d) \text{Log}\left[\frac{a}{b}+x\right] \left( 1 + \text{Log}\left[\frac{c}{d}+x\right] \right) + b(c+d x) \right. \right. \right. \right. \\
 & \left. \left. \left( \text{Log}\left[\frac{c}{d}+x\right]^2 - 2 \text{Log}[a+b x] - 2 \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + 2 \text{Log}[c+d x] \right) - 2 \right. \right. \right. \\
 & \left. \left. \left. b(c+d x) \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right) / \left( d^3 (-b c+a d) (c+d x) \right) \right) - \\
 & \left( c^2 \left( -b(b c-a d) (c+d x) + (b c-a d)^2 \text{Log}\left[\frac{a}{b}+x\right] \left( 1 + 2 \text{Log}\left[\frac{c}{d}+x\right] \right) - \right. \right. \\
 & \left. \left. b^2 (c+d x)^2 \text{Log}[a+b x] + b^2 (c+d x)^2 \text{Log}[c+d x] + \right. \right. \\
 & \left. \left. b(c+d x) \left( b(c+d x) \text{Log}\left[\frac{c}{d}+x\right]^2 - 2(b c-a d) \left( 1 + \text{Log}\left[\frac{c}{d}+x\right] \right) - \right. \right. \right. \\
 & \left. \left. \left. 2 b(c+d x) \left( \text{Log}\left[\frac{c}{d}+x\right] \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] + \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] \right) \right) \right) \right) / \\
 & \left( 4 d^3 (b c-a d)^2 (c+d x)^2 \right) + \frac{1}{2 d^3} \left( \text{Log}\left[\frac{c}{d}+x\right]^2 \left( \text{Log}\left[\frac{a}{b}+x\right] - \text{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \right) - \right. \\
 & \left. 2 \text{Log}\left[\frac{c}{d}+x\right] \text{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] + 2 \text{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] \right) \right)
 \end{aligned}$$

**Problem 203: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g + b g x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{(c i + d i x)^3} dx$$

Optimal (type 4, 441 leaves, 11 steps):

$$\begin{aligned} & -\frac{B^2 g^2 n^2 (a+b x)^2}{4 d i^3 (c+d x)^2} + \frac{2 A b B g^2 n (a+b x)}{d^2 i^3 (c+d x)} - \frac{2 b B^2 g^2 n^2 (a+b x)}{d^2 i^3 (c+d x)} + \frac{2 b B^2 g^2 n (a+b x) \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right]}{d^2 i^3 (c+d x)} + \\ & \frac{B g^2 n (a+b x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)}{2 d i^3 (c+d x)^2} - \frac{g^2 (a+b x)^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{2 d i^3 (c+d x)^2} - \\ & \frac{b g^2 (a+b x) \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2}{d^2 i^3 (c+d x)} - \frac{b^2 g^2 \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right)^2 \operatorname{Log}\left[ \frac{b c - a d}{b (c+d x)} \right]}{d^3 i^3} - \\ & \frac{2 b^2 B g^2 n \left( A + B \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] \right) \operatorname{PolyLog}\left[ 2, \frac{d (a+b x)}{b (c+d x)} \right]}{d^3 i^3} + \frac{2 b^2 B^2 g^2 n^2 \operatorname{PolyLog}\left[ 3, \frac{d (a+b x)}{b (c+d x)} \right]}{d^3 i^3} \end{aligned}$$

Result (type 4, 4247 leaves):

$$\begin{aligned} & -\frac{1}{d^3 i^3 (c+d x)} \\ & 2 \left( -A^2 b^2 c g^2 + a A^2 b d g^2 - 2 A b^2 B c g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) + 2 a A b B d g^2 \right. \\ & \quad \left. \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - b^2 B^2 c g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 + \right. \\ & \quad \left. a b B^2 d g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) + \frac{1}{2 d^3 i^3 (c+d x)^2} \\ & \left( -A^2 b^2 c^2 g^2 + 2 a A^2 b c d g^2 - a^2 A^2 d^2 g^2 - 2 A b^2 B c^2 g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) + \right. \\ & \quad 4 a A b B c d g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - \\ & \quad 2 a^2 A B d^2 g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) - \\ & \quad \left. b^2 B^2 c^2 g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 + 2 a b B^2 c d g^2 \right. \\ & \quad \left. \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 - a^2 B^2 d^2 g^2 \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right)^2 \right) + \\ & \frac{b^2 g^2 \left( A + B \left( \operatorname{Log}\left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] \right) \right)^2 \operatorname{Log}[c+d x]}{d^3 i^3} + \\ & \left( a^2 B^2 g^2 n^2 \left( -7 b^2 c^2 + 8 a b c d - a^2 d^2 - 6 b^2 c d x + 6 a b d^2 x - 6 b^2 (c+d x)^2 \operatorname{Log}[a+b x] + \right. \right. \\ & \quad \left. \left. 2 (b c - a d) (3 b c - a d + 2 b d x) \operatorname{Log}\left[ \frac{a+b x}{c+d x} \right] - 2 d (a+b x) (-2 b c + a d - b d x) \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \left( \log \left[ \frac{a+b x}{c+d x} \right]^2 + 6 b^2 c^2 \log [c+d x] + 12 b^2 c d x \log [c+d x] + 6 b^2 d^2 x^2 \log [c+d x] \right) \right) / \\
 & \left( 4 d (b c - a d)^2 i^3 (c+d x)^2 + \frac{1}{i^3} 2 a^2 B g^2 n \left( A+B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right) \right) \\
 & \left( \frac{\left( \frac{c}{d} + x \right) \left( 2 \log \left[ \frac{c}{d} + x \right] + 4 \log \left[ \frac{c}{d} + x \right]^2 \right)}{8 (c+d x)^3 \log \left[ \frac{c}{d} + x \right]} + \frac{1}{2 d} \right. \\
 & \left. \left( \frac{d \left( \frac{a}{b} + x \right)}{\left( -c + \frac{a d}{b} \right)^3 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)} - \left( \frac{d^2 \left( \frac{a}{b} + x \right)^2}{\left( -c + \frac{a d}{b} \right)^4 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)^2} + \frac{2 d \left( \frac{a}{b} + x \right)}{\left( -c + \frac{a d}{b} \right)^3 \left( 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right)} \right) \log \left[ \frac{a}{b} + x \right] - \right. \\
 & \left. \frac{\log \left[ 1 - \frac{d \left( \frac{a+x}{b} \right)}{-c + \frac{a d}{b}} \right]}{\left( -c + \frac{a d}{b} \right)^2} \right) - \frac{-\log \left[ \frac{a}{b} + x \right] + \log \left[ \frac{c}{d} + x \right] + \log \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right]}{2 d (c+d x)^2} \right) + \\
 & \frac{1}{i^3} 4 a b B g^2 n \left( A+B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( \frac{1 + \log \left[ \frac{c}{d} + x \right]}{d^2 (c+d x)} - \frac{c \left( 1 + 2 \log \left[ \frac{c}{d} + x \right] \right)}{4 d^2 (c+d x)^2} + \frac{-\frac{\log \left[ \frac{a+x}{b} \right]}{d (c+d x)} - \frac{b \log [a+b x]}{d (-b c+a d)} + \frac{b \log [c+d x]}{d (-b c+a d)}}{d} - \right. \\
 & \frac{c \left( -\log \left[ \frac{a}{b} + x \right] + \frac{b (c+d x) (b c-a d+b (c+d x) \log [a+b x] - b (c+d x) \log [c+d x])}{(b c-a d)^2} \right)}{2 d^2 (c+d x)^2} - \\
 & \left. \frac{(c+2 d x) \left( -\log \left[ \frac{a}{b} + x \right] + \log \left[ \frac{c}{d} + x \right] + \log \left[ \frac{a}{c+d x} + \frac{b x}{c+d x} \right] \right)}{2 d^2 (c+d x)^2} \right) + \\
 & \frac{1}{i^3} 2 b^2 B g^2 n \left( A+B \left( \log \left[ e \left( \frac{a+b x}{c+d x} \right)^n \right] - n \log \left[ \frac{a+b x}{c+d x} \right] \right) \right) \\
 & \left( -\frac{\log \left[ \frac{c}{d} + x \right]^2}{2 d^3} - \frac{2 c \left( 1 + \log \left[ \frac{c}{d} + x \right] \right)}{d^3 (c+d x)} + \right. \\
 & \frac{c^2 \left( 1 + 2 \log \left[ \frac{c}{d} + x \right] \right)}{4 d^3 (c+d x)^2} - \frac{2 c \left( -\frac{\log \left[ \frac{a+x}{b} \right]}{d (c+d x)} - \frac{b \log [a+b x]}{d (-b c+a d)} + \frac{b \log [c+d x]}{d (-b c+a d)} \right)}{d^2} + \\
 & \left. \frac{c^2 \left( -\log \left[ \frac{a}{b} + x \right] + \frac{b (c+d x) (b c-a d+b (c+d x) \log [a+b x] - b (c+d x) \log [c+d x])}{(b c-a d)^2} \right)}{2 d^3 (c+d x)^2} + \frac{1}{2 d^3} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left( \frac{c(3c+4dx)}{(c+dx)^2} + 2 \operatorname{Log}[c+dx] \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) + \\
 & \left. \frac{\operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right]}{d^3} \right) + \\
 & \frac{1}{i^3} 2abB^2g^2n^2 \left( -\frac{2+2 \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right]^2}{d^2(c+dx)} + \frac{c\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right] + 2 \operatorname{Log}\left[\frac{c}{d}+x\right]^2\right)}{4d^2(c+dx)^2} + \right. \\
 & 2 \left( \frac{1+\operatorname{Log}\left[\frac{c}{d}+x\right]}{d^2(c+dx)} - \frac{c\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right]\right)}{4d^2(c+dx)^2} + \frac{-\frac{\operatorname{Log}\left[\frac{a}{b}+x\right]}{d(c+dx)} - \frac{b \operatorname{Log}[a+bx]}{d(-bc+ad)} + \frac{b \operatorname{Log}[c+dx]}{d(-bc+ad)}}{d} - \frac{1}{2d^2(c+dx)^2} \right. \\
 & \left. \left. c \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \frac{1}{(bc-ad)^2} b(c+dx)(bc-ad+b(c+dx) \operatorname{Log}[a+bx] - \right. \right. \right. \\
 & \left. \left. \left. b(c+dx) \operatorname{Log}[c+dx] \right) \right) \right) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right) - \\
 & \frac{(c+2dx) \left( -\operatorname{Log}\left[\frac{a}{b}+x\right] + \operatorname{Log}\left[\frac{c}{d}+x\right] + \operatorname{Log}\left[\frac{a}{c+dx} + \frac{bx}{c+dx}\right] \right)^2}{2d^2(c+dx)^2} + \left( -d(a+bx) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 + \right. \\
 & \left. 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) / \\
 & (d^2(-bc+ad)(c+dx)) + \left( c \left( d(a+bx)(ad-b(2c+dx)) \operatorname{Log}\left[\frac{a}{b}+x\right]^2 - \right. \right. \\
 & \left. \left. 2b^2(c+dx)^2 \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] + 2b(c+dx) \operatorname{Log}\left[\frac{a}{b}+x\right] \right. \right. \\
 & \left. \left. \left( d(a+bx) + b(c+dx) \operatorname{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) + 2b^2(c+dx)^2 \operatorname{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] \right) \right) / \\
 & (2d^2(bc-ad)^2(c+dx)^2) - 2 \left( \left( 2(bc-ad) \operatorname{Log}\left[\frac{a}{b}+x\right] \left( 1 + \operatorname{Log}\left[\frac{c}{d}+x\right] \right) + b(c+dx) \right. \right. \\
 & \left. \left. \left( \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - 2 \operatorname{Log}[a+bx] - 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] + 2 \operatorname{Log}[c+dx] \right) - \right. \right. \\
 & \left. \left. 2b(c+dx) \operatorname{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] \right) \right) / (2d^2(-bc+ad)(c+dx)) + \\
 & \left( c \left( -b(bc-ad)(c+dx) + (bc-ad)^2 \operatorname{Log}\left[\frac{a}{b}+x\right] \left( 1 + 2 \operatorname{Log}\left[\frac{c}{d}+x\right] \right) - b^2(c+dx)^2 \right. \right. \\
 & \left. \left. \operatorname{Log}[a+bx] + b^2(c+dx)^2 \operatorname{Log}[c+dx] + b(c+dx) \left( b(c+dx) \operatorname{Log}\left[\frac{c}{d}+x\right]^2 - \right. \right. \right.
 \end{aligned}$$



$$\begin{aligned}
 & 2 (b c - a d) \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right) - 2 b (c + d x) \left( \text{Log} \left[ \frac{c}{d} + x \right] \text{Log} \left[ \frac{d (a + b x)}{-b c + a d} \right] + \right. \\
 & \quad \left. \text{PolyLog} \left[ 2, \frac{b (c + d x)}{b c - a d} \right] \right) \Big/ \left( 4 d^2 (b c - a d)^2 (c + d x)^2 \right) \Big) + \\
 & \frac{1}{i^3} b^2 B^2 g^2 n^2 \left( \frac{\text{Log} \left[ \frac{c}{d} + x \right]^3}{3 d^3} + \frac{2 c \left( 2 + 2 \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{d^3 (c + d x)} - \right. \\
 & \quad \frac{c^2 \left( 1 + 2 \text{Log} \left[ \frac{c}{d} + x \right] + 2 \text{Log} \left[ \frac{c}{d} + x \right]^2 \right)}{4 d^3 (c + d x)^2} + \frac{1}{2 d^3} \\
 & \quad \left( \frac{c (3 c + 4 d x)}{(c + d x)^2} + 2 \text{Log} [c + d x] \right) \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right)^2 - \\
 & \quad \left( 2 c \left( -d (a + b x) \text{Log} \left[ \frac{a}{b} + x \right]^2 + 2 b (c + d x) \text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \right. \right. \\
 & \quad \left. \left. 2 b (c + d x) \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right) \Big/ \left( d^3 (-b c + a d) (c + d x) \right) - \\
 & \quad \left( c^2 \left( d (a + b x) (a d - b (2 c + d x)) \text{Log} \left[ \frac{a}{b} + x \right]^2 - 2 b^2 (c + d x)^2 \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \right. \right. \\
 & \quad \left. \left. 2 b (c + d x) \text{Log} \left[ \frac{a}{b} + x \right] \left( d (a + b x) + b (c + d x) \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] \right) + \right. \\
 & \quad \left. \left. 2 b^2 (c + d x)^2 \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right] \right) \Big/ \right. \\
 & \quad \left. \left( 2 d^3 (b c - a d)^2 (c + d x)^2 \right) + 2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \text{Log} \left[ \frac{c}{d} + x \right] + \text{Log} \left[ \frac{a}{c + d x} + \frac{b x}{c + d x} \right] \right) \right. \\
 & \quad \left( -\frac{\text{Log} \left[ \frac{c}{d} + x \right]^2}{2 d^3} - \frac{2 c \left( 1 + \text{Log} \left[ \frac{c}{d} + x \right] \right)}{d^3 (c + d x)} + \frac{c^2 \left( 1 + 2 \text{Log} \left[ \frac{c}{d} + x \right] \right)}{4 d^3 (c + d x)^2} - \right. \\
 & \quad \frac{2 c \left( -\frac{\text{Log} \left[ \frac{a}{b} + x \right]}{d (c + d x)} - \frac{b \text{Log} [a + b x]}{d (-b c + a d)} + \frac{b \text{Log} [c + d x]}{d (-b c + a d)} \right)}{d^2} + \frac{1}{2 d^3 (c + d x)^2} c^2 \left( -\text{Log} \left[ \frac{a}{b} + x \right] + \frac{1}{(b c - a d)^2} \right. \\
 & \quad \left. \left. b (c + d x) (b c - a d + b (c + d x) \text{Log} [a + b x] - b (c + d x) \text{Log} [c + d x]) \right) \right) + \\
 & \quad \left. \frac{\text{Log} \left[ \frac{a}{b} + x \right] \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \text{PolyLog} \left[ 2, \frac{d (a + b x)}{-b c + a d} \right]}{d^3} \right) + \frac{1}{d^3} \left( \text{Log} \left[ \frac{a}{b} + x \right]^2 \text{Log} \left[ \frac{b (c + d x)}{b c - a d} \right] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 2 \operatorname{Log}\left[\frac{a}{b}+x\right] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]-2 \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right]- \\
 & 2\left(-\left(\left(c\left(2(b c-a d) \operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)+b(c+d x)\right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2-2 \operatorname{Log}[a+b x]-2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+2 \operatorname{Log}[c+d x]\right)\right.\right.\right.\right. \\
 & \quad \left.\left.\left.\left.b(c+d x) \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right)\right) / \left(d^3(-b c+a d)(c+d x)\right)- \\
 & \left(c^2\left(-b(b c-a d)(c+d x)+(b c-a d)^2 \operatorname{Log}\left[\frac{a}{b}+x\right]\left(1+2 \operatorname{Log}\left[\frac{c}{d}+x\right]\right)-\right.\right. \\
 & \quad \left.\left.b^2(c+d x)^2 \operatorname{Log}[a+b x]+b^2(c+d x)^2 \operatorname{Log}[c+d x]+b(c+d x)\left(b(c+d x) \operatorname{Log}\left[\frac{c}{d}+x\right]^2-2(b c-a d)\left(1+\operatorname{Log}\left[\frac{c}{d}+x\right]\right)-\right.\right.\right. \\
 & \quad \left.\left.\left.2 b(c+d x)\left(\operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]+\operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]\right)\right)\right)\right) / \\
 & \left(4 d^3(b c-a d)^2(c+d x)^2+\frac{1}{2 d^3}\left(\operatorname{Log}\left[\frac{c}{d}+x\right]^2\left(\operatorname{Log}\left[\frac{a}{b}+x\right]-\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]\right)-\right.\right. \\
 & \quad \left.\left.2 \operatorname{Log}\left[\frac{c}{d}+x\right] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]+2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right]\right)\right)
 \end{aligned}$$

**Problem 204: Result more than twice size of optimal antiderivative.**

$$\int \frac{(a g+b g x)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(c i+d i x)^3} d x$$

Optimal (type 3, 151 leaves, 3 steps):

$$\frac{B^2 g n^2(a+b x)^2}{4(b c-a d) i^3(c+d x)^2}-\frac{B g n(a+b x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2(b c-a d) i^3(c+d x)^2}+\frac{g(a+b x)^2\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2(b c-a d) i^3(c+d x)^2}$$

Result (type 3, 582 leaves):

$$\frac{1}{4 d^2 (b c - a d) i^3 (c + d x)^2} g \left( 2 B^2 d^2 n^2 (a + b x)^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 - \right.$$

$$2 b^2 B n (c + d x)^2 \text{Log} [a + b x] \left( -2 A + B n - 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) +$$

$$2 B (b c - a d) n (a d + b (c + 2 d x)) \text{Log} \left[ \frac{a + b x}{c + d x} \right]$$

$$\left( -2 A + B n - 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) +$$

$$(b c - a d)^2 \left( 2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 + 2 B n (-2 A + B n) \text{Log} \left[ \frac{a + b x}{c + d x} \right] + \right.$$

$$\left. 2 B^2 n^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 - 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \left( -2 A + B n + 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) - 2 b (b c - a d)$$

$$(c + d x) \left( 2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right]^2 + 2 B n (-2 A + B n) \text{Log} \left[ \frac{a + b x}{c + d x} \right] + \right.$$

$$\left. 2 B^2 n^2 \text{Log} \left[ \frac{a + b x}{c + d x} \right]^2 - 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] \left( -2 A + B n + 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \right) +$$

$$2 b^2 B n (c + d x)^2 \left( -2 A + B n - 2 B \text{Log} \left[ e \left( \frac{a + b x}{c + d x} \right)^n \right] + 2 B n \text{Log} \left[ \frac{a + b x}{c + d x} \right] \right) \text{Log} [c + d x] \Big)$$

**Problem 206: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \text{Log} [e (\frac{a+bx}{c+dx})^n])^2}{(a g + b g x) (c i + d i x)^3} dx$$

Optimal (type 3, 402 leaves, 15 steps):

$$\frac{B^2 d^2 n^2 (a + b x)^2}{4 (b c - a d)^3 g i^3 (c + d x)^2} + \frac{4 A b B d n (a + b x)}{(b c - a d)^3 g i^3 (c + d x)} -$$

$$\frac{4 b B^2 d n^2 (a + b x)}{(b c - a d)^3 g i^3 (c + d x)} + \frac{4 b B^2 d n (a + b x) \text{Log} [e (\frac{a+bx}{c+dx})^n]}{(b c - a d)^3 g i^3 (c + d x)} -$$

$$\frac{B d^2 n (a + b x)^2 (A + B \text{Log} [e (\frac{a+bx}{c+dx})^n])}{2 (b c - a d)^3 g i^3 (c + d x)^2} + \frac{d^2 (a + b x)^2 (A + B \text{Log} [e (\frac{a+bx}{c+dx})^n])^2}{2 (b c - a d)^3 g i^3 (c + d x)^2} -$$

$$\frac{2 b d (a + b x) (A + B \text{Log} [e (\frac{a+bx}{c+dx})^n])^2}{(b c - a d)^3 g i^3 (c + d x)} + \frac{b^2 (A + B \text{Log} [e (\frac{a+bx}{c+dx})^n])^3}{3 B (b c - a d)^3 g i^3 n}$$

Result (type 3, 971 leaves):

$$\begin{aligned} & \frac{1}{12 (b c - a d)^3 g i^3} \left( 4 b^2 B^2 n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^3 - \frac{1}{(c+d x)^2} 6 B n \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 \right. \\ & \quad \left( -2 A b^2 c^2 + 4 a b B c d n - a^2 B d^2 n - 4 A b^2 c d x + 4 b^2 B c d n x + 2 a b B d^2 n x - 2 A b^2 d^2 x^2 + \right. \\ & \quad \left. 3 b^2 B d^2 n x^2 - 2 b^2 B (c+d x)^2 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2 b^2 B n (c+d x)^2 \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) - \frac{1}{(c+d x)^2} \\ & 6 B (b c - a d) n \text{Log}\left[\frac{a+b x}{c+d x}\right] \left( -6 A b c + 2 a A d + 7 b B c n - a B d n - 4 A b d x + 6 b B d n x + 2 B \right. \\ & \quad \left. (-3 b c + a d - 2 b d x) \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] + 2 B n (3 b c - a d + 2 b d x) \text{Log}\left[\frac{a+b x}{c+d x}\right] \right) + \frac{1}{(c+d x)^2} \\ & 3 (b c - a d)^2 \left( 2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2 B n (-2 A + B n) \text{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\ & \quad \left. 2 B^2 n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 - 2 B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] (-2 A + B n + 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right]) \right) + \frac{1}{c+d x} \\ & 6 b (b c - a d) \left( 2 A^2 - 6 A B n + 7 B^2 n^2 + 2 B^2 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2 B n (-2 A + 3 B n) \text{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\ & \quad \left. 2 B^2 n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 - 2 B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] (-2 A + 3 B n + 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right]) \right) + \\ & 6 b^2 \text{Log}[a+b x] \left( 2 A^2 - 6 A B n + 7 B^2 n^2 + 2 B^2 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2 B n (-2 A + 3 B n) \text{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\ & \quad \left. 2 B^2 n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 - 2 B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] (-2 A + 3 B n + 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right]) \right) - \\ & 6 b^2 \left( 2 A^2 - 6 A B n + 7 B^2 n^2 + 2 B^2 \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2 + 2 B n (-2 A + 3 B n) \text{Log}\left[\frac{a+b x}{c+d x}\right] + \right. \\ & \quad \left. 2 B^2 n^2 \text{Log}\left[\frac{a+b x}{c+d x}\right]^2 - 2 B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right] (-2 A + 3 B n + 2 B n \text{Log}\left[\frac{a+b x}{c+d x}\right]) \right) \text{Log}[c+d x] \left. \right) \end{aligned}$$

**Problem 207: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right])^2}{(a g + b g x)^2 (c i + d i x)^3} dx$$

Optimal (type 3, 562 leaves, 12 steps):

$$\begin{aligned}
 & - \frac{B^2 d^3 n^2 (a + b x)^2}{4 (b c - a d)^4 g^2 i^3 (c + d x)^2} - \frac{6 A b B d^2 n (a + b x)}{(b c - a d)^4 g^2 i^3 (c + d x)} + \\
 & \frac{6 b B^2 d^2 n^2 (a + b x)}{(b c - a d)^4 g^2 i^3 (c + d x)} - \frac{2 b^3 B^2 n^2 (c + d x)}{(b c - a d)^4 g^2 i^3 (a + b x)} - \frac{6 b B^2 d^2 n (a + b x) \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]}{(b c - a d)^4 g^2 i^3 (c + d x)} + \\
 & \frac{B d^3 n (a + b x)^2 \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{2 (b c - a d)^4 g^2 i^3 (c + d x)^2} - \frac{2 b^3 B n (c + d x) \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{(b c - a d)^4 g^2 i^3 (a + b x)} - \\
 & \frac{d^3 (a + b x)^2 \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{2 (b c - a d)^4 g^2 i^3 (c + d x)^2} + \frac{3 b d^2 (a + b x) \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^4 g^2 i^3 (c + d x)} - \\
 & \frac{b^3 (c + d x) \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^2}{(b c - a d)^4 g^2 i^3 (a + b x)} - \frac{b^2 d \left(A + B \text{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^3}{B (b c - a d)^4 g^2 i^3 n}
 \end{aligned}$$

Result(type 3, 1334 leaves):

$$\begin{aligned}
 & \frac{1}{4 (b c - a d)^4 g^2 i^3 (a + b x) (c + d x)^2} \\
 & \left( 4 b^2 B^2 d n^2 (a + b x) (c + d x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^3 + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 \right. \\
 & \quad \left( 6 a A b^2 c^2 d + 2 b^3 B c^3 n - 6 a^2 b B c d^2 n + a^3 B d^3 n + 6 A b^3 c^2 d x + 12 a A b^2 c d^2 x + \right. \\
 & \quad 6 b^3 B c^2 d n x - 12 a b^2 B c d^2 n x - 3 a^2 b B d^3 n x + 12 A b^3 c d^2 x^2 + 6 a A b^2 d^3 x^2 - \\
 & \quad 9 a b^2 B d^3 n x^2 + 6 A b^3 d^3 x^3 - 3 b^3 B d^3 n x^3 + 6 b^2 B d (a + b x) (c + d x)^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - \\
 & \quad \left. 6 b^2 B d n (a + b x) (c + d x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + 4 b^2 (b c - a d) (c + d x)^2 \\
 & \quad \left( A^2 + 2 A B n + 2 B^2 n^2 + B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + \right. \\
 & \quad \left. 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( A + B n - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 2 B (b c - a d) n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \\
 & \quad \left( 2 b d (a + b x) (c + d x) \left( 4 A - 5 B n + 4 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad d (b c - a d) (a + b x) \left( 2 A - B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \\
 & \quad \left. 4 b^2 (c + d x)^2 \left( A + B n + B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + d (b c - a d)^2 \\
 & \quad (a + b x) \left( 2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
 & \quad 6 b^2 d (a + b x) (c + d x)^2 \operatorname{Log}[a + b x] \left( 2 A^2 - 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \right. \\
 & \quad \left. 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - \right. \\
 & \quad \left. 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 2 b d (b c - a d) (a + b x) (c + d x) \\
 & \quad \left( 4 A^2 - 10 A B n + 11 B^2 n^2 + 4 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-4 A + 5 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 4 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -4 A + 5 B n + 4 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - \\
 & \quad 6 b^2 d (a + b x) (c + d x)^2 \left( 2 A^2 - 2 A B n + 5 B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \right. \\
 & \quad \left. 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - \right. \\
 & \quad \left. 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) \operatorname{Log}[c + d x]
 \end{aligned}$$

### Problem 208: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right])^2}{(ag + bgx)^3 (ci + dix)^3} dx$$

Optimal (type 3, 732 leaves, 14 steps):

$$\begin{aligned} & \frac{B^2 d^4 n^2 (a+bx)^2}{4 (bc-ad)^5 g^3 i^3 (c+dx)^2} + \frac{8 A b B d^3 n (a+bx)}{(bc-ad)^5 g^3 i^3 (c+dx)} - \frac{8 b B^2 d^3 n^2 (a+bx)}{(bc-ad)^5 g^3 i^3 (c+dx)} + \\ & \frac{8 b^3 B^2 d n^2 (c+dx)}{(bc-ad)^5 g^3 i^3 (a+bx)} - \frac{b^4 B^2 n^2 (c+dx)^2}{4 (bc-ad)^5 g^3 i^3 (a+bx)^2} + \frac{8 b B^2 d^3 n (a+bx) \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]}{(bc-ad)^5 g^3 i^3 (c+dx)} - \\ & \frac{B d^4 n (a+bx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{2 (bc-ad)^5 g^3 i^3 (c+dx)^2} + \frac{8 b^3 B d n (c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{(bc-ad)^5 g^3 i^3 (a+bx)} - \\ & \frac{b^4 B n (c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)}{2 (bc-ad)^5 g^3 i^3 (a+bx)^2} + \frac{d^4 (a+bx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2 (bc-ad)^5 g^3 i^3 (c+dx)^2} - \\ & \frac{4 b d^3 (a+bx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bc-ad)^5 g^3 i^3 (c+dx)} + \frac{4 b^3 d (c+dx) \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{(bc-ad)^5 g^3 i^3 (a+bx)} - \\ & \frac{b^4 (c+dx)^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^2}{2 (bc-ad)^5 g^3 i^3 (a+bx)^2} + \frac{2 b^2 d^2 \left(A + B \operatorname{Log}\left[e \left(\frac{a+bx}{c+dx}\right)^n\right]\right)^3}{B (bc-ad)^5 g^3 i^3 n} \end{aligned}$$

Result (type 3, 1653 leaves):

$$\begin{aligned}
 & \frac{1}{4 (b c - a d)^5 g^3 i^3 (a + b x)^2 (c + d x)^2} \\
 & \left( 8 b^2 B^2 d^2 n^2 (a + b x)^2 (c + d x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^3 + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 \right. \\
 & \quad \left( 12 a^2 A b^2 c^2 d^2 - b^4 B c^4 n + 8 a b^3 B c^3 d n - 8 a^3 b B c d^3 n + a^4 B d^4 n + 24 a A b^3 c^2 d^2 x + \right. \\
 & \quad 24 a^2 A b^2 c d^3 x + 4 b^4 B c^3 d n x + 24 a b^3 B c^2 d^2 n x - 24 a^2 b^2 B c d^3 n x - 4 a^3 b B d^4 n x + \\
 & \quad 12 A b^4 c^2 d^2 x^2 + 48 a A b^3 c d^3 x^2 + 12 a^2 A b^2 d^4 x^2 + 18 b^4 B c^2 d^2 n x^2 - 18 a^2 b^2 B d^4 n x^2 + \\
 & \quad 24 A b^4 c d^3 x^3 + 24 a A b^3 d^4 x^3 + 12 b^4 B c d^3 n x^3 - 12 a b^3 B d^4 n x^3 + 12 A b^4 d^4 x^4 + 12 b^2 B d^2 \\
 & \quad \left. (a + b x)^2 (c + d x)^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 12 b^2 B d^2 n (a + b x)^2 (c + d x)^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \\
 & 12 b^2 d^2 (a + b x)^2 (c + d x)^2 \operatorname{Log}[a + b x] \left( 2 A^2 + 5 B^2 n^2 + 4 A B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \left. 2 B^2 \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 \right) + 2 b^2 d (b c - a d) (a + b x) (c + d x)^2 \\
 & \left( 6 A^2 + 14 A B n + 15 B^2 n^2 + 6 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (6 A + 7 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 6 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 6 A + 7 B n - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - b^2 (b c - a d)^2 \\
 & (c + d x)^2 \left( 2 A^2 + 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 - 2 B n (2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( 2 A + B n - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 2 B (b c - a d) n \\
 & \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \left( 2 b d^2 (a + b x)^2 (c + d x) \left( 6 A - 7 B n + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \left. 2 b^2 d (a + b x) (c + d x)^2 \left( 6 A + 7 B n + 6 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
 & \quad d^2 (b c - a d) (a + b x)^2 \left( 2 A - B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) - \\
 & \quad b^2 (b c - a d) (c + d x)^2 \left( 2 A + B n + 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + \\
 & d^2 (b c - a d)^2 (a + b x)^2 \left( 2 A^2 - 2 A B n + B^2 n^2 + 2 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + \right. \\
 & \quad \left. 2 B n (-2 A + B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + 2 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - \right. \\
 & \quad \left. 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -2 A + B n + 2 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) + 2 b d^2 (b c - a d) (a + b x)^2 (c + d x) \\
 & \left( 6 A^2 - 14 A B n + 15 B^2 n^2 + 6 B^2 \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right]^2 + 2 B n (-6 A + 7 B n) \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] + \right. \\
 & \quad \left. 6 B^2 n^2 \operatorname{Log}\left[\frac{a + b x}{c + d x}\right]^2 - 2 B \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] \left( -6 A + 7 B n + 6 B n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) \right) - \\
 & 12 b^2 d^2 (a + b x)^2 (c + d x)^2 \left( 2 A^2 + 5 B^2 n^2 + 4 A B \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right) + \right. \\
 & \quad \left. 2 B^2 \left( \operatorname{Log}\left[e\left(\frac{a + b x}{c + d x}\right)^n\right] - n \operatorname{Log}\left[\frac{a + b x}{c + d x}\right] \right)^2 \right) \operatorname{Log}[c + d x] \Big)
 \end{aligned}$$



### Problem 209: Result more than twice size of optimal antiderivative.

$$\int \frac{(A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])^2}{(ag + bgx)^4 (ci + dix)^3} dx$$

Optimal (type 3, 908 leaves, 16 steps):

$$\begin{aligned} & -\frac{B^2 d^5 n^2 (a+bx)^2}{4 (bc-ad)^6 g^4 i^3 (c+dx)^2} - \frac{10 A b B d^4 n (a+bx)}{(bc-ad)^6 g^4 i^3 (c+dx)} + \\ & \frac{10 b B^2 d^4 n^2 (a+bx)}{(bc-ad)^6 g^4 i^3 (c+dx)} - \frac{20 b^3 B^2 d^2 n^2 (c+dx)}{(bc-ad)^6 g^4 i^3 (a+bx)} + \frac{5 b^4 B^2 d n^2 (c+dx)^2}{4 (bc-ad)^6 g^4 i^3 (a+bx)^2} - \\ & \frac{2 b^5 B^2 n^2 (c+dx)^3}{27 (bc-ad)^6 g^4 i^3 (a+bx)^3} - \frac{10 b B^2 d^4 n (a+bx) \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right]}{(bc-ad)^6 g^4 i^3 (c+dx)} + \\ & \frac{B d^5 n (a+bx)^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{2 (bc-ad)^6 g^4 i^3 (c+dx)^2} - \frac{20 b^3 B d^2 n (c+dx) (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{(bc-ad)^6 g^4 i^3 (a+bx)} + \\ & \frac{5 b^4 B d n (c+dx)^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{2 (bc-ad)^6 g^4 i^3 (a+bx)^2} - \frac{2 b^5 B n (c+dx)^3 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])}{9 (bc-ad)^6 g^4 i^3 (a+bx)^3} - \\ & \frac{d^5 (a+bx)^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])^2}{2 (bc-ad)^6 g^4 i^3 (c+dx)^2} + \frac{5 b d^4 (a+bx) (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])^2}{(bc-ad)^6 g^4 i^3 (c+dx)} - \\ & \frac{10 b^3 d^2 (c+dx) (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])^2}{(bc-ad)^6 g^4 i^3 (a+bx)} + \frac{5 b^4 d (c+dx)^2 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])^2}{2 (bc-ad)^6 g^4 i^3 (a+bx)^2} - \\ & \frac{b^5 (c+dx)^3 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])^2}{3 (bc-ad)^6 g^4 i^3 (a+bx)^3} - \frac{10 b^2 d^3 (A + B \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right])^3}{3 B (bc-ad)^6 g^4 i^3 n} \end{aligned}$$

Result (type 3, 2138 leaves):

$$\begin{aligned} & \frac{1}{108 (bc-ad)^6 g^4 i^3 (a+bx)^3 (c+dx)^2} \\ & \left( 360 b^2 B^2 d^3 n^2 (a+bx)^3 (c+dx)^2 \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^3 + 18 B n \operatorname{Log}\left[\frac{a+bx}{c+dx}\right]^2 \right. \\ & \left( 60 a^3 A b^2 c^2 d^3 + 2 b^5 B c^5 n - 15 a b^4 B c^4 d n + 60 a^2 b^3 B c^3 d^2 n - 30 a^4 b B c d^4 n + \right. \\ & 3 a^5 B d^5 n + 180 a^2 A b^3 c^2 d^3 x + 120 a^3 A b^2 c d^4 x - 5 b^5 B c^4 d n x + 60 a b^4 B c^3 d^2 n x + \\ & 180 a^2 b^3 B c^2 d^3 n x - 120 a^3 b^2 B c d^4 n x - 15 a^4 b B d^5 n x + 180 a A b^4 c^2 d^3 x^2 + \\ & 360 a^2 A b^3 c d^4 x^2 + 60 a^3 A b^2 d^5 x^2 + 20 b^5 B c^3 d^2 n x^2 + 270 a b^4 B c^2 d^3 n x^2 - \\ & 90 a^3 b^2 B d^5 n x^2 + 60 A b^5 c^2 d^3 x^3 + 360 a A b^4 c d^4 x^3 + 180 a^2 A b^3 d^5 x^3 + 110 b^5 B c^2 d^3 n x^3 + \\ & 180 a b^4 B c d^4 n x^3 - 90 a^2 b^3 B d^5 n x^3 + 120 A b^5 c d^4 x^4 + 180 a A b^4 d^5 x^4 + 100 b^5 B c d^4 n x^4 + \\ & \left. \left. 60 A b^5 d^5 x^5 + 20 b^5 B d^5 n x^5 + 60 b^2 B d^3 (a+bx)^3 (c+dx)^2 \operatorname{Log}\left[e\left(\frac{a+bx}{c+dx}\right)^n\right] \right) \right] - \end{aligned}$$

$$\begin{aligned}
 & 60 b^2 B d^3 n (a+b x)^3 (c+d x)^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] + 6 b^2 d^2 (b c-a d) (a+b x)^2 (c+d x)^2 \\
 & \left(108 A^2+282 A B n+319 B^2 n^2+108 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-6 B n(36 A+47 B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \right. \\
 & \left.108 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(36 A+47 B n-36 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)- \\
 & 3 b^2 d(b c-a d)^2(a+b x)(c+d x)^2\left(54 A^2+66 A B n+37 B^2 n^2+54 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-\right. \\
 & \left.6 B n(18 A+11 B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+54 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+\right. \\
 & \left.6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(18 A+11 B n-18 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)+4 b^2(b c-a d)^3(c+d x)^2 \\
 & \left(9 A^2+6 A B n+2 B^2 n^2+9 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-6 B n(3 A+B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \right. \\
 & \left.9 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+6 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(3 A+B n-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)+ \\
 & 60 b^2 d^3(a+b x)^3(c+d x)^2 \operatorname{Log}[a+b x]\left(18 A^2+12 A B n+49 B^2 n^2+\right. \\
 & \left.18 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-12 B n(3 A+B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+18 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+\right. \\
 & \left.12 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(3 A+B n-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)+27 d^3(b c-a d)^2(a+b x)^3 \\
 & \left(2 A^2-2 A B n+B^2 n^2+2 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+2 B n(-2 A+B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+ \right. \\
 & \left.2 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2-2 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(-2 A+B n+2 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)+ \\
 & 54 b d^3(b c-a d)(a+b x)^3(c+d x)\left(8 A^2-18 A B n+19 B^2 n^2+8 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2+\right. \\
 & \left.2 B n(-8 A+9 B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+8 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2-\right. \\
 & \left.2 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(-8 A+9 B n+8 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)+6 B(b c-a d) n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right] \\
 & \left(18 b d^3(a+b x)^3(c+d x)\left(8 A-9 B n+8 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-8 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+ \right. \\
 & \left.4 b^2(b c-a d)^2(c+d x)^2\left(3 A+B n+3 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)+ \right. \\
 & \left.9 d^3(b c-a d)(a+b x)^3\left(2 A-B n+2 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-2 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)-3 b^2 d \right. \\
 & \left.(b c-a d)(a+b x)(c+d x)^2\left(18 A+11 B n+18 B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)\right)+ \\
 & \left.6 b^2 d^2(a+b x)^2(c+d x)^2\left(36 A+47 B n+36 B\left(\operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]-n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right)\right)\right)- \\
 & 60 b^2 d^3(a+b x)^3(c+d x)^2\left(18 A^2+12 A B n+49 B^2 n^2+18 B^2 \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]^2-\right. \\
 & \left.12 B n(3 A+B n) \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]+18 B^2 n^2 \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]^2+\right.
 \end{aligned}$$

$$12 B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\left(3 A+B n-3 B n \operatorname{Log}\left[\frac{a+b x}{c+d x}\right]\right) \operatorname{Log}[c+d x]$$

### Problem 210: Unable to integrate problem.

$$\int (a g+b g x)^m (c i+d i x)^{-2-m}\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^p d x$$

Optimal (type 4, 189 leaves, 3 steps):

$$\begin{aligned} & e^{-\frac{A(1+m)}{B n}}(a+b x)(g(a+b x))^m\left(e\left(\frac{a+b x}{c+d x}\right)^n\right)^{-\frac{1+m}{n}}(i(c+d x))^{-m} \\ & \operatorname{Gamma}\left[1+p,-\frac{(1+m)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{B n}\right]\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^p \\ & \left(-\frac{(1+m)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{B n}\right)^{-p} /((b c-a d) i^2(1+m)(c+d x)) \end{aligned}$$

Result (type 8, 51 leaves):

$$\int (a g+b g x)^m (c i+d i x)^{-2-m}\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^p d x$$

### Problem 211: Unable to integrate problem.

$$\int (a g+b g x)^{-2-m}(c i+d i x)^m\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^p d x$$

Optimal (type 4, 190 leaves, 3 steps):

$$\begin{aligned} & -\left(e^{\frac{A(1+m)}{B n}}(a+b x)(g(a+b x))^{-2-m}\left(e\left(\frac{a+b x}{c+d x}\right)^n\right)^{\frac{1+m}{n}}(i(c+d x))^{2+m}\right. \\ & \operatorname{Gamma}\left[1+p,\frac{(1+m)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{B n}\right]\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^p \\ & \left.\left(\frac{(1+m)\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)}{B n}\right)^{-p} /((b c-a d) i^2(1+m)(c+d x))\right) \end{aligned}$$

Result (type 8, 51 leaves):

$$\int (a g+b g x)^{-2-m}(c i+d i x)^m\left(A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]\right)^p d x$$

### Problem 215: Unable to integrate problem.

$$\int \frac{(a g+b g x)^m (c i+d i x)^{-2-m}}{A+B \operatorname{Log}\left[e\left(\frac{a+b x}{c+d x}\right)^n\right]} d x$$

Optimal (type 4, 125 leaves, 3 steps):

$$\left( e^{-\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^m \left( e \left( \frac{a+bx}{c+dx} \right)^n \right)^{-\frac{1+m}{n}} (i(c+dx))^{-m} \right. \\ \left. \text{ExpIntegralEi} \left[ \frac{(1+m) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) / (B(bc-ad) i^2 n (c+dx))$$

Result (type 8, 51 leaves):

$$\int \frac{(ag+bgx)^m (ci+dix)^{-2-m}}{A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right]} dx$$

**Problem 216: Unable to integrate problem.**

$$\int \frac{(ag+bgx)^m (ci+dix)^{-2-m}}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2} dx$$

Optimal (type 4, 206 leaves, 4 steps):

$$\left( e^{-\frac{A(1+m)}{Bn}} (1+m) (a+bx) (g(a+bx))^m \left( e \left( \frac{a+bx}{c+dx} \right)^n \right)^{-\frac{1+m}{n}} \right. \\ \left. (i(c+dx))^{-m} \text{ExpIntegralEi} \left[ \frac{(1+m) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) / \\ (B^2 (bc-ad) i^2 n^2 (c+dx)) - \frac{(a+bx) (g(a+bx))^m (i(c+dx))^{-m}}{B(bc-ad) i^2 n (c+dx) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}$$

Result (type 8, 51 leaves):

$$\int \frac{(ag+bgx)^m (ci+dix)^{-2-m}}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2} dx$$

**Problem 217: Unable to integrate problem.**

$$\int \frac{(ag+bgx)^m (ci+dix)^{-2-m}}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^3} dx$$

Optimal (type 4, 295 leaves, 5 steps):

$$\begin{aligned}
 & \left( e^{-\frac{A(1+m)}{Bn}} (1+m)^2 (a+bx) (g(a+bx))^m \left( e \left( \frac{a+bx}{c+dx} \right)^n \right)^{-\frac{1+m}{n}} (i(c+dx))^{-m} \right. \\
 & \quad \left. \text{ExpIntegralEi} \left[ \frac{(1+m) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) / (2B^3 (bc-ad) i^2 n^3 (c+dx)) - \\
 & \quad \frac{(a+bx) (g(a+bx))^m (i(c+dx))^{-m}}{2B (bc-ad) i^2 n (c+dx) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2} - \\
 & \quad \frac{(1+m) (a+bx) (g(a+bx))^m (i(c+dx))^{-m}}{2B^2 (bc-ad) i^2 n^2 (c+dx) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}
 \end{aligned}$$

Result (type 8, 51 leaves):

$$\int \frac{(ag+bgx)^m (ci+dix)^{-2-m}}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^3} dx$$

Problem 221: Unable to integrate problem.

$$\int \frac{(ag+bgx)^{-2-m} (ci+dix)^m}{A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right]} dx$$

Optimal (type 4, 128 leaves, 3 steps):

$$\begin{aligned}
 & \left( e^{\frac{A(1-m)}{Bn}} (a+bx) (g(a+bx))^{-2-m} \left( e \left( \frac{a+bx}{c+dx} \right)^n \right)^{\frac{1+m}{n}} (i(c+dx))^{2+m} \right. \\
 & \quad \left. \text{ExpIntegralEi} \left[ -\frac{(1+m) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) / (B (bc-ad) i^2 n (c+dx))
 \end{aligned}$$

Result (type 8, 51 leaves):

$$\int \frac{(ag+bgx)^{-2-m} (ci+dix)^m}{A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right]} dx$$

Problem 222: Unable to integrate problem.

$$\int \frac{(ag+bgx)^{-2-m} (ci+dix)^m}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2} dx$$

Optimal (type 4, 214 leaves, 4 steps):

$$- \left( \left( e^{\frac{A(1+m)}{Bn}} (1+m) (a+bx) (g(a+bx))^{-2-m} \left( e \left( \frac{a+bx}{c+dx} \right)^n \right)^{\frac{1+m}{n}} (i(c+dx))^{2+m} \right. \right. \\ \left. \left. \text{ExpIntegralEi} \left[ -\frac{(1+m) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) \right) / (B^2 (bc-ad) i^2 n^2 (c+dx)) \Bigg) - \\ \frac{(a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m}}{B (bc-ad) i^2 n (c+dx) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}$$

Result (type 8, 51 leaves):

$$\int \frac{(ag+bgx)^{-2-m} (ci+dix)^m}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2} dx$$

Problem 223: Unable to integrate problem.

$$\int \frac{(ag+bgx)^{-2-m} (ci+dix)^m}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^3} dx$$

Optimal (type 4, 306 leaves, 5 steps):

$$\left( e^{\frac{A(1+m)}{Bn}} (1+m)^2 (a+bx) (g(a+bx))^{-2-m} \left( e \left( \frac{a+bx}{c+dx} \right)^n \right)^{\frac{1+m}{n}} \right. \\ \left. (i(c+dx))^{2+m} \text{ExpIntegralEi} \left[ -\frac{(1+m) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}{Bn} \right] \right) / \\ (2B^3 (bc-ad) i^2 n^3 (c+dx)) - \frac{(a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m}}{2B (bc-ad) i^2 n (c+dx) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^2} + \\ \frac{(1+m) (a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m}}{2B^2 (bc-ad) i^2 n^2 (c+dx) \left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)}$$

Result (type 8, 51 leaves):

$$\int \frac{(ag+bgx)^{-2-m} (ci+dix)^m}{\left( A+B \text{Log} \left[ e \left( \frac{a+bx}{c+dx} \right)^n \right] \right)^3} dx$$

Problem 226: Unable to integrate problem.

$$\int (ag+bgx)^m (ci+dix)^{-2-m} (A+B \text{Log} [e (a+bx)^n (c+dx)^{-n}])^p dx$$

Optimal (type 4, 193 leaves, 4 steps):

$$\left( e^{-\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^m (i(c+dx))^{-m} (e(a+bx)^n (c+dx)^{-n})^{-\frac{1+m}{n}} \right. \\ \left. \text{Gamma}\left[1+p, -\frac{(1+m)(A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])}{Bn}\right] (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^p \right. \\ \left. \left( -\frac{(1+m)(A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])}{Bn} \right)^{-p} \right) / ((bc-ad) i^2 (1+m) (c+dx))$$

Result (type 8, 52 leaves):

$$\int (ag+bgx)^m (ci+dix)^{-2-m} (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^p dx$$

**Problem 227: Unable to integrate problem.**

$$\int (ag+bgx)^{-2-m} (ci+dix)^m (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^p dx$$

Optimal (type 4, 194 leaves, 4 steps):

$$- \left( \left( e^{\frac{A(1+m)}{Bn}} (a+bx) (g(a+bx))^{-2-m} (i(c+dx))^{2+m} (e(a+bx)^n (c+dx)^{-n})^{\frac{1+m}{n}} \right. \right. \\ \left. \left. \text{Gamma}\left[1+p, \frac{(1+m)(A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])}{Bn}\right] (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^p \right. \right. \\ \left. \left. \left( \frac{(1+m)(A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])}{Bn} \right)^{-p} \right) / ((bc-ad) i^2 (1+m) (c+dx)) \right)$$

Result (type 8, 52 leaves):

$$\int (ag+bgx)^{-2-m} (ci+dix)^m (A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^p dx$$

**Problem 228: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^3}{(a+bx)(c+dx)} dx$$

Optimal (type 3, 45 leaves, 4 steps):

$$\frac{(A+B \text{Log}[e(a+bx)^n (c+dx)^{-n}])^4}{4B(bc-ad)n}$$

Result (type 3, 118 leaves):

$$\frac{1}{4bcn-4adn} \left( 4A^3 \text{Log}[e(a+bx)^n (c+dx)^{-n}] + 6A^2 B \text{Log}[e(a+bx)^n (c+dx)^{-n}]^2 + \right. \\ \left. 4A B^2 \text{Log}[e(a+bx)^n (c+dx)^{-n}]^3 + B^3 \text{Log}[e(a+bx)^n (c+dx)^{-n}]^4 \right)$$

### Problem 240: Unable to integrate problem.

$$\int \frac{(a + b x)^m (c + d x)^{-2-m}}{\text{Log}[e (a + b x)^n (c + d x)^{-n}]} dx$$

Optimal (type 4, 88 leaves, 4 steps):

$$\frac{1}{(b c - a d) n} (a + b x)^{1+m} (c + d x)^{-1-m} (e (a + b x)^n (c + d x)^{-n})^{-\frac{1+m}{n}}$$

$$\text{ExpIntegralEi}\left[\frac{(1+m) \text{Log}[e (a + b x)^n (c + d x)^{-n}]}{n}\right]$$

Result (type 8, 42 leaves):

$$\int \frac{(a + b x)^m (c + d x)^{-2-m}}{\text{Log}[e (a + b x)^n (c + d x)^{-n}]} dx$$

### Problem 249: Unable to integrate problem.

$$\int \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^4}{(f + g x) (a h + b h x)} dx$$

Optimal (type 4, 361 leaves, 8 steps):

$$-\frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^4 \text{Log}\left[1 - \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} +$$

$$\frac{4 B n (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^3 \text{PolyLog}\left[2, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} + \frac{1}{(b f - a g) h}$$

$$+ \frac{12 B^2 n^2 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^2 \text{PolyLog}\left[3, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} +$$

$$+ \frac{24 B^3 n^3 (A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{PolyLog}\left[4, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} +$$

$$+ \frac{24 B^4 n^4 \text{PolyLog}\left[5, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h}$$

Result (type 8, 45 leaves):

$$\int \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^4}{(f + g x) (a h + b h x)} dx$$

### Problem 250: Unable to integrate problem.

$$\int \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{(f + g x) (a h + b h x)} dx$$



Optimal (type 4, 282 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}])^3 \operatorname{Log}\left[1-\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{3 B n(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}])^2 \operatorname{PolyLog}\left[2, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{6 B^2 n^2(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}]) \operatorname{PolyLog}\left[3, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{6 B^3 n^3 \operatorname{PolyLog}\left[4, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h}
 \end{aligned}$$

Result (type 8, 45 leaves):

$$\int \frac{(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}])^3}{(f+g x)(a h+b h x)} dx$$

**Problem 251: Result more than twice size of optimal antiderivative.**

$$\int \frac{(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}])^2}{(f+g x)(a h+b h x)} dx$$

Optimal (type 4, 203 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}])^2 \operatorname{Log}\left[1-\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{2 B n(A+B \operatorname{Log}[e(a+b x)^n(c+d x)^{-n}]) \operatorname{PolyLog}\left[2, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h}
 \end{aligned}$$

Result (type 4, 1415 leaves):

$$\begin{aligned}
 & \frac{1}{3(b f-a g) h} \\
 & \left( 3 \operatorname{Log}[a+b x] (A+B(-n \operatorname{Log}[a+b x]+n \operatorname{Log}[c+d x]+\operatorname{Log}[e(a+b x)^n(c+d x)^{-n}]))^2 - \right. \\
 & \quad 3(A+B(-n \operatorname{Log}[a+b x]+n \operatorname{Log}[c+d x]+\operatorname{Log}[e(a+b x)^n(c+d x)^{-n}]))^2 \operatorname{Log}[f+g x] + \\
 & \quad 3 B n(A+B(-n \operatorname{Log}[a+b x]+n \operatorname{Log}[c+d x]+\operatorname{Log}[e(a+b x)^n(c+d x)^{-n}]))) \\
 & \quad \left. \left( \operatorname{Log}[a+b x]^2 - 2 \left( \operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right] + \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right] \right) \right) - \right. \\
 & \quad \left. 6 A B n \left( \operatorname{Log}[c+d x] \left( \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right] \right) \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \text{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] + \\
 & 6B^2n \left( n \text{Log}[a+bx] - n \text{Log}[c+dx] - \text{Log}\left[e(a+bx)^n(c+dx)^{-n}\right] \right) \\
 & \left( \text{Log}[c+dx] \left( \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] - \text{Log}\left[\frac{d(f+gx)}{df-cg}\right] \right) + \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - \right. \\
 & \left. \text{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] \right) + B^2n^2 \left( \text{Log}[a+bx]^2 \left( \text{Log}[a+bx] - 3 \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] \right) - \right. \\
 & \left. 6 \text{Log}[a+bx] \text{PolyLog}\left[2, \frac{g(a+bx)}{-bf+ag}\right] + 6 \text{PolyLog}\left[3, \frac{g(a+bx)}{-bf+ag}\right] \right) + \\
 & 3B^2n^2 \left( \text{Log}\left[\frac{d(a+bx)}{-bc+ad}\right] \text{Log}[c+dx]^2 - \text{Log}[c+dx]^2 \text{Log}\left[\frac{d(f+gx)}{df-cg}\right] + \right. \\
 & \left. 2 \text{Log}[c+dx] \text{PolyLog}\left[2, \frac{b(c+dx)}{bc-ad}\right] - 2 \text{Log}[c+dx] \text{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] - \right. \\
 & \left. 2 \text{PolyLog}\left[3, \frac{b(c+dx)}{bc-ad}\right] + 2 \text{PolyLog}\left[3, \frac{g(c+dx)}{-df+cg}\right] \right) - \\
 & 6B^2n^2 \left( \frac{1}{2} \text{Log}[a+bx]^2 \left( \text{Log}[c+dx] - \text{Log}\left[\frac{b(c+dx)}{bc-ad}\right] \right) - \text{Log}[a+bx] \text{Log}[c+dx] \right. \\
 & \left. \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \frac{1}{2} \text{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \left( -2 \text{Log}[a+bx] + \text{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \right) \right) \\
 & \left( \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[\frac{d(f+gx)}{df-cg}\right] \right) + \text{Log}\left[\frac{g(c+dx)}{-df+cg}\right] \text{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \\
 & \left( \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[\frac{d(f+gx)}{df-cg}\right] \right) - \frac{1}{2} \text{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right]^2 \\
 & \left( \text{Log}\left[\frac{-bc+ad}{d(a+bx)}\right] + \text{Log}\left[\frac{b(f+gx)}{bf-ag}\right] - \text{Log}\left[\frac{(-bc+ad)(f+gx)}{(df-cg)(a+bx)}\right] \right) - \\
 & \text{Log}[a+bx] \text{PolyLog}\left[2, \frac{d(a+bx)}{-bc+ad}\right] - \left( \text{Log}[c+dx] - \text{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) \text{PolyLog}\left[ \right. \\
 & \left. 2, \frac{g(a+bx)}{-bf+ag}\right] - \left( \text{Log}[a+bx] + \text{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) \text{PolyLog}\left[2, \frac{g(c+dx)}{-df+cg}\right] - \\
 & \text{Log}\left[\frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \left( \text{PolyLog}\left[2, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[2, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right) + \\
 & \text{PolyLog}\left[3, \frac{d(a+bx)}{-bc+ad}\right] + \text{PolyLog}\left[3, \frac{g(a+bx)}{-bf+ag}\right] + \text{PolyLog}\left[3, \frac{g(c+dx)}{-df+cg}\right] + \\
 & \left. \text{PolyLog}\left[3, \frac{b(c+dx)}{d(a+bx)}\right] - \text{PolyLog}\left[3, \frac{(bf-ag)(c+dx)}{(df-cg)(a+bx)}\right] \right)
 \end{aligned}$$

Problem 252: Result more than twice size of optimal antiderivative.

$$\int \frac{A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]}{(f + g x) (a h + b h x)} dx$$

Optimal (type 4, 123 leaves, 5 steps):

$$-\frac{(A + B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right]) \operatorname{Log}\left[1 - \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} + \frac{B n \operatorname{PolyLog}\left[2, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h}$$

Result (type 4, 304 leaves):

$$\begin{aligned} & -\frac{1}{2 (b f - a g) h} \left( -2 A \operatorname{Log}[a + b x] + B n \operatorname{Log}[a + b x]^2 - 2 B n \operatorname{Log}[a + b x] \operatorname{Log}[c + d x] + \right. \\ & \quad 2 B n \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \operatorname{Log}[c + d x] - 2 B \operatorname{Log}[a + b x] \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + \\ & \quad 2 A \operatorname{Log}[f + g x] - 2 B n \operatorname{Log}[a + b x] \operatorname{Log}[f + g x] + 2 B n \operatorname{Log}[c + d x] \operatorname{Log}[f + g x] + \\ & \quad 2 B \operatorname{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] \operatorname{Log}[f + g x] + 2 B n \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \\ & \quad 2 B n \operatorname{Log}[c + d x] \operatorname{Log}\left[\frac{d (f + g x)}{d f - c g}\right] + 2 B n \operatorname{PolyLog}\left[2, \frac{g (a + b x)}{-b f + a g}\right] + \\ & \quad \left. 2 B n \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 2 B n \operatorname{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g}\right] \right) \end{aligned}$$

**Problem 255: Result more than twice size of optimal antiderivative.**

$$\int \frac{\operatorname{Log}\left[\frac{c + d x}{a + b x}\right]}{(a + b x) ((a - c) h + (b - d) h x)} dx$$

Optimal (type 4, 33 leaves, 2 steps):

$$-\frac{\operatorname{PolyLog}\left[2, 1 - \frac{c + d x}{a + b x}\right]}{(b c - a d) h}$$

Result (type 4, 324 leaves):

$$\begin{aligned} & \frac{1}{(2 b c - 2 a d) h} \left( \operatorname{Log}\left[\frac{a}{b} + x\right]^2 - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a + b x] + 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a + b x] - \right. \\ & \quad 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] + 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}[a - c + b x - d x] - \\ & \quad 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}[a - c + b x - d x] - 2 \operatorname{Log}\left[\frac{a}{b} + x\right] \operatorname{Log}\left[\frac{b (a - c + b x - d x)}{-b c + a d}\right] + \\ & \quad 2 \operatorname{Log}\left[\frac{c}{d} + x\right] \operatorname{Log}\left[\frac{d (a - c + b x - d x)}{-b c + a d}\right] - 2 \operatorname{Log}[a + b x] \operatorname{Log}\left[\frac{c + d x}{a + b x}\right] + \\ & \quad 2 \operatorname{Log}[a - c + b x - d x] \operatorname{Log}\left[\frac{c + d x}{a + b x}\right] - 2 \operatorname{PolyLog}\left[2, \frac{(b - d) (a + b x)}{b c - a d}\right] - \\ & \quad \left. 2 \operatorname{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] + 2 \operatorname{PolyLog}\left[2, \frac{(b - d) (c + d x)}{b c - a d}\right] \right) \end{aligned}$$

**Problem 256: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}\left[\frac{a-c g+(b-d g) x}{a+b x}\right]}{(a+b x)(c+d x)} dx$$

Optimal (type 4, 27 leaves, 2 steps):

$$\frac{\text{PolyLog}\left[2, \frac{g(c+d x)}{a+b x}\right]}{b c-a d}$$

Result (type 4, 375 leaves):

$$\begin{aligned} & \frac{1}{2 b c-2 a d}\left(-\text{Log}\left[\frac{a}{b}+x\right]^2+2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}[a+b x]-\right. \\ & 2 \text{Log}\left[\frac{a-c g}{b-d g}+x\right] \text{Log}[a+b x]+2 \text{Log}\left[\frac{a-c g}{b-d g}+x\right] \text{Log}\left[\frac{(b-d g)(a+b x)}{(b c-a d) g}\right]- \\ & 2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}[c+d x]+2 \text{Log}\left[\frac{a-c g}{b-d g}+x\right] \text{Log}[c+d x]+2 \text{Log}\left[\frac{a}{b}+x\right] \text{Log}\left[\frac{b(c+d x)}{b c-a d}\right]- \\ & 2 \text{Log}\left[\frac{a-c g}{b-d g}+x\right] \text{Log}\left[\frac{(b-d g)(c+d x)}{b c-a d}\right]+2 \text{Log}[a+b x] \text{Log}\left[\frac{a-c g+b x-d g x}{a+b x}\right]- \\ & 2 \text{Log}[c+d x] \text{Log}\left[\frac{a-c g+b x-d g x}{a+b x}\right]+2 \text{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right]+ \\ & \left. 2 \text{PolyLog}\left[2, -\frac{b(a-c g+b x-d g x)}{(b c-a d) g}\right]-2 \text{PolyLog}\left[2, -\frac{d(-a+c g-b x+d g x)}{-b c+a d}\right]\right) \end{aligned}$$

**Problem 257: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}\left[1-\frac{g(c+d x)}{a+b x}\right]}{(a+b x)(c+d x)} dx$$

Optimal (type 4, 27 leaves, 3 steps):

$$\frac{\text{PolyLog}\left[2, \frac{g(c+d x)}{a+b x}\right]}{b c-a d}$$

Result (type 4, 375 leaves):

$$\begin{aligned} & \frac{1}{2 b c - 2 a d} \left( -\text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] - \right. \\ & 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}[a + b x] + 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}\left[\frac{(b - d g)(a + b x)}{(b c - a d) g}\right] - \\ & 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] + 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}[c + d x] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\ & 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}\left[\frac{(b - d g)(c + d x)}{b c - a d}\right] + 2 \text{Log}[a + b x] \text{Log}\left[\frac{a - c g + b x - d g x}{a + b x}\right] - \\ & 2 \text{Log}[c + d x] \text{Log}\left[\frac{a - c g + b x - d g x}{a + b x}\right] + 2 \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \\ & \left. 2 \text{PolyLog}\left[2, -\frac{b(a - c g + b x - d g x)}{(b c - a d) g}\right] - 2 \text{PolyLog}\left[2, -\frac{d(-a + c g - b x + d g x)}{-b c + a d}\right] \right) \end{aligned}$$

**Problem 258: Result more than twice size of optimal antiderivative.**

$$\int \frac{\text{Log}\left[\frac{a - c g + b x - d g x}{a + b x}\right]}{(a + b x)(c + d x)} dx$$

Optimal (type 4, 27 leaves, 3 steps):

$$\frac{\text{PolyLog}\left[2, \frac{g(c + d x)}{a + b x}\right]}{b c - a d}$$

Result (type 4, 375 leaves):

$$\begin{aligned} & \frac{1}{2 b c - 2 a d} \left( -\text{Log}\left[\frac{a}{b} + x\right]^2 + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[a + b x] - \right. \\ & 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}[a + b x] + 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}\left[\frac{(b - d g)(a + b x)}{(b c - a d) g}\right] - \\ & 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}[c + d x] + 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}[c + d x] + 2 \text{Log}\left[\frac{a}{b} + x\right] \text{Log}\left[\frac{b(c + d x)}{b c - a d}\right] - \\ & 2 \text{Log}\left[\frac{a - c g}{b - d g} + x\right] \text{Log}\left[\frac{(b - d g)(c + d x)}{b c - a d}\right] + 2 \text{Log}[a + b x] \text{Log}\left[\frac{a - c g + b x - d g x}{a + b x}\right] - \\ & 2 \text{Log}[c + d x] \text{Log}\left[\frac{a - c g + b x - d g x}{a + b x}\right] + 2 \text{PolyLog}\left[2, \frac{d(a + b x)}{-b c + a d}\right] + \\ & \left. 2 \text{PolyLog}\left[2, -\frac{b(a - c g + b x - d g x)}{(b c - a d) g}\right] - 2 \text{PolyLog}\left[2, -\frac{d(-a + c g - b x + d g x)}{-b c + a d}\right] \right) \end{aligned}$$

**Problem 259: Unable to integrate problem.**

$$\int \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}])^3}{a f h + b g h x^2 + h (b f x + a g x)} dx$$

Optimal (type 4, 282 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^3 \operatorname{Log}\left[1-\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{3 B n(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^2 \operatorname{PolyLog}\left[2, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{6 B^2 n^2(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]) \operatorname{PolyLog}\left[3, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{6 B^3 n^3 \operatorname{PolyLog}\left[4, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h}
 \end{aligned}$$

Result (type 8, 53 leaves):

$$\int \frac{(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^3}{a f h+b g h x^2+h(b f x+a g x)} dx$$

### Problem 260: Result more than twice size of optimal antiderivative.

$$\int \frac{(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^2}{a f h+b g h x^2+h(b f x+a g x)} dx$$

Optimal (type 4, 203 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])^2 \operatorname{Log}\left[1-\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{2 B n(A+B \operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]) \operatorname{PolyLog}\left[2, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h} + \\
 & \frac{2 B^2 n^2 \operatorname{PolyLog}\left[3, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]}{(b f-a g) h}
 \end{aligned}$$

Result (type 4, 1415 leaves):

$$\begin{aligned}
 & \frac{1}{3(b f-a g) h} \\
 & \left(3 \operatorname{Log}[a+b x](A+B(-n \operatorname{Log}[a+b x]+n \operatorname{Log}[c+d x]+\operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]))^2 - \right. \\
 & 3(A+B(-n \operatorname{Log}[a+b x]+n \operatorname{Log}[c+d x]+\operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right]))^2 \operatorname{Log}[f+g x] + \\
 & 3 B n(A+B(-n \operatorname{Log}[a+b x]+n \operatorname{Log}[c+d x]+\operatorname{Log}\left[e(a+b x)^n(c+d x)^{-n}\right])) \\
 & \left. \left(\operatorname{Log}[a+b x]^2-2\left(\operatorname{Log}[a+b x] \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right]+\operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right]\right)\right) - \right. \\
 & 6 A B n\left(\operatorname{Log}[c+d x]\left(\operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right]-\operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right]\right) + \right. \\
 & \left. \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right]-\operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right]\right) +
 \end{aligned}$$

$$\begin{aligned}
 & 6 B^2 n \left( n \operatorname{Log}[a+b x] - n \operatorname{Log}[c+d x] - \operatorname{Log}\left[e(a+b x)^n (c+d x)^{-n}\right] \right) \\
 & \left( \operatorname{Log}[c+d x] \left( \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] - \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right] \right) + \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - \right. \\
 & \quad \left. \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right] \right) + B^2 n^2 \left( \operatorname{Log}[a+b x]^2 \left( \operatorname{Log}[a+b x] - 3 \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right] \right) - \right. \\
 & \quad \left. 6 \operatorname{Log}[a+b x] \operatorname{PolyLog}\left[2, \frac{g(a+b x)}{-b f+a g}\right] + 6 \operatorname{PolyLog}\left[3, \frac{g(a+b x)}{-b f+a g}\right] \right) + \\
 & 3 B^2 n^2 \left( \operatorname{Log}\left[\frac{d(a+b x)}{-b c+a d}\right] \operatorname{Log}[c+d x]^2 - \operatorname{Log}[c+d x]^2 \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right] + \right. \\
 & \quad 2 \operatorname{Log}[c+d x] \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{b c-a d}\right] - 2 \operatorname{Log}[c+d x] \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right] - \\
 & \quad \left. 2 \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{b c-a d}\right] + 2 \operatorname{PolyLog}\left[3, \frac{g(c+d x)}{-d f+c g}\right] \right) - \\
 & 6 B^2 n^2 \left( \frac{1}{2} \operatorname{Log}[a+b x]^2 \left( \operatorname{Log}[c+d x] - \operatorname{Log}\left[\frac{b(c+d x)}{b c-a d}\right] \right) - \operatorname{Log}[a+b x] \operatorname{Log}[c+d x] \right. \\
 & \quad \left. \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right] - \frac{1}{2} \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \left( -2 \operatorname{Log}[a+b x] + \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \right) \right. \\
 & \quad \left( \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right] - \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right] \right) + \operatorname{Log}\left[\frac{g(c+d x)}{-d f+c g}\right] \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \\
 & \quad \left( \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right] - \operatorname{Log}\left[\frac{d(f+g x)}{d f-c g}\right] \right) - \frac{1}{2} \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right]^2 \\
 & \quad \left. \left( \operatorname{Log}\left[\frac{-b c+a d}{d(a+b x)}\right] + \operatorname{Log}\left[\frac{b(f+g x)}{b f-a g}\right] - \operatorname{Log}\left[\frac{(-b c+a d)(f+g x)}{(d f-c g)(a+b x)}\right] \right) - \right. \\
 & \quad \left. \operatorname{Log}[a+b x] \operatorname{PolyLog}\left[2, \frac{d(a+b x)}{-b c+a d}\right] - \left( \operatorname{Log}[c+d x] - \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \right) \operatorname{PolyLog}\left[ \right. \right. \\
 & \quad \left. \left. 2, \frac{g(a+b x)}{-b f+a g}\right] - \left( \operatorname{Log}[a+b x] + \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \right) \operatorname{PolyLog}\left[2, \frac{g(c+d x)}{-d f+c g}\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[\frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \left( \operatorname{PolyLog}\left[2, \frac{b(c+d x)}{d(a+b x)}\right] - \operatorname{PolyLog}\left[2, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \right) \right) + \\
 & \quad \operatorname{PolyLog}\left[3, \frac{d(a+b x)}{-b c+a d}\right] + \operatorname{PolyLog}\left[3, \frac{g(a+b x)}{-b f+a g}\right] + \operatorname{PolyLog}\left[3, \frac{g(c+d x)}{-d f+c g}\right] + \\
 & \quad \left. \operatorname{PolyLog}\left[3, \frac{b(c+d x)}{d(a+b x)}\right] - \operatorname{PolyLog}\left[3, \frac{(b f-a g)(c+d x)}{(d f-c g)(a+b x)}\right] \right) \right)
 \end{aligned}$$

### Problem 261: Result more than twice size of optimal antiderivative.

$$\int \frac{A+B \operatorname{Log}\left[e(a+b x)^n (c+d x)^{-n}\right]}{a f h+b g h x^2+h(b f x+a g x)} d x$$

Optimal (type 4, 123 leaves, 6 steps):

$$- \frac{(A + B \text{Log}[e (a + b x)^n (c + d x)^{-n}]) \text{Log}\left[1 - \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h} + \frac{B n \text{PolyLog}\left[2, \frac{(b f - a g) (c + d x)}{(d f - c g) (a + b x)}\right]}{(b f - a g) h}$$

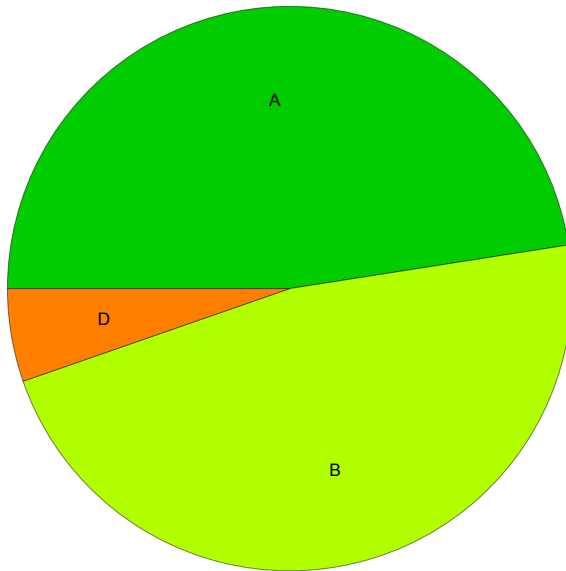
Result (type 4, 303 leaves):

$$- \frac{1}{(2 b f - 2 a g) h} \left( -2 A \text{Log}[a + b x] + B n \text{Log}[a + b x]^2 - 2 B n \text{Log}[a + b x] \text{Log}[c + d x] + \right. \\ \left. 2 B n \text{Log}\left[\frac{d (a + b x)}{-b c + a d}\right] \text{Log}[c + d x] - 2 B \text{Log}[a + b x] \text{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] + \right. \\ \left. 2 A \text{Log}[f + g x] - 2 B n \text{Log}[a + b x] \text{Log}[f + g x] + 2 B n \text{Log}[c + d x] \text{Log}[f + g x] + \right. \\ \left. 2 B \text{Log}\left[e (a + b x)^n (c + d x)^{-n}\right] \text{Log}[f + g x] + 2 B n \text{Log}[a + b x] \text{Log}\left[\frac{b (f + g x)}{b f - a g}\right] - \right. \\ \left. 2 B n \text{Log}[c + d x] \text{Log}\left[\frac{d (f + g x)}{d f - c g}\right] + 2 B n \text{PolyLog}\left[2, \frac{g (a + b x)}{-b f + a g}\right] + \right. \\ \left. 2 B n \text{PolyLog}\left[2, \frac{b (c + d x)}{b c - a d}\right] - 2 B n \text{PolyLog}\left[2, \frac{g (c + d x)}{-d f + c g}\right] \right)$$



## Summary of Integration Test Results

263 integration problems



A - 125 optimal antiderivatives

B - 124 more than twice size of optimal antiderivatives

C - 0 unnecessarily complex antiderivatives

D - 14 unable to integrate problems

E - 0 integration timeouts